



# Measurement of $\gamma\gamma^* \rightarrow \pi^0$ Transition Form Factor at Belle



Sadaharu Uehara (KEK)

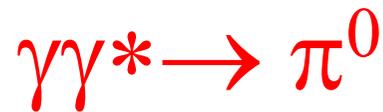
The Belle Collaboration

*Meson TFF Workshop, 29-30 May, 2012*

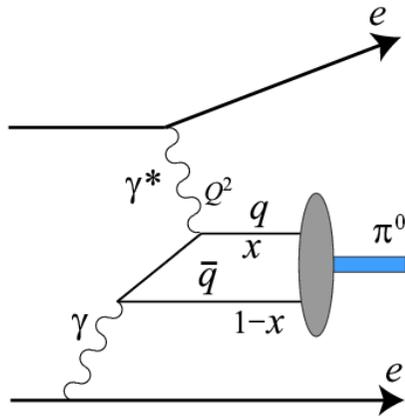
*MESON2012, 31 May – 5 June, 2012*

*Jagiellonian University, Kraków*

# $\pi^0$ Transition Form Factor



Coupling of neutral pion with two photons  
Good test for QCD at high  $Q^2$



Single-tag  $\pi^0$  production in two-photon process with a large- $Q^2$  and a small- $Q^2$  photon

Theoretically calculated from pion distribution amplitude and decay constant

$$F(Q^2) = \frac{\sqrt{2}f_\pi}{3} \int T_H(x, Q^2, \mu) \phi_\pi(x, \mu) dx$$

Measurement:

$$|F(Q^2)|^2 = |F(Q^2, 0)|^2 = (d\sigma/dQ^2)/(2A(Q^2)) \quad A(Q^2) \text{ is calculated by QED}$$

$$|F(0, 0)|^2 = 64\pi\Gamma_{\gamma\gamma}/\{(4\pi\alpha)^2 m_R^3\}$$

Detects  $e$  (tag side) and  $\pi^0$

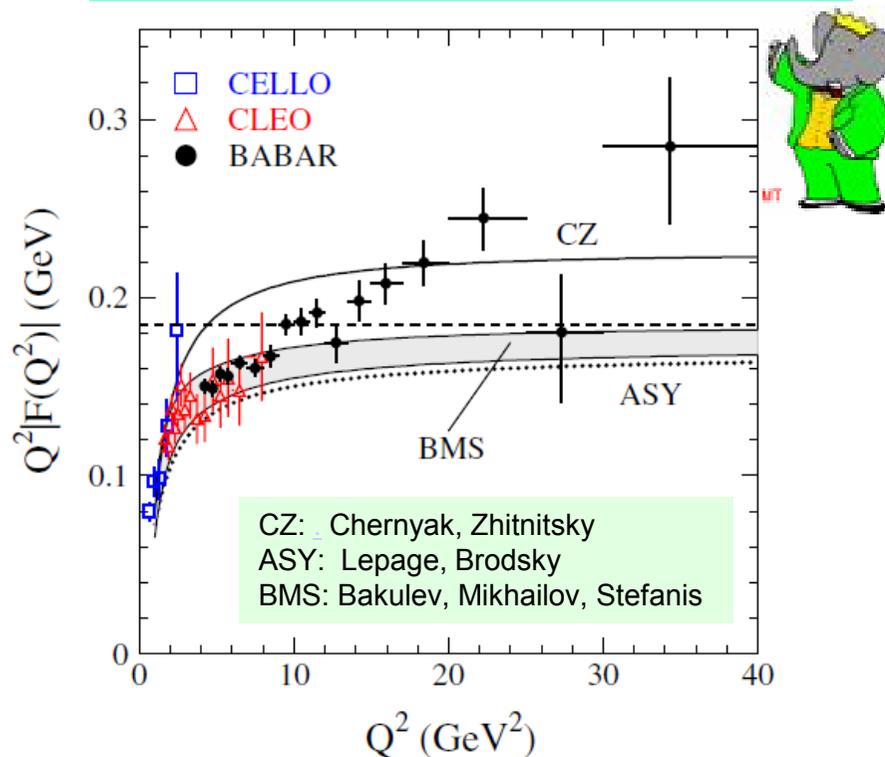
$Q^2 = 2EE'(1 - \cos \theta)$  from energy and polar angle of the tagged electron



# BaBar's Measurement

$\pi^0$  transition form factor (TFF) measured by BaBar is larger than the asymptotic pQCD prediction above  $Q^2 > 10 \text{ GeV}^2$

BaBar, PRD 80, 052009 (2009)  $442 \text{ fb}^{-1}$



Below  $Q^2 < 8 \text{ GeV}^2$ , the BaBar result supports the CLEO result.

$\eta$  and  $\eta'$  TFFs from BaBar PRD 84, 052001(2011) are consistent with QCD predictions.

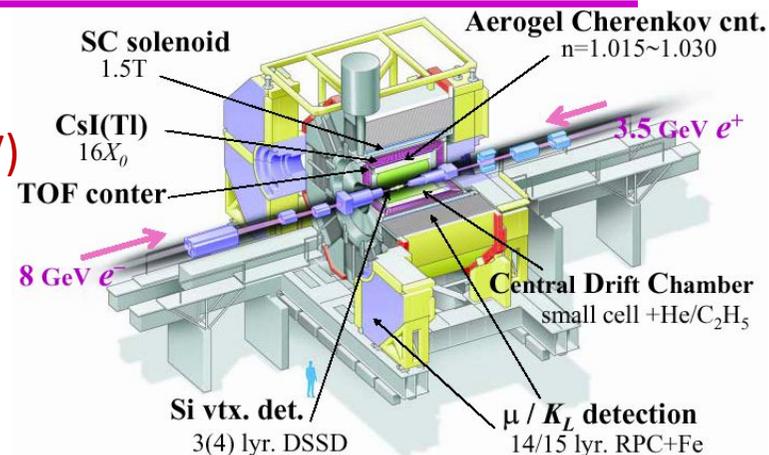
Explanation within standard QCD calculations is difficult.



# Measurement of $\pi^0$ TFF at Belle

## KEKB accelerator and Belle detector

Asymmetric for beam energy ( $e^+$ : 3.5 GeV,  $e^-$ : 8 GeV)  
for kinematic coverage of  
 $e^+$ -tag(**p-tag**) and  $e^-$ -tag(**e-tag**)

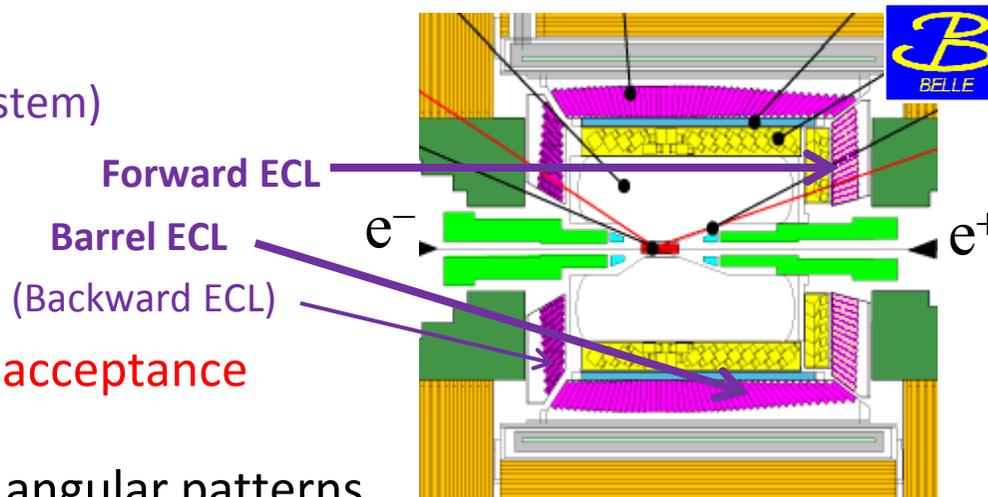


## Available Triggers:

### HiE & Bhabha(-veto)

by ECL (electromagnetic calorimeter system)

HiE ---  $E(\text{Forward}+\text{Barrel}) > 1.15 \text{ GeV}$



**Bhabha-veto logic** kills a part of the acceptance

Significant loss of efficiency for some angular patterns

in contrast to BaBar, where a special salvaging logic was prepared.

Int. Luminosity :  $759 \text{ fb}^{-1}$  (Larger than BaBar's)



# Selection Criteria for Signal Events

- Triggered by HiE or CsIBB(≡Bhabha prescaled by factor 50)
- **1 good track only, Electron-ID**  $E/p > 0.8$ ,  $p_e > 1.0 \text{ GeV}/c$  in lab. system
- **2 Photons from  $\pi^0$**   $E_{\gamma i} > 0.2 \text{ GeV}$ ,  $E_{\gamma\gamma} \equiv E_{\gamma 1} + E_{\gamma 2} > 1.0 \text{ GeV}$

No big energy asymmetry:  $|E_{\gamma 1} - E_{\gamma 2}| / E_{\gamma\gamma} < 0.8$

Polar-angle difference:  $\Delta\theta \equiv |\theta_{\gamma 1} - \theta_{\gamma 2}| > \frac{0.18 \text{ [rad}\cdot\text{GeV]}}{E_{\gamma\gamma}}$

To reject large background from Radiative Bhabha ( $e\gamma$ ) process

- Polar- angle of the electron and the two photons  
 $-0.6235 < \cos \theta < +0.9481$  and **Bhabha Mask cut**

- **e-charge vs.  $p_z$  direction correlation**

$$-Q_{\text{tag}} (p_z^* e + p_z^* \gamma\gamma) > 0 \quad (* \text{ --- } e^+e^- \text{ c.m.s.})$$

- **3-body kinematical cut for  $\pi^0$  energy  $E_{\gamma\gamma}^*$**

Energy-momentum conservation using direction of  $\mathbf{p}_{\gamma\gamma}$ , and  $m_{\gamma\gamma} = m_{\pi^0}$

$$0.85 < (E_{\text{ratio}} \equiv E_{\gamma\gamma}^* \text{ measured} / E_{\gamma\gamma}^* \text{ expected}) < 1.1$$

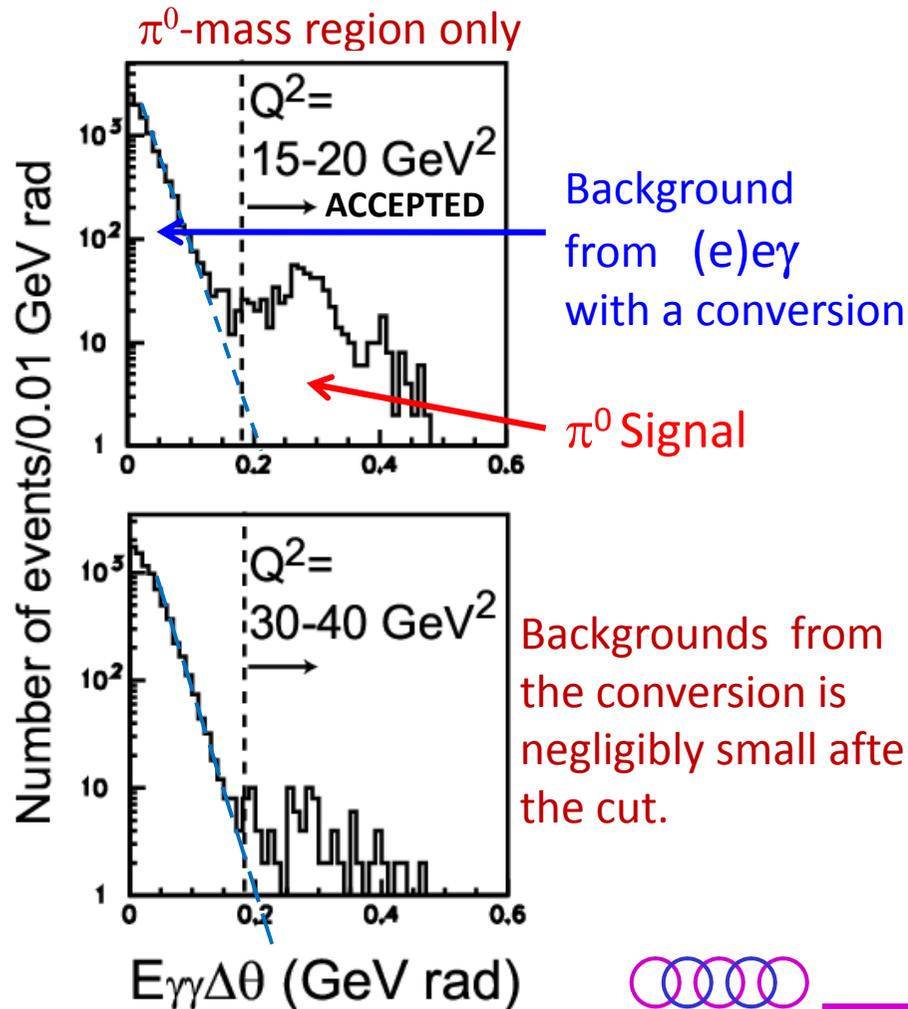
- Bhabha-background rejection, Acollinearity angle( $e, \gamma\gamma$ )  $< 177^\circ$  in  $e^+e^-$  c.m. frame
- **Good balances in azimuthal angle and  $p_t$  between e and  $\pi^0$**

Acoplanarity angle( $e, \gamma\gamma$ )  $< 0.1 \text{ rad}$ ,  $|\Sigma \mathbf{p}_t| < 0.2 \text{ GeV}/c$

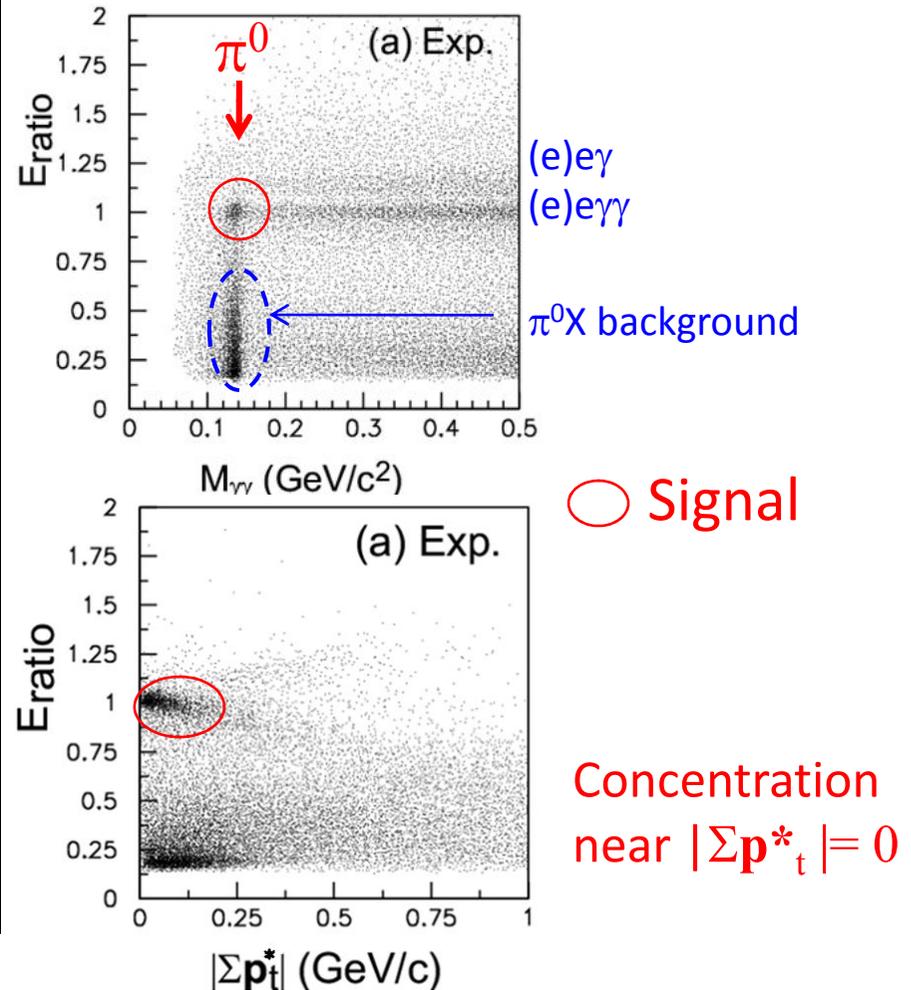


# Background rejection and signal enhancement

$\Delta\theta$  : Polar-angle difference of  $\gamma\gamma$   
is used to reject 2 clusters from  $\gamma \rightarrow ee$



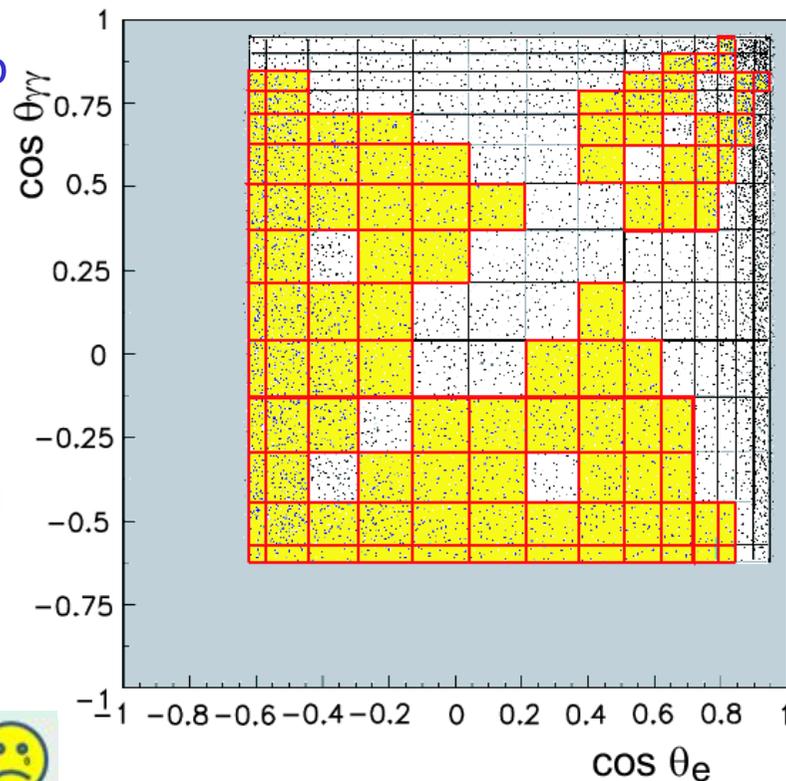
$$E_{\text{ratio}} \equiv E_{\gamma\gamma}^* \text{ measured} / E_{\gamma\gamma}^* \text{ expected}$$



# Bhabha Mask; Unbiased sample

## Bhabha-Mask criteria (Yellow regions for selection)

masks low-efficiency regions due to Bhabha veto  
in  $(\cos \theta_e, \cos \theta_{\gamma\gamma})$   
to reduce uncertainty from trigger inefficiency



## Unbiased sample using CsIBB trigger (1/50)

Effects from the Bhabha-veto is compensated in

**Nevent(HiE) + 50\*Nevent(CsIBB)**

≡ “Unbiased sample”



Statistically too small for the signal analysis



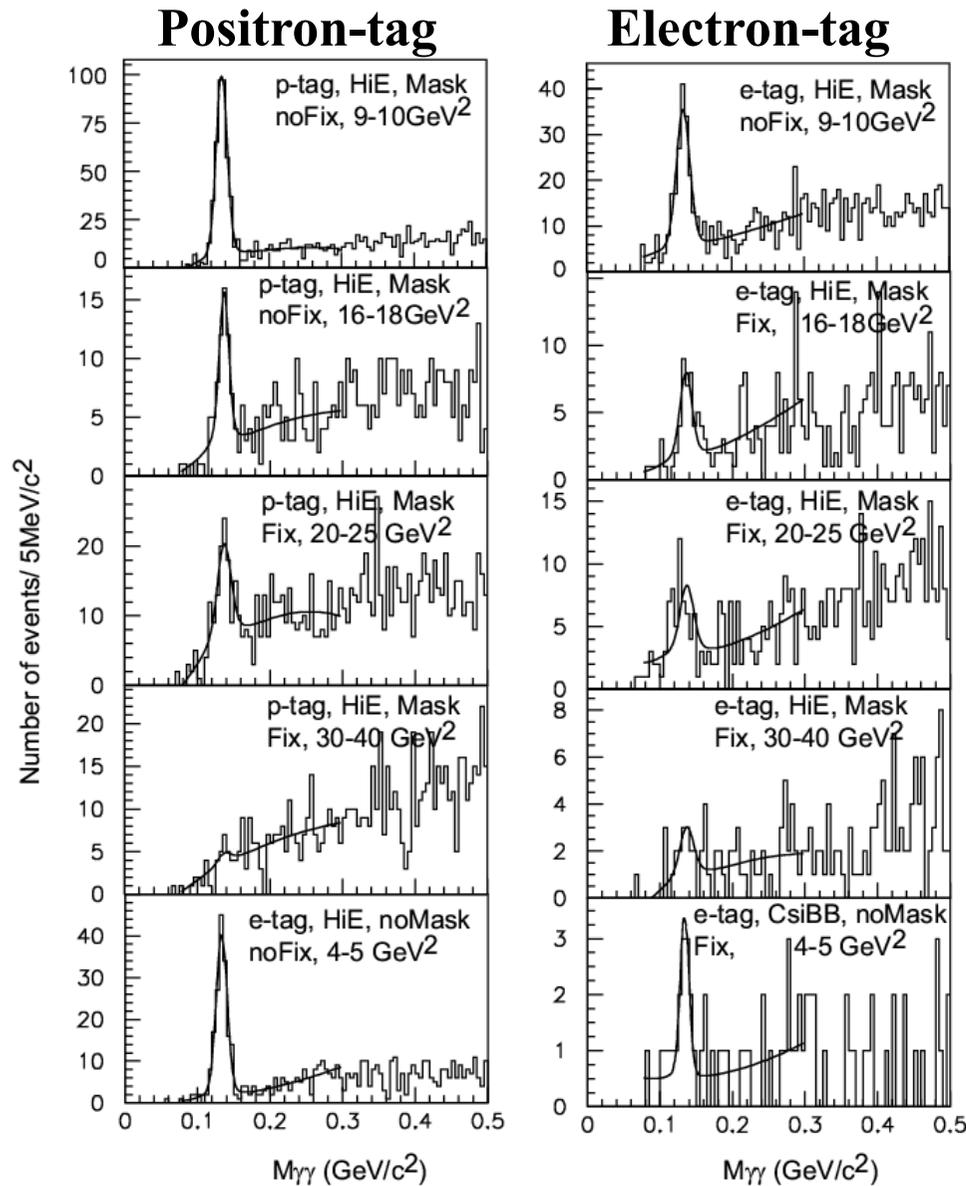
e-tag  $4 < Q^2 < 6 \text{ GeV}^2$  : HiE+50\*CsIBB sample

other regions: HiE sample only

Extensively used for tuning and evaluation of the trigger simulator



# Extraction of $\pi^0$ Yield



Fit  $M_{\gamma\gamma}$  distribution by  
 Double Gaussian (for signal)  
 + 2<sup>nd</sup>-Order Polynomial (for background)  
 in each  $Q^2$  bin

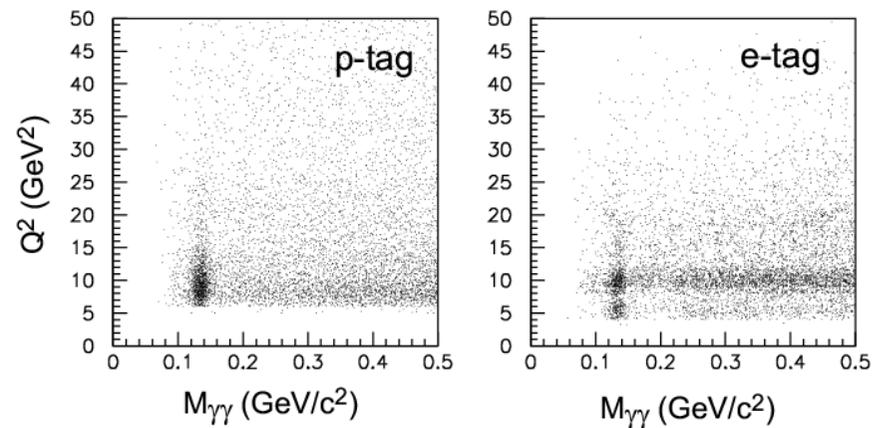
$\pi^0$ -mass resolution

the narrower Gaussian component

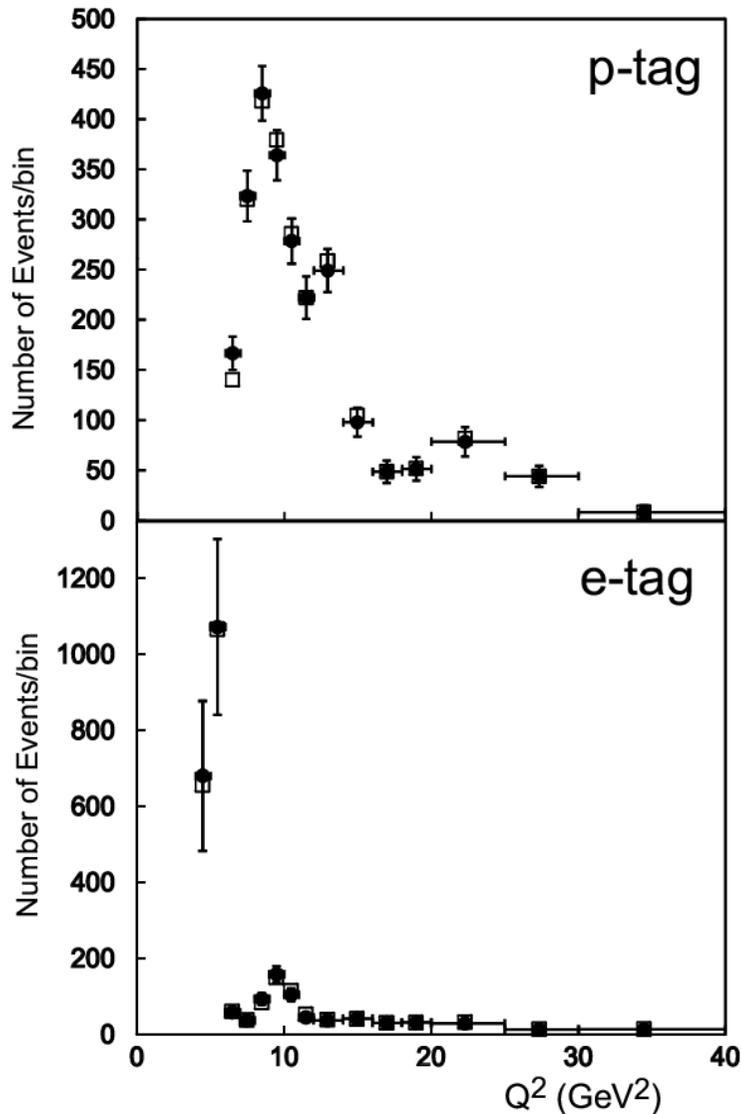
6 – 9 MeV (dependent on  $Q^2 = 4 - 40$  GeV<sup>2</sup>)

consistent between the exp. and MC

the wider  $\sim 2.4$  times larger than the narrower



# Signal Yields ; $Q^2$ Unfolding



**$Q^2$  – unfolding is applied**  
using **inverted migration matrix**  
that takes into account the effects from:

- Detector resolution
- ISR at the tagged electron

## Signal yields

- Before the unfolding
- After the unfolding



# Calibration of Bhabha-veto Thresholds using Radiative-Bhabha (VC) Events

Bhabha-veto threshold is measured in real data  
of **Virtual-Compton process of (e)e $\gamma$**   
and is tuned in Trigger Simulator

MC generator **Rabhat** treats  $t$ -channel mass singularity

Comput. Phys. Commun. 55, 337 (1989)

VC process has a similar topology to the signal process

Require a single  $\gamma$  instead of  $\pi^0$

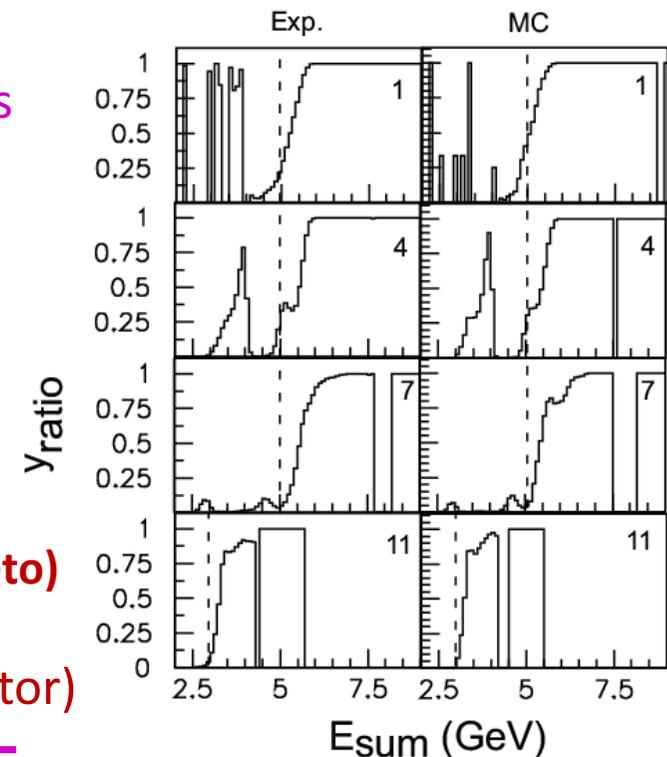
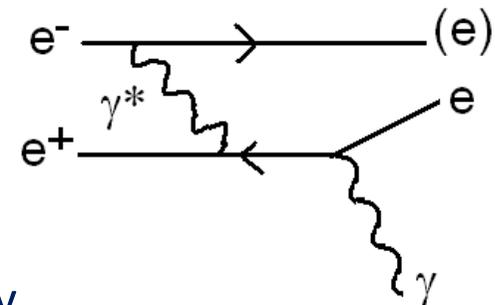
Big cross section ( $\sim O(1\text{nb})$ )

In **unbiased sample**, enough statistics available 😊

Bhabha-veto condition:  $\Sigma E(\text{at least one of 11 patterns}) > E_{\text{thres}}$

$$Y_{\text{ratio}} = \frac{50 \cdot N(\text{CsiBB})}{N(\text{HiE}) + 50 \cdot N(\text{CsiBB})}$$

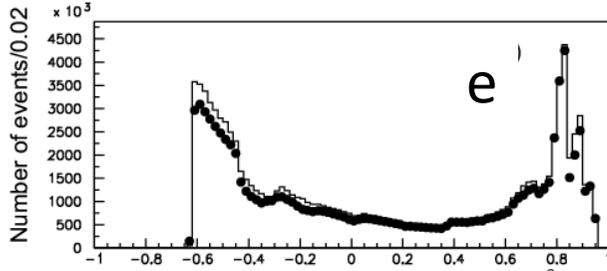
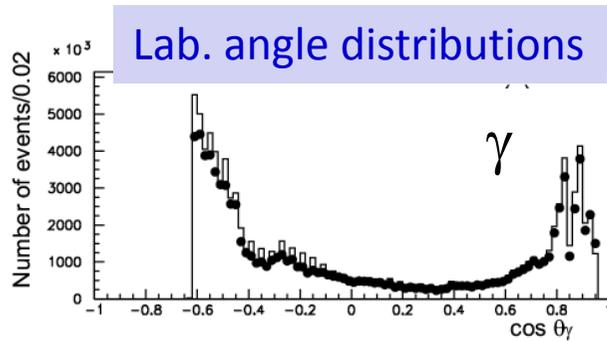
**Trigger Efficiency for Bhabha (-veto)**  
as a function of energy deposit  
→ tune MC (trigger simulator)



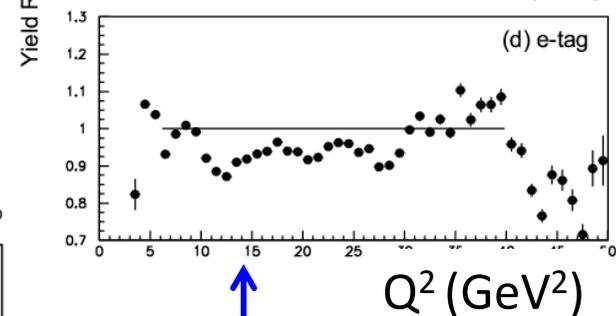
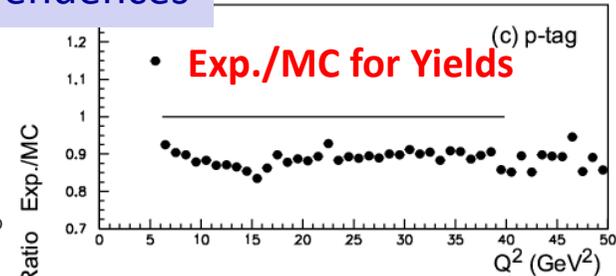
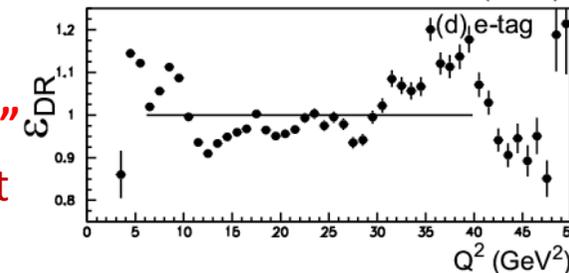
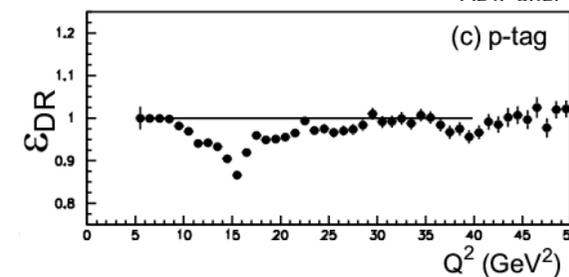
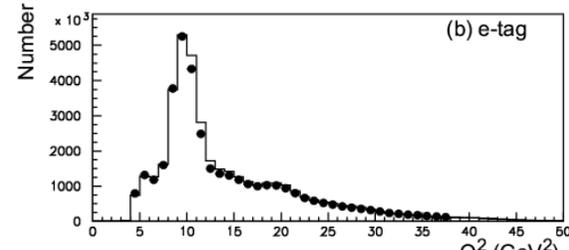
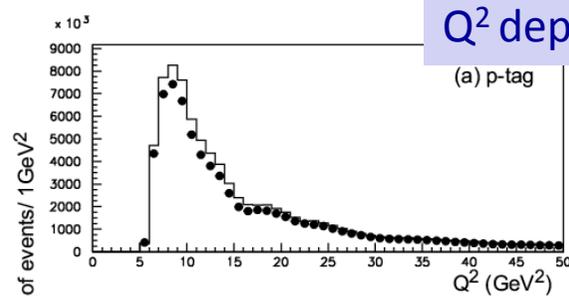
# Comparisons in Radiative Bhabha (VC) samples

MC (Rabhat) is normalized by int. luminosity

For HiE (Bhabha-Masked) sample Lowest order-only --  $\delta(\text{rad. corr.}) \sim -6\% (\pm 4\%)$  applied



dots: Exp.  
histograms: MC

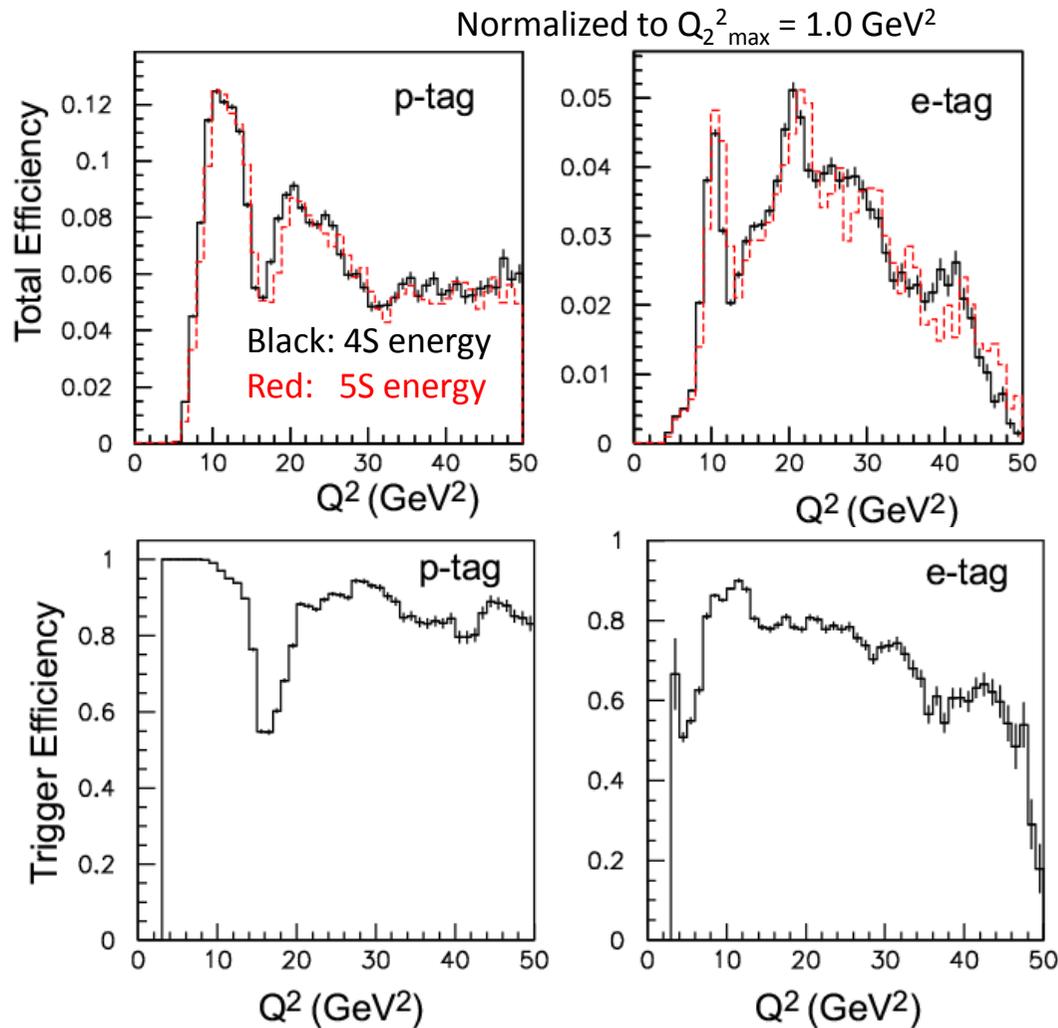


Horizontal line (=1): Expectation  
5-10% disagreement is explained  
by uncertainties in radiative  
correction and systematic  
uncertainty in the measurement

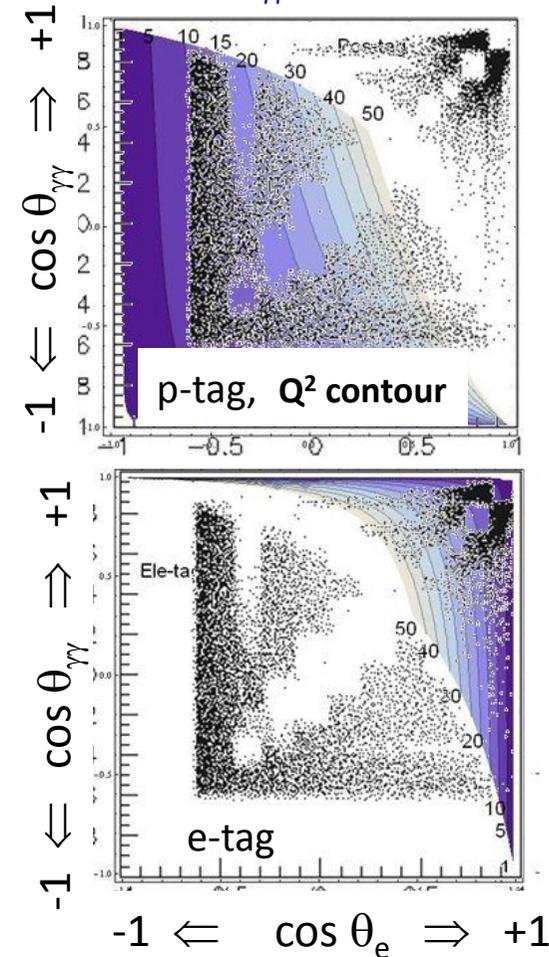
$\epsilon_{DR}$ :  
Exp./MC Ratio for Efficiency for  
"Bhabha-Mask"  $\times$  "Bhabha-veto"  
shows a better agreement  
between Exp. and MC

# Efficiency for the Signal Process

Efficiency determined by MC  
(twice of BaBar's definition)



Up-down structures are reflection of  
Bhabha-mask and -veto correlated to  
 $Q^2$  in  $(\cos\theta_e, \cos\theta_{\gamma\gamma})$  plane



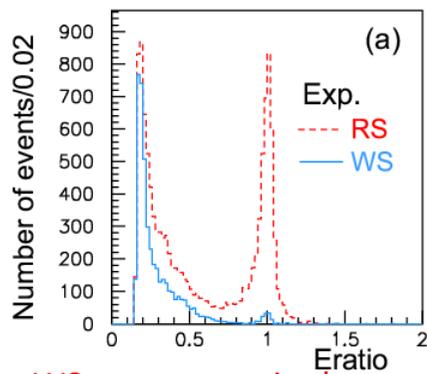
The trigger efficiency is defined for the acceptance  
after the selection



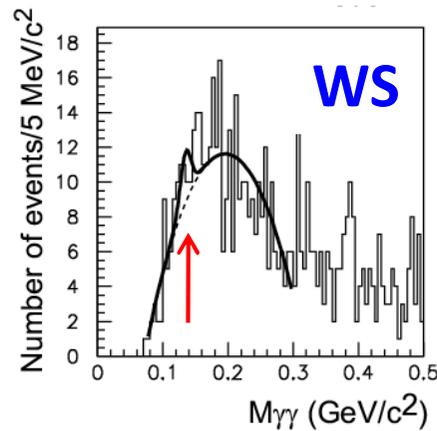
# Peaking ( $\pi^0$ ) Backgrounds

(e)e $\pi^0$ X --- Backgrounds peaking at the pion mass,  
 which leak near to ( $E_{\text{ratio}}=1, |\Sigma p_t|=0$ )

**(1) Study of wrong-sign events** (defined by the charge vs. z-direction correlation)



WS component in the signal region is very small



Noise from Signal Process

**No  $\pi^0$  is there** ( $1.2 \pm 0.9$  events)

Backgrounds from  $e^+e^-$  annihilation and particle misidentification (of muon or hadron) are **negligibly small**.

**(2) Background processes**

$\gamma\gamma^* \rightarrow \pi^0\pi^0$

$ee \rightarrow (e)e \rho^0/\omega, \rho^0/\omega \rightarrow \pi^0\gamma$

are **experimentally observed**

**We build background MC's**

normalized to these observations

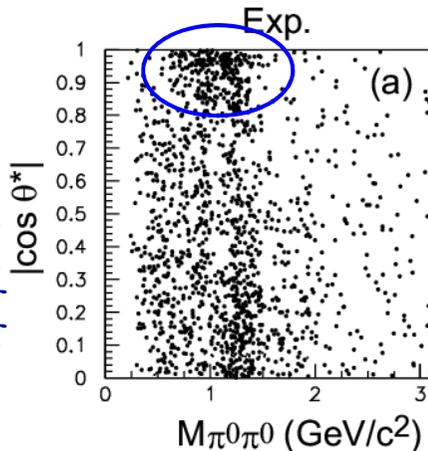
**Background contamination estimated**

$\pi^0\pi^0$ : 2% uniformly for  $Q^2$

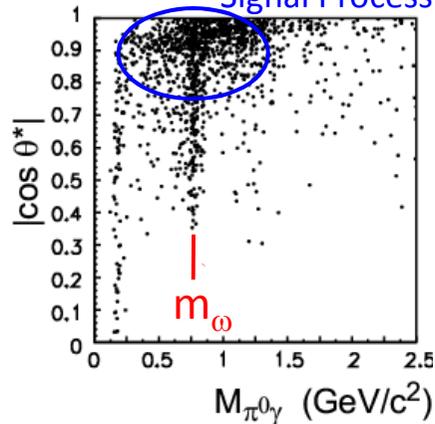
$\pi^0\gamma$ : 0.8% @  $Q^2 < 12 \text{ GeV}^2$

1–3% @ 12–40  $\text{GeV}^2$

c.m. scattering angle  
wrt  $\gamma^*\gamma$  axis



wrt  $\pi^0\gamma$  direction

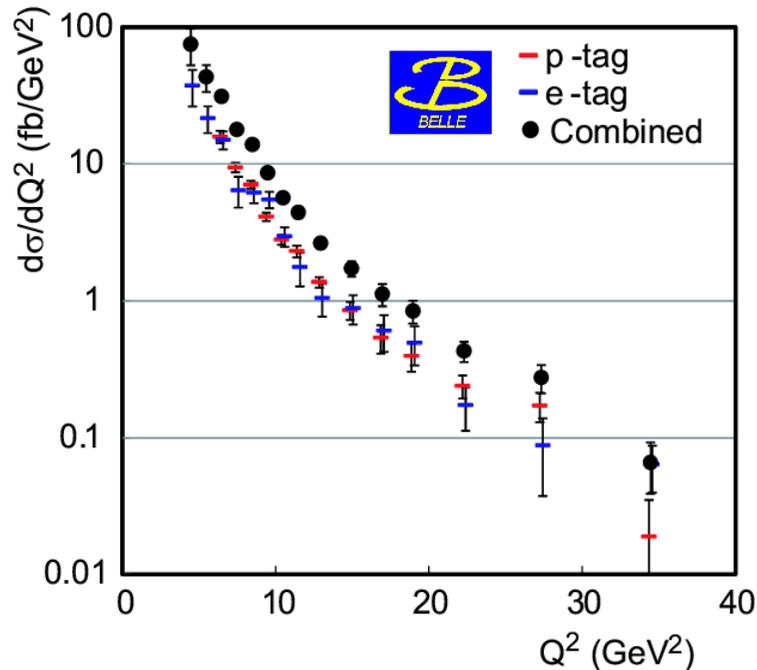


# Cross Section

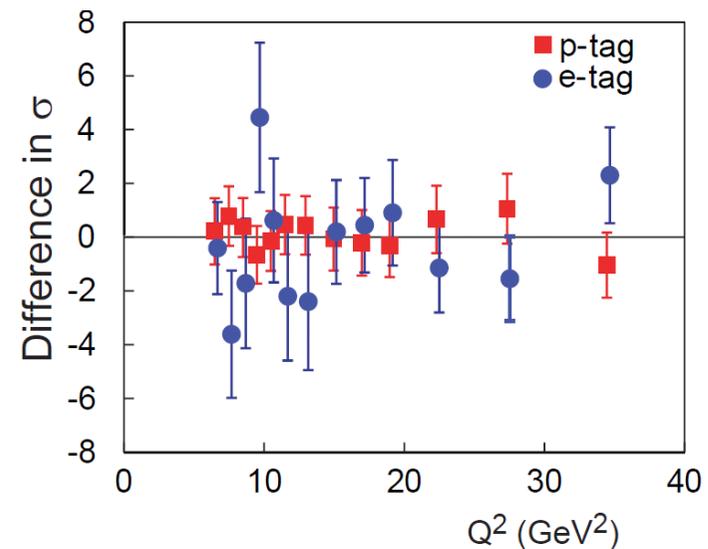
$$\frac{d\sigma}{dQ^2} = \frac{N (1-r_b)}{\int L dt \text{ eff } B(\pi^0 \rightarrow \gamma\gamma) (1+\delta) \Delta Q^2}$$

$r_b$ : background fraction  
 eff -- signal selection efficiency  
 d : radiative correction = +2%

The cross sections from p-tag and e-tag are evaluated, separately, and then combined.



$Q^2_{\max} = 1.0 \text{ GeV}^2$  for the less-virtual photon  
 Corrected for  $\sqrt{s} = 10.58 \text{ GeV}$

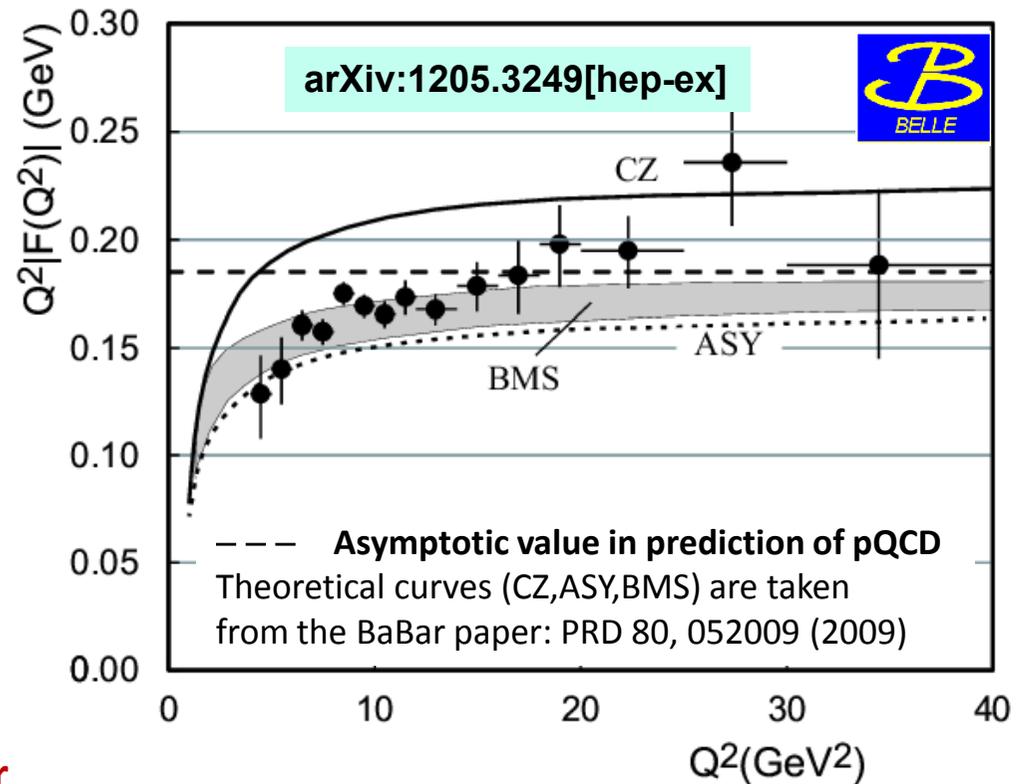
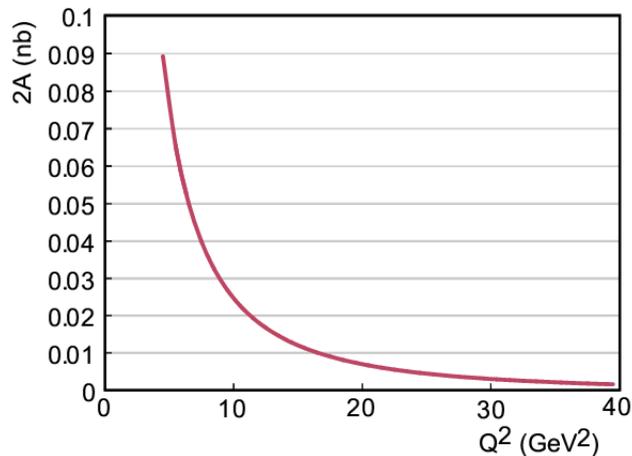


No systematic bias found between the p-tag and e-tag results.



# Transition Form Factor

$$Q^2 |F(Q^2)| = Q^2 \sqrt{(d\sigma/dQ^2)/(2A(Q^2))}$$



Representative value  $\bar{Q}^2$  is used for

$Q^2$  point that gives the cross section with the same size as the mean over the bin calculated using an approximated dependence,  $d\sigma/dQ^2 \sim Q^{-7}$



# Systematic Uncertainties

## For Cross Section:

Q <sup>2</sup> independent:	Tracking	1%	
	e-ID	1%	
	$\gamma\gamma$ reconstruction	3%	
	kinematical selection	2%	
	geometrical selection	2%	
	beam background	2%	
	integrated luminosity	1.4%	
	radiative correction	3%	
	form-factor effect	1.0%	
			( subtotal 6%)
Q <sup>2</sup> dependent:	Extraction of $\pi^0$ -yield	5–10%	estimated variation of fit (single Gauss + linear fit)
	Trigger efficiency	2–12%	
			estimated by studies of trigger threshold & Rad.Bhabha events
	Peaking-background	1 – 4%	8 – 14% in total

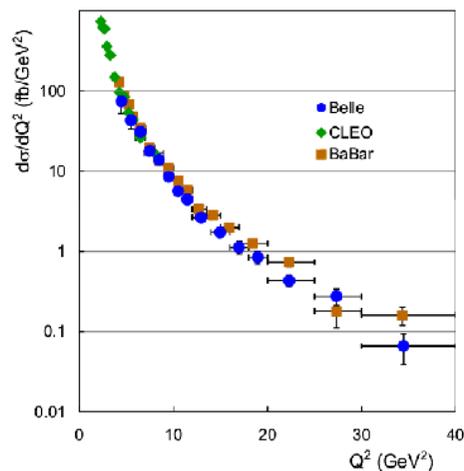
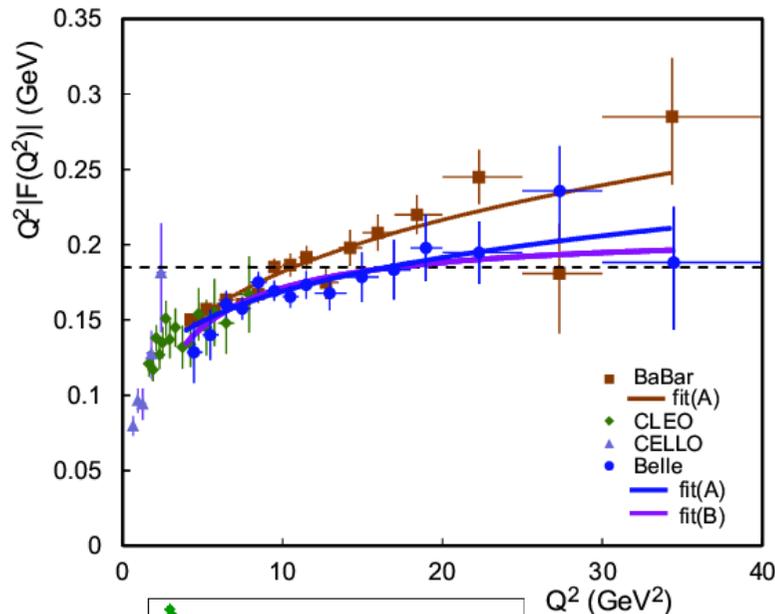
## For Transition Form Factor:

Half of the above values, as  $|F| \sim \sqrt{d\sigma/dQ^2}$

with **added by an** uncertainty of  $2A(Q^2) \sim 2\%$  (form-factor effect for the low-Q<sup>2</sup>photon)



# Comparisons with Previous Measurements and Fits



## Fit A (suggested by BaBar)

$$Q^2|F(Q^2)| = A (Q^2/10\text{GeV}^2)^\beta$$

BaBar: —

$$A = 0.182 \pm 0.002 (\pm 0.004) \text{ GeV}$$

$$\beta = 0.25 \pm 0.02$$

Belle: —

$$A = 0.169 \pm 0.006 \text{ GeV}$$

$$\beta = 0.18 \pm 0.05$$

$$\chi^2/\text{ndf} = 6.90/13 \quad \sim 1.5\sigma \text{ difference from BaBar}$$

## Fit B (with an asymptotic parameter)

$$Q^2|F(Q^2)| = BQ^2/(Q^2+C)$$

Belle: —

$$B = 0.209 \pm 0.016 \text{ GeV}$$

$$C = 2.2 \pm 0.8 \text{ GeV}^2$$

$$\chi^2/\text{ndf} = 7.07/13$$

B is consistent with the QCD value (0.185 GeV)

No rapid growth above  $Q^2 > 9 \text{ GeV}^2$  is seen in Belle result.



# Summary

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- The  $\pi^0$  transition form factor is measured at Belle in the range,  $4 \text{ GeV}^2 \lesssim Q^2 \lesssim 40 \text{ GeV}^2$ .

There was a significant effect from Bhabha-veto, but the trigger simulator to estimate the signal efficiency is tuned, reliably, calibrating it using radiative Bhabha events.

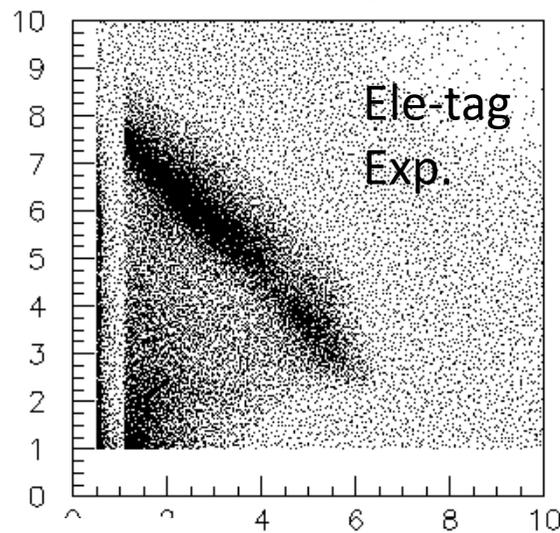
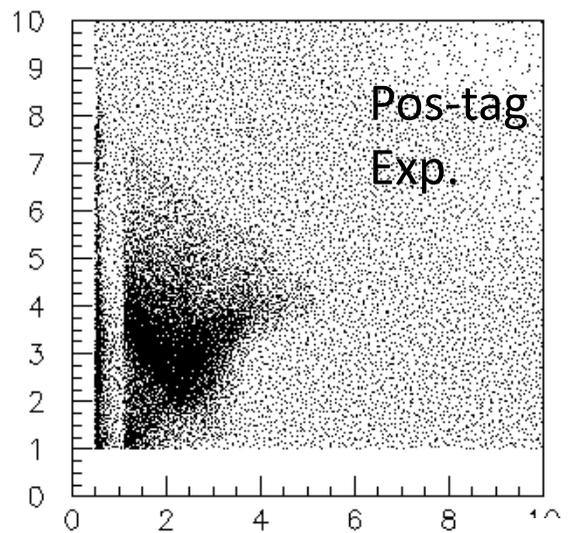
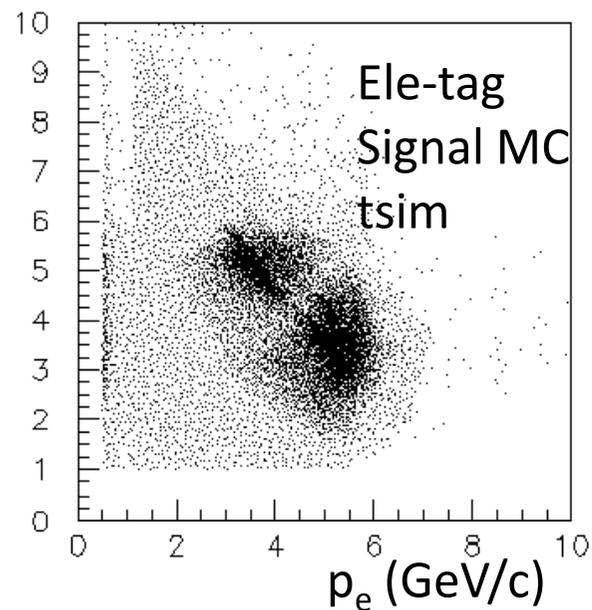
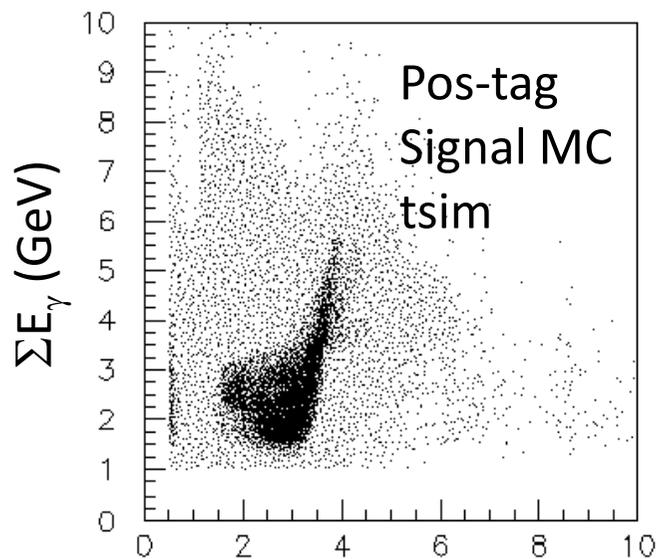
- No rapid growth of  $\pi^0$  TFF is observed for the region  $Q^2 > 9 \text{ GeV}^2$ .
- Phenomenological fits are applied for  $Q^2$  dependence of  $\pi^0$  TFF.

**Belle**  
**arXiv:1205.3249[hep-ex] (2012)**  
**Submitted to Phys. Rev. D**



Backup

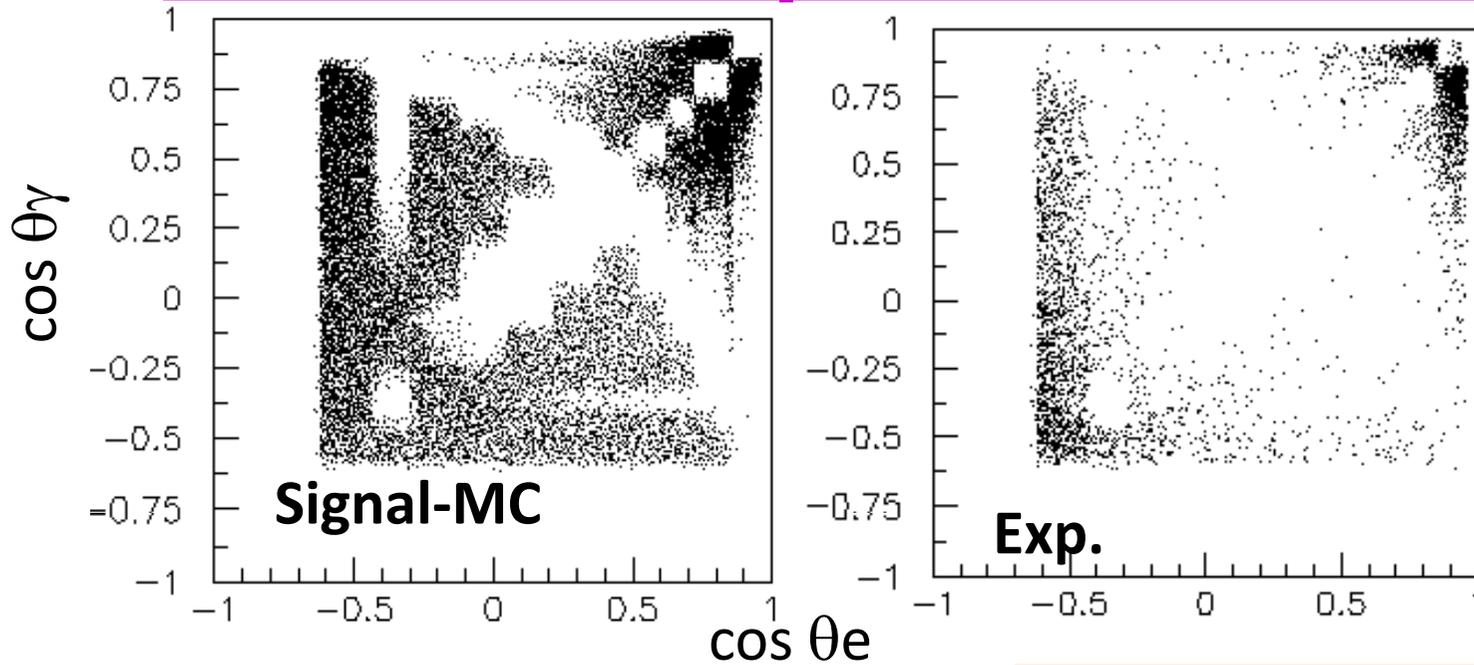
# Energy-correlations in the skim file, $\Sigma E_\gamma > 1.0$ GeV



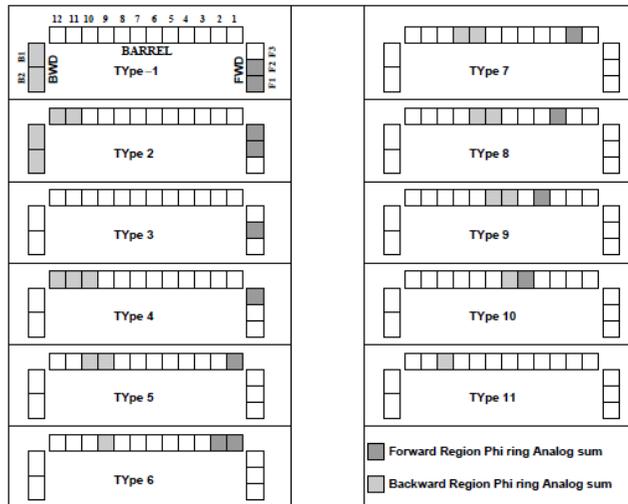
Similar distribution to  
Signal-MC.

But, the exp. events are  
dominated by backgrounds  
(Radiative Bhabha )

# Effect of Bhabha-veto in angle correlation



Bhabha-mask is not applied



Bhabha-veto patterns in trigger

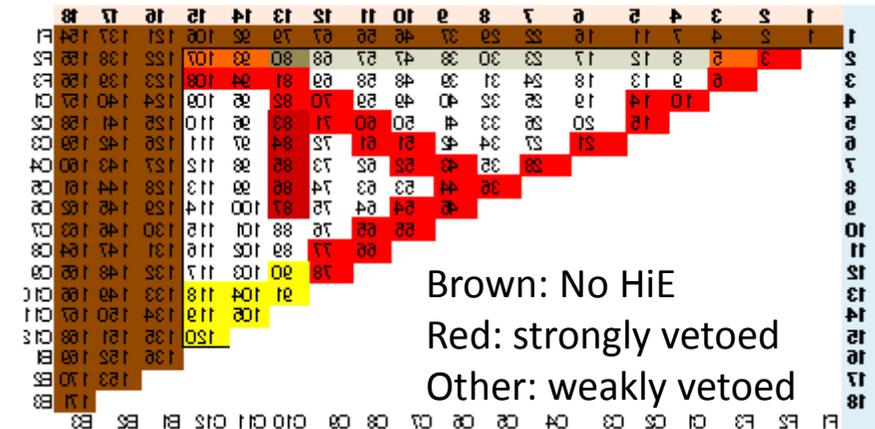


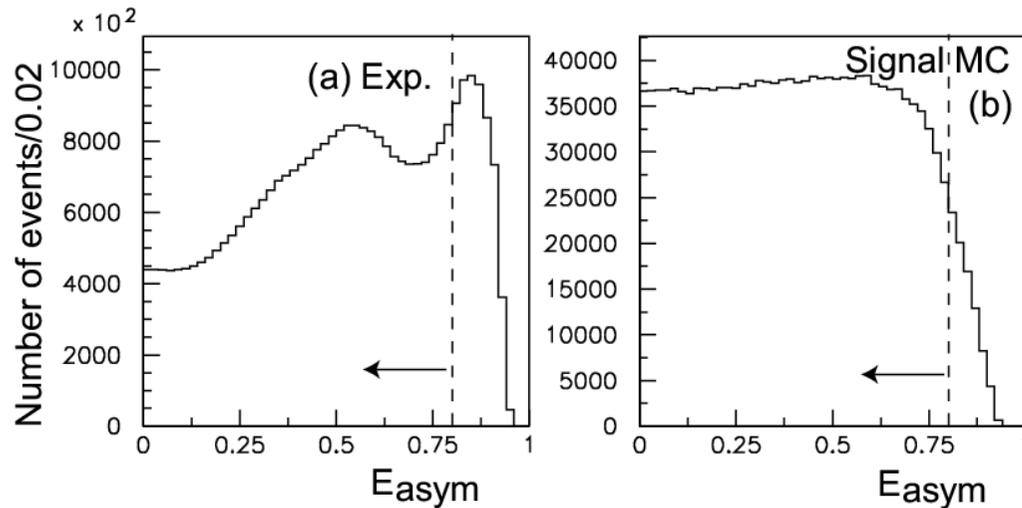
Fig. 4. Eleven types of Bhabha triggers based on each  $\phi$ -ring sum.



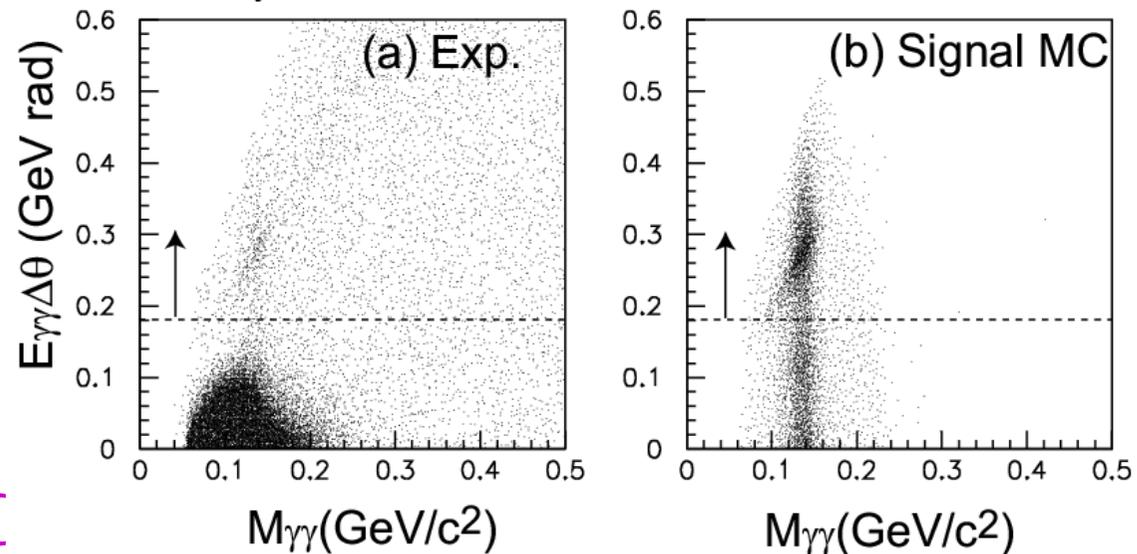
# $\gamma\gamma$ from $\pi^0$ and from backgrounds

## Energy asymmetry

to reject low-energy photon background

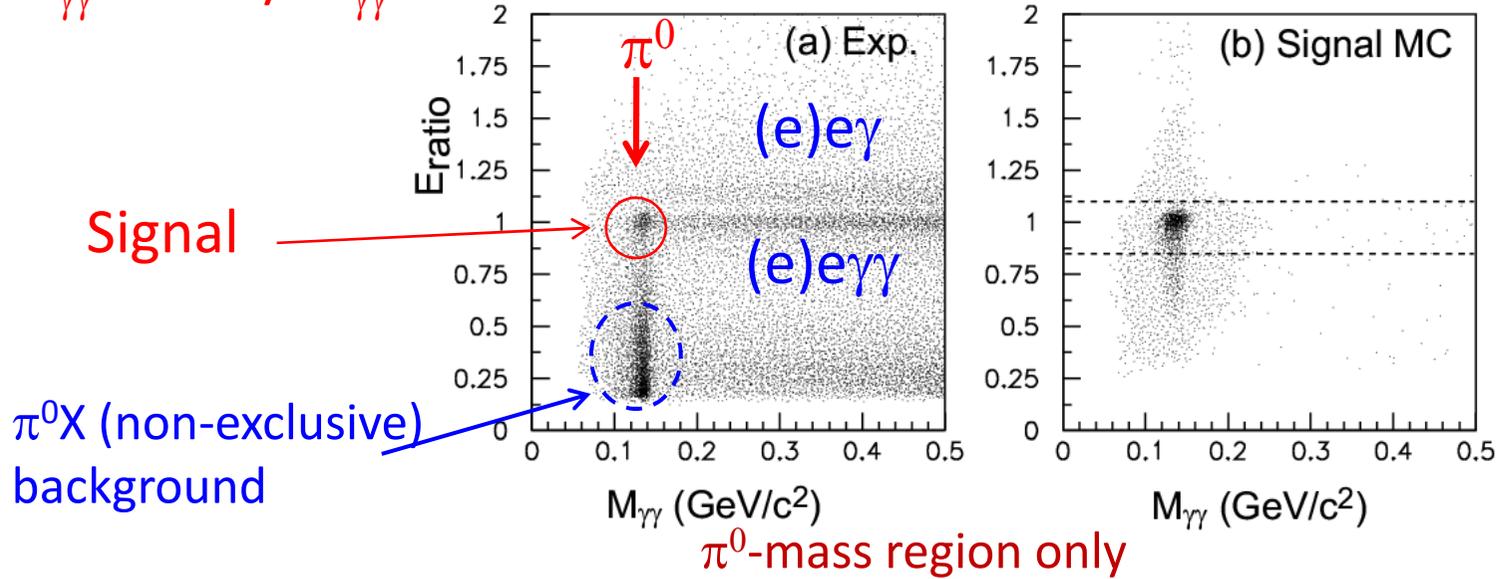


$\Delta\theta$  – Polar-angle difference of  $\gamma\gamma$   
Used to reject 2 clusters from  $\gamma \rightarrow ee$

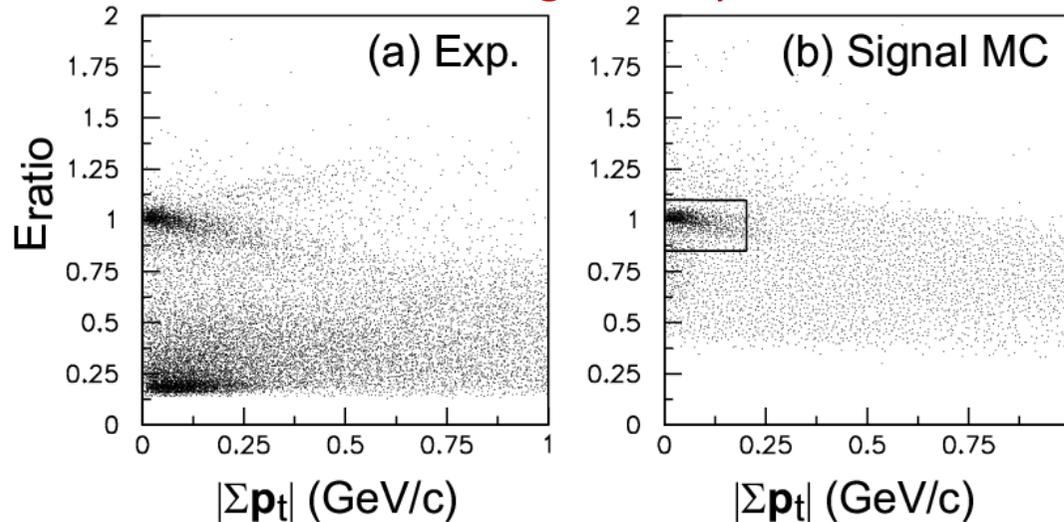


# Kinematical Criteria

$$E_{\text{ratio}} \equiv E_{\gamma\gamma}^* \text{ measured} / E_{\gamma\gamma}^* \text{ expected}$$

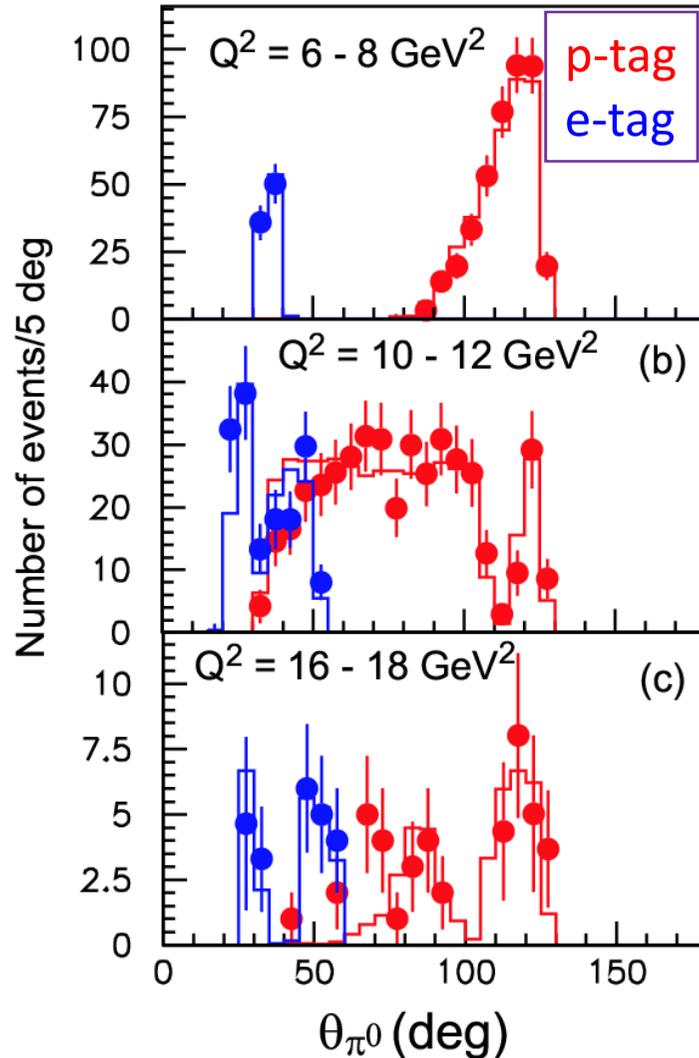


Concentration near  $\Sigma \mathbf{p}_t = 0$

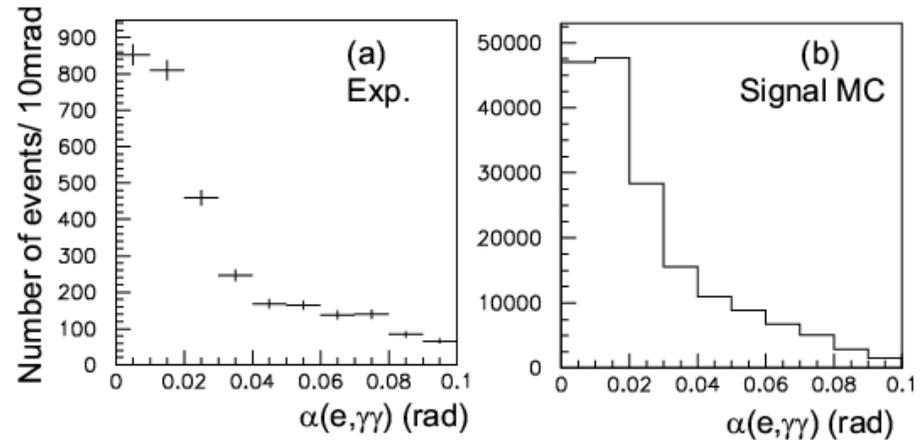


# Checks of Signal Details

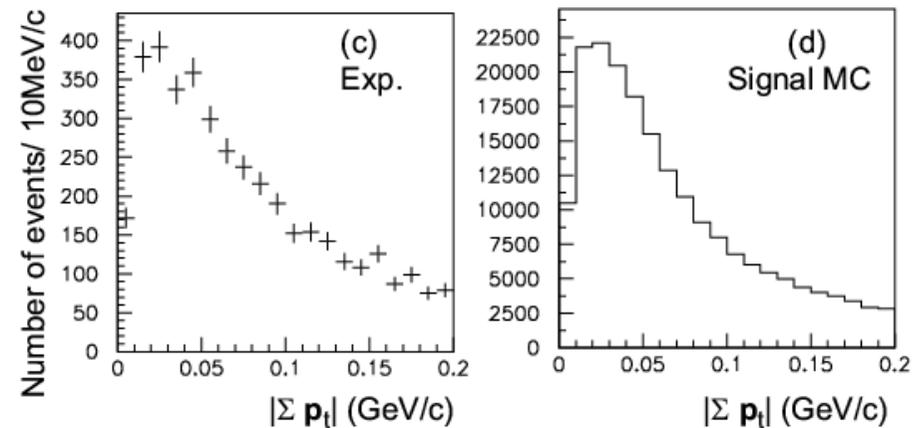
## $\pi^0$ -angle distribution



## Radiative tails Acoplanarity angle

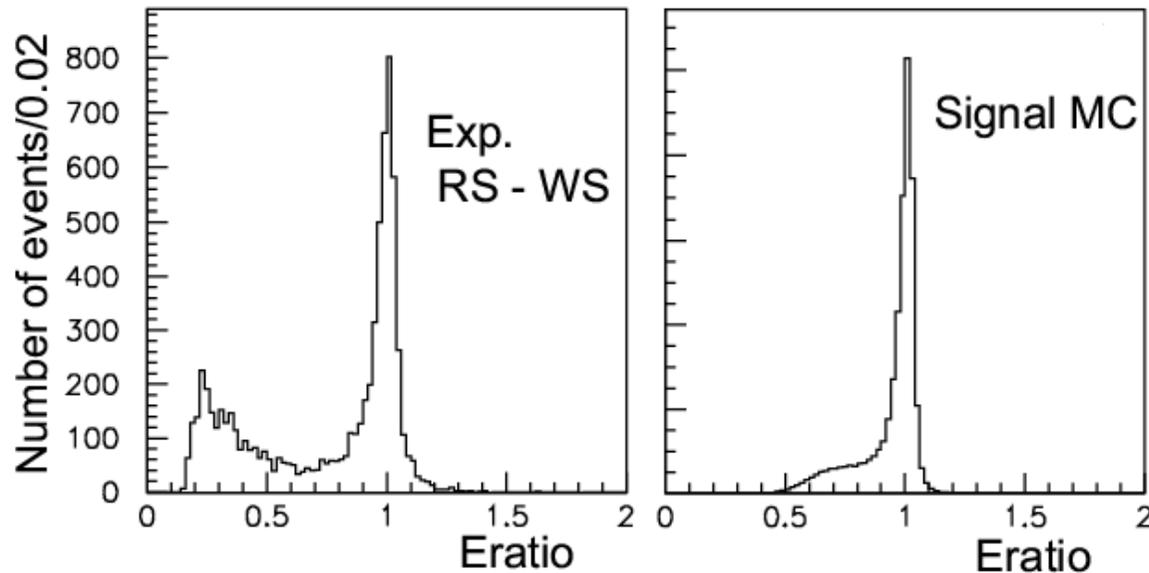


## $p_t$ -balance



# $E_{\text{ratio}}$ tail

Study of **wrong-sign events** defined by the charge vs direction relation.



The tail around  $E_{\text{ratio}} \sim 0.75$  is consistent with the expected radiative tail of the signal process.



# $M_{\gamma\gamma}$ Fit

---

Double Gaussian(for signal)+ 2<sup>nd</sup>-O<sup>rd</sup>er Polynomial (background)

$$f(x) \sim a + bx + cx^2 + \frac{A}{\sqrt{2\pi}\sigma} \left\{ r e^{-\frac{(x-m)^2}{2\sigma^2}} + \frac{1-r}{k} e^{-\frac{\{x-(m+\Delta m)\}^2}{2(k\sigma)^2}} \right\}$$



# Conversion factor for $|F(Q^2)|: 2A(Q^2)$

Use the cross section formula by

“Brodsky-Kinoshita-Terazawa” (PRD 4, 1532(1971))

Not using EPA --- not trivial

CLEO, PRD57, 33(1998)

EPA – Equivalent Photon Approximation

Assume being factorized as

$$\sigma_{ee} \sim \int \sigma_{\gamma\gamma}(Q_1^2, Q_2^2) N_\gamma(Q_1^2) N_\gamma(Q_2^2) \quad (\text{we do not assume this})$$

We assume only the form factors is factorized

$$\sigma_{ee} \sim \int a(Q_1^2, Q_2^2) |F(Q_1^2, Q_2^2)|^2, \quad \text{and}$$
$$F(Q_1^2, Q_2^2) = F(0, 0) f(Q_1^2) f(Q_2^2), \quad f(0) = 1$$

Furthermore,

we assume  $f(Q^2) = 1/(1+Q^2/m_\rho^2)$  when  $Q^2 < m_\rho^2$

But,  $f(Q^2)$  is unknown for  $Q^2 > m_\rho^2$  (what we measure)

Define as  $F(Q^2) \equiv F(Q^2, 0) = F(0, Q^2) = F(0, 0) f(Q^2)$



## Conversion factor for $|F(Q^2)|$ (cont.)

---

$$c = F(0, 0) \rightarrow F(Q_1^2, Q_2^2) = c f(Q_1^2) f(Q_2^2) = c f(Q_1^2) / (1 + Q_2^2/m_\rho^2)$$

-- factorization assumption

Assume some values for  $c$  and  $f(Q_1^2)$

$$\rightarrow d\sigma/dQ_1^2 = A(Q_1^2) c^2 |f(Q_1^2)|^2 \quad (\text{by BKT formula})$$

conversion factor  $A(Q^2)$  is determined by the calculation

- Single-tag measurement  $d\sigma/dQ^2$

Factor 2 : Ele-tag + Pos-tag

$$\begin{aligned} (d\sigma/dQ^2)/2A(Q^2) &= c^2 |f(Q^2)|^2 = c^2 |f(Q^2)|^2 |f(0)|^2 \\ &= |F(Q^2, 0)|^2 = |F(Q^2)|^2 \end{aligned}$$

with the same scheme for the efficiency determination

and event generation  $\rightarrow$  Signal MC

Calculation of  $A(Q^2)$  coincides BaBar's calculation with the same BKT and the same  $f(Q_2^2)$  within 0.1%.

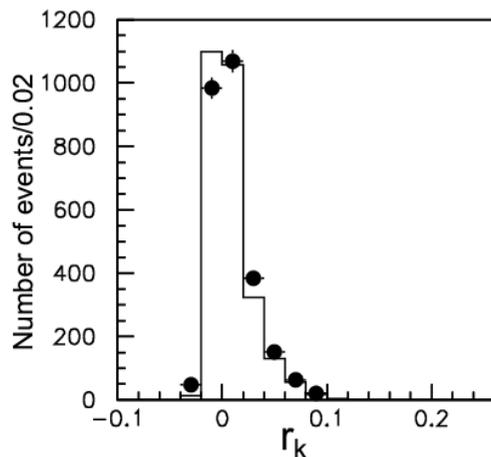
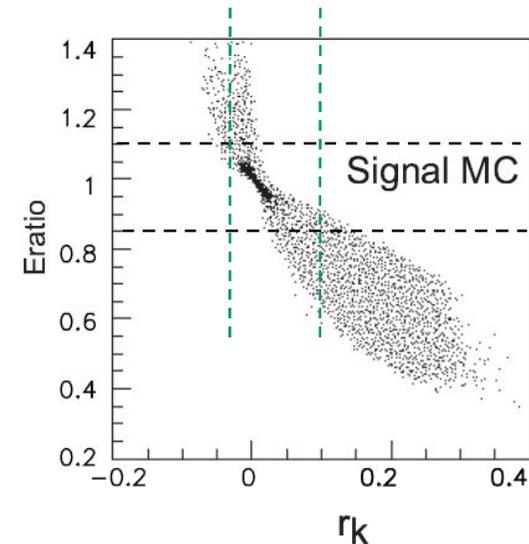


# ISR and Radiative Correction

$r_k$  --- Energy fraction of the ISR photon  
wrt. the beam energy

The  $r_k$  range for the signals is constrained by  $E_{\text{ratio}}$  cut  
which roughly corresponds to  $-0.03 < r_k < 0.10$

MC event generation includes the ISR effect  
by exponentiation technique for  $r_k < 0.25$



$r_k$  distribution is consistent  
between the data and the signal MC,  
The selected events are contained in  $r_k < 0.10$

## Radiative correction for cross section

$1 + \delta = 1.02$  (definition:  $\sigma_{\text{LO+NLO}} = \sigma_{\text{LO}}(1 + \delta)$ ,  
including +0.03 hadron-loop in vacuum polarization.  
with small  $Q^2$  dependence ( $\sim 1\%$  effect).

Our cross section and TFF are converted to those for the LO.

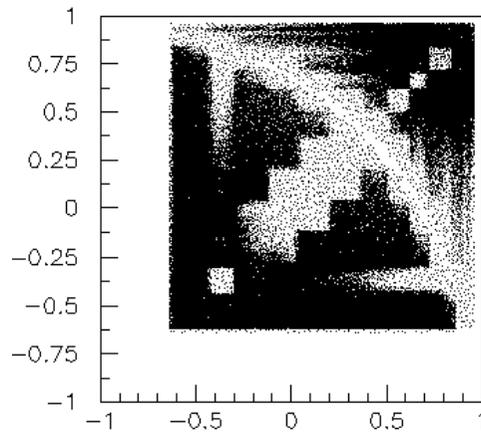


# Study of Radiative Bhabha samples

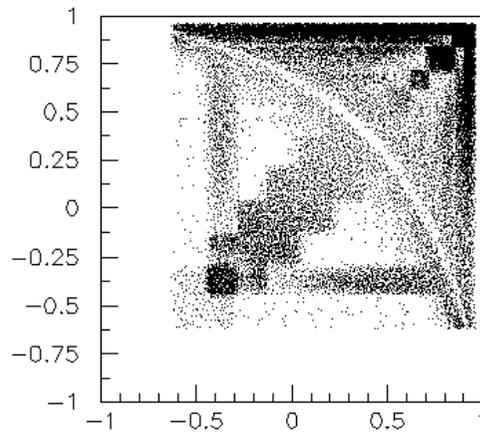
Experimental  $(e)e\gamma$  sample with the similar topology to  $(e)e\pi^0$   
**10,000 times larger statistics** (but physics is different...)

**Angle-angle ( $\cos \theta_\gamma$  vs.  $\cos \theta_e$ )** Bhabha-Veto pattern in Exp.data

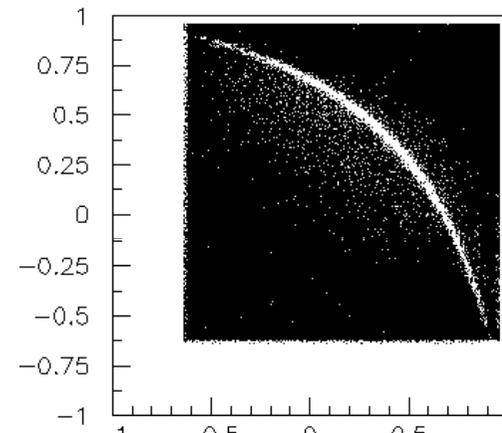
Exp.  
Data



HiE

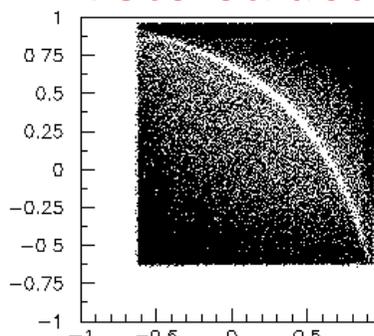
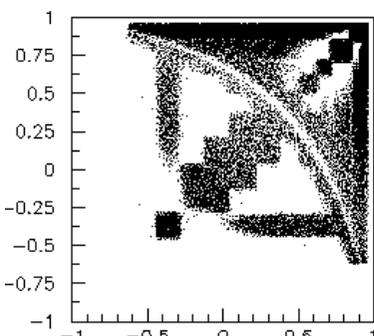
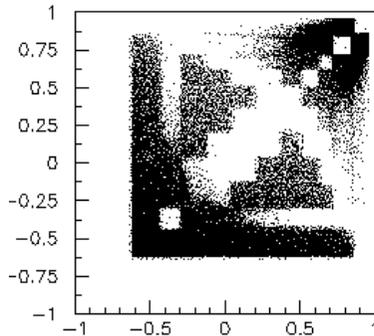


CsiBB



Unbiased: HiE + 50\*CsiBB

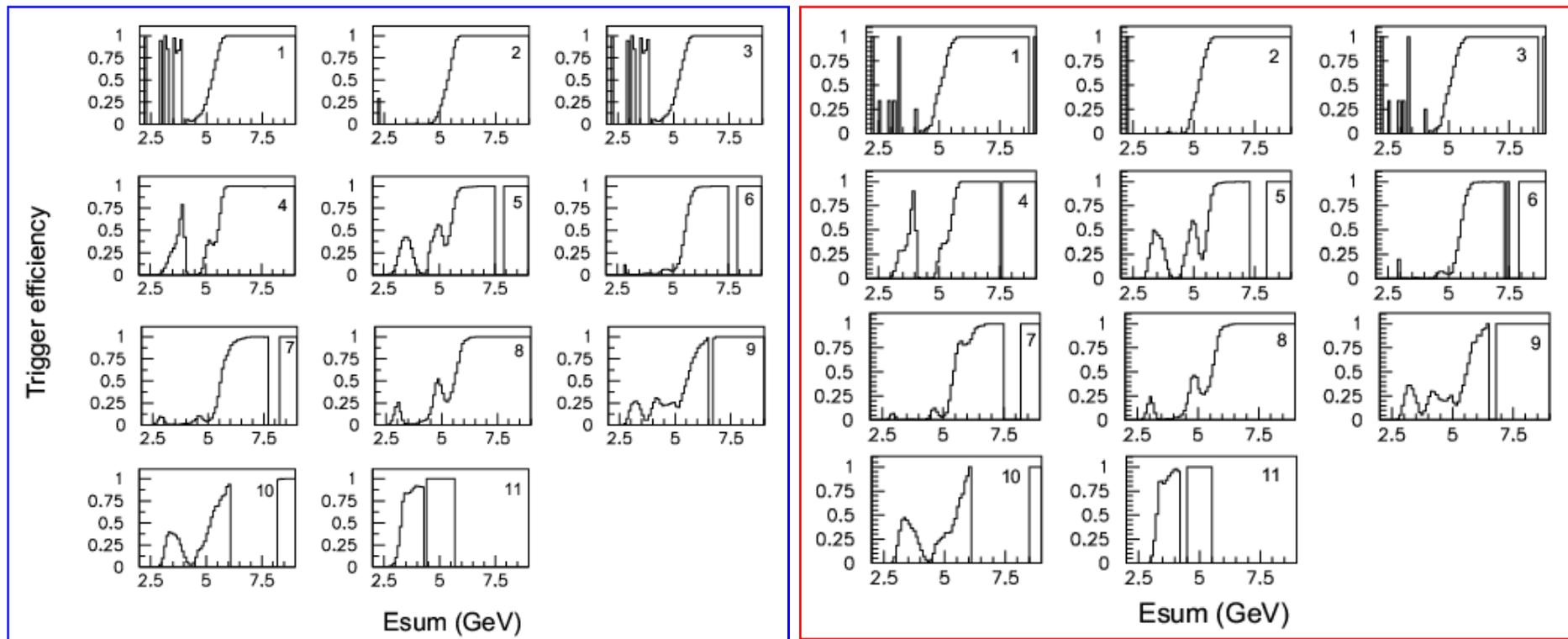
Veto-structure is compensated!



← MC(Rabhat)

# Tuning of Bhabha-veto thresholds

Looking at  $N(\text{HiE})/N(\text{Unbiased})$  as a function of E-deposit in Each ECL-Bhabha trigger segment



Experimental Rad.Bhabha sample

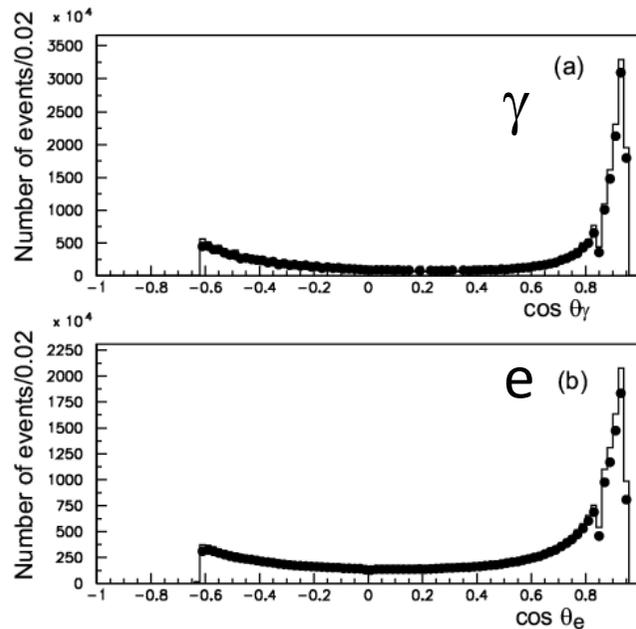
Tuned MC



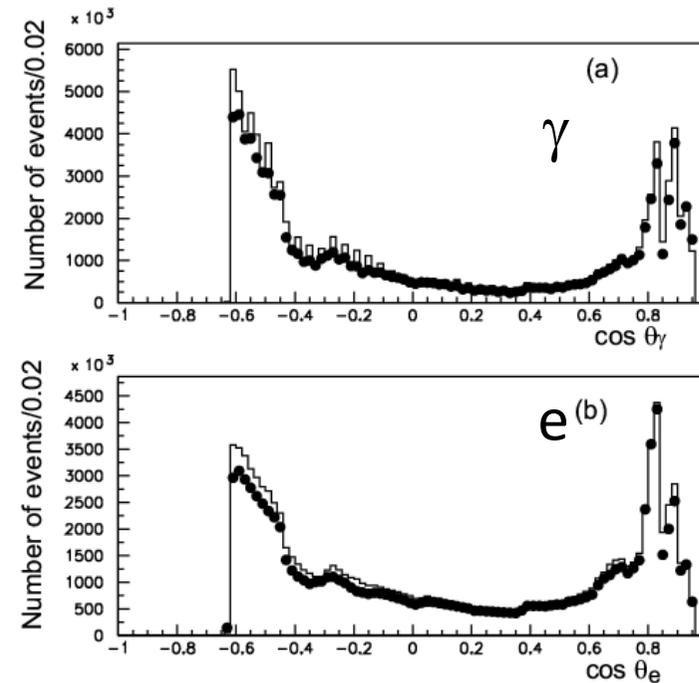
# Comparisons of Radiative Bhabha (VC) samples

Dots: Exp.  
Histograms: MC

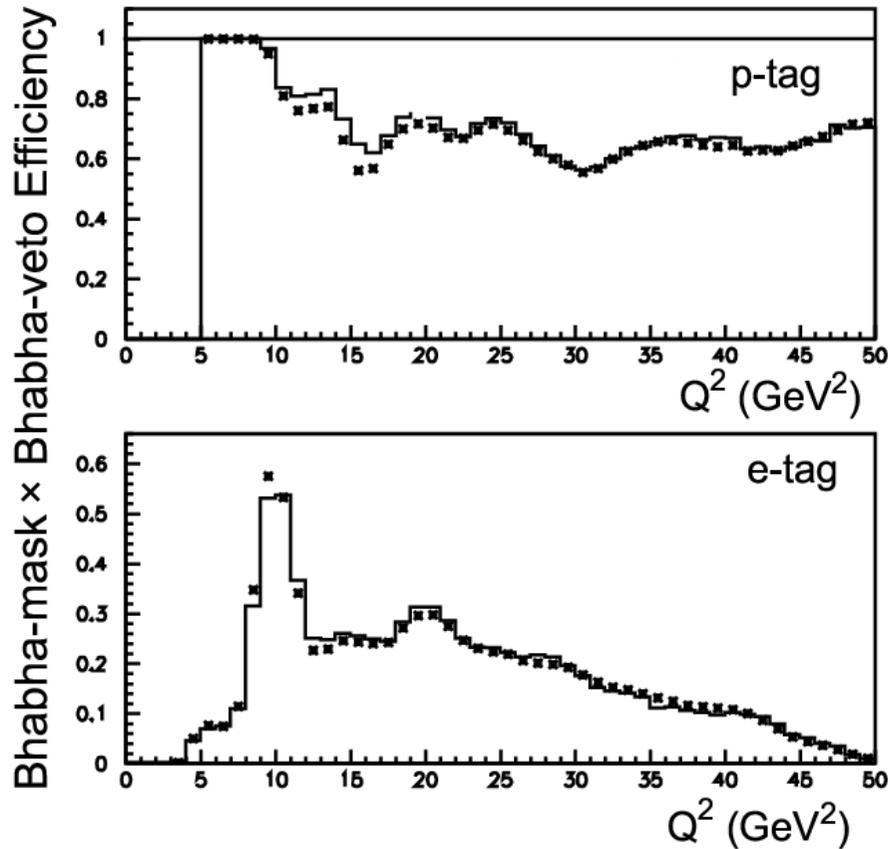
Angular  $\cos \theta \in (-1, +1)$   
distributions for  $\gamma$  and  $e$   
Unbiased



HiE (Bhabha-Masked)



# Comparison of Bhabha Mask\*Veto efficiency for Radiative Bhabha events



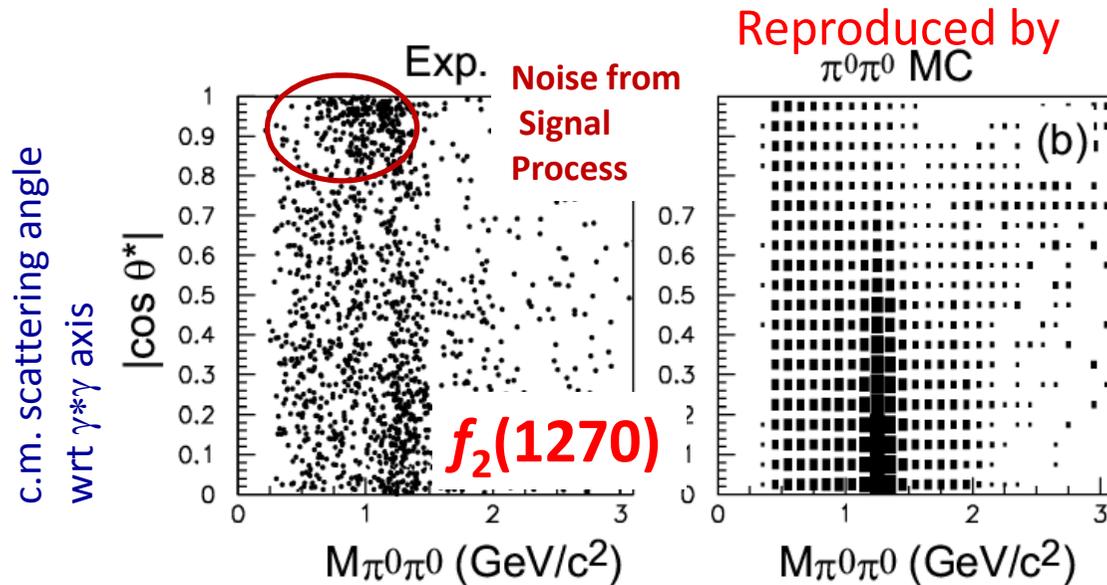
Asterisk: Exp.  
Histogram: MC

Bhabha mask\*veto efficiency from MC is confident  
Within 5 – 12% error depending on Q<sup>2</sup>



# $\pi^0\pi^0$ background MC

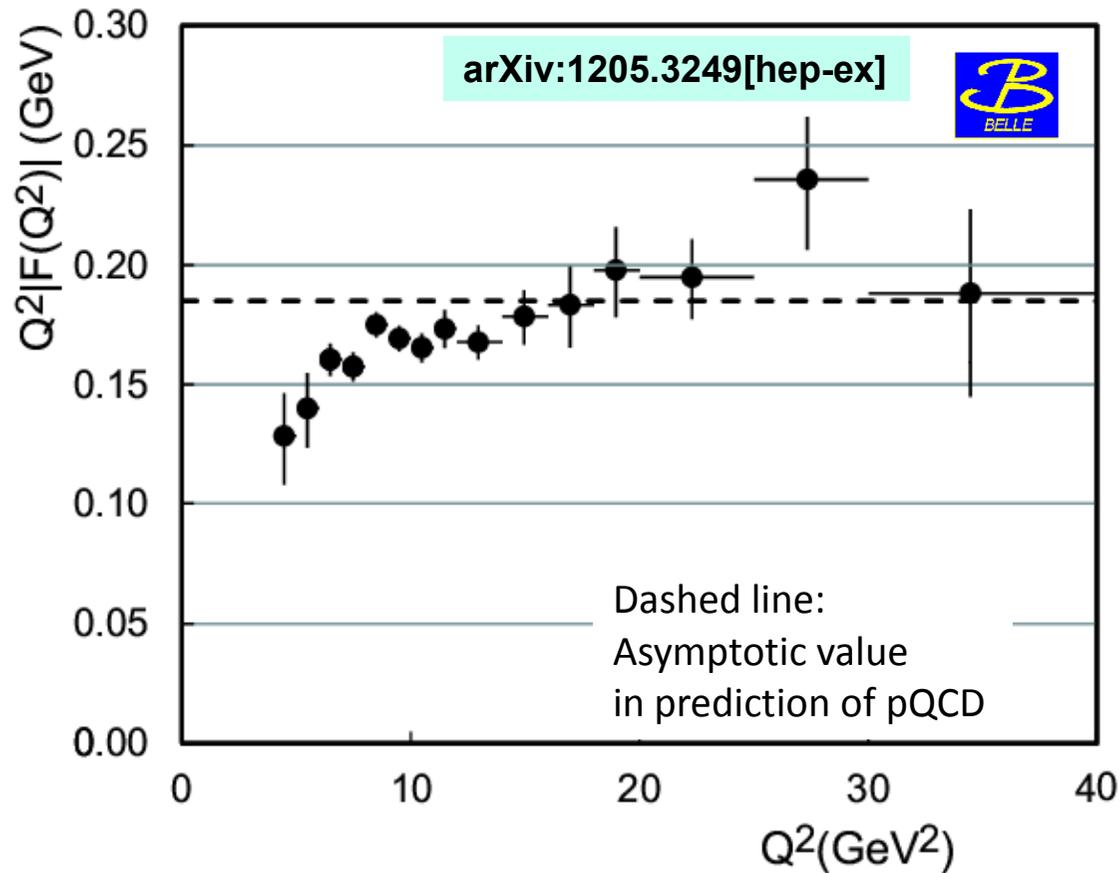
Experimentally identified  $\gamma\gamma^* \rightarrow \pi^0\pi^0$



Background contamination in signal is estimated by the  $\pi^0\pi^0$  **background MC** which is normalized to the observation, **as 2%**



# Transition Form Factor



**Representative value  $\bar{Q}^2$  is used for each  $Q^2$  bin**

$Q^2$  point that gives the cross section with the same size as the mean over the bin calculated using an approximated dependence,  $d\sigma/dQ^2 \sim Q^{-7}$



# BaBar's Efficiency and Cross section

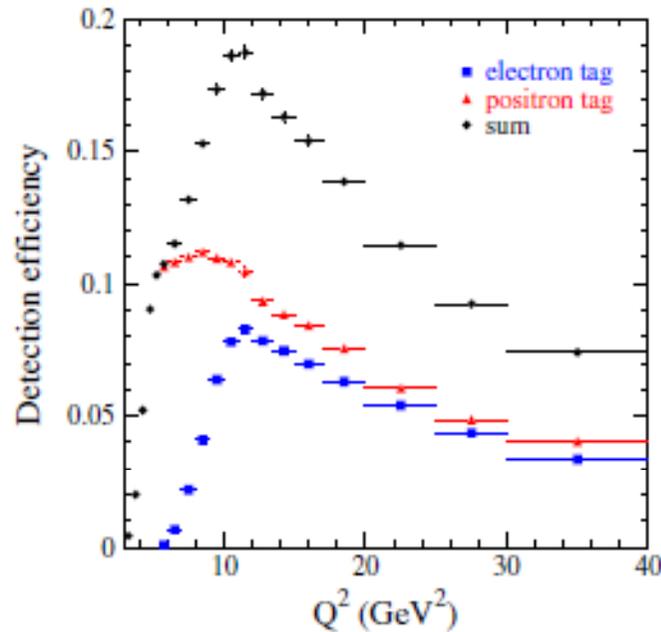


FIG. 4 (color online). The detection efficiency as a function of the momentum transfer squared for events with a tagged electron (squares), a tagged positron (triangles), and their sum (circles).

BaBar, PRD 80, 052009 (2009)

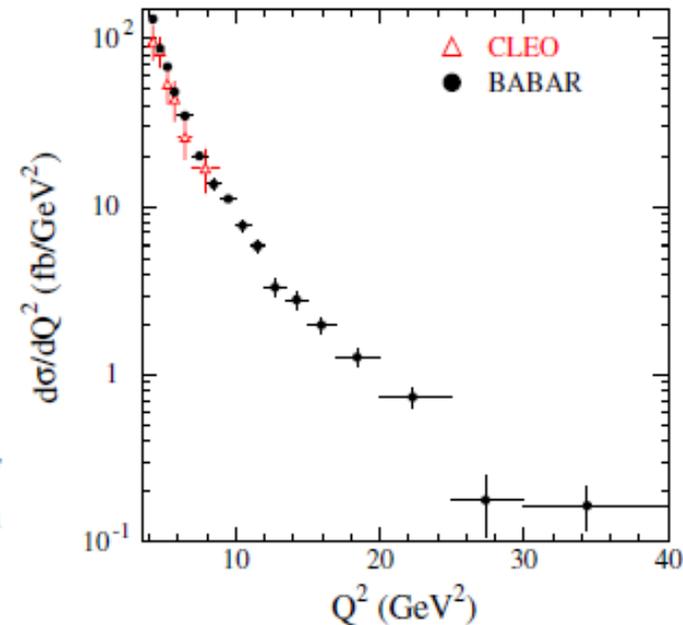


FIG. 21 (color online). The  $e^+e^- \rightarrow e^+e^-\pi^0$  differential cross section obtained in this experiment compared to that from the CLEO experiment [12].

