



Search for the $K_S \rightarrow 3\pi^0$ decay with the KLOE detection setup

Michał Silarski on behalf of the KLOE-2 collaboration
Jagiellonian University, Cracow, Poland



- ☐ Introduction
- ☐ Search for the $K_S \rightarrow \pi^0\pi^0\pi^0$ decay
- ☐ Background studies Monte Carlo calibration
- ☐ Preliminary result
- ☐ Summary & outlook



- Time evolution of the $K^0 \leftrightarrow \bar{K}^0$ system in the rest frame:

$$i \frac{\partial}{\partial t} \begin{pmatrix} |K^0\rangle \\ |\bar{K}^0\rangle \end{pmatrix} = \mathbf{H} \begin{pmatrix} |K^0\rangle \\ |\bar{K}^0\rangle \end{pmatrix} = \left[\mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right] \begin{pmatrix} |K^0\rangle \\ |\bar{K}^0\rangle \end{pmatrix}$$

$$\mathbf{M} = \begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{22} \end{pmatrix}$$

$$\mathbf{\Gamma} = \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{22} \end{pmatrix}$$

- In the basis of the CP operator:

$$|K_1\rangle = \frac{1}{\sqrt{2}} (|K^0\rangle + |\bar{K}^0\rangle) \quad (\text{CP} = 1)$$

$$|K_2\rangle = \frac{1}{\sqrt{2}} (|K^0\rangle - |\bar{K}^0\rangle) \quad (\text{CP} = -1)$$

- The eigenstates of $\mathbf{H}$:

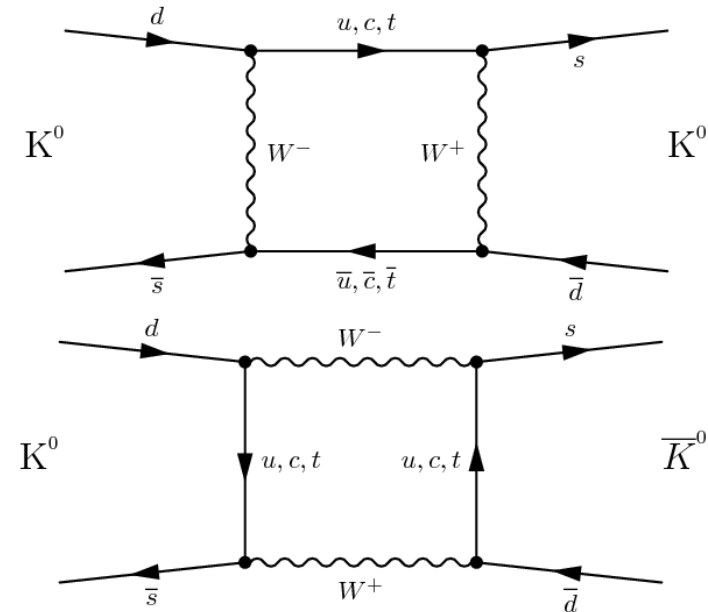
$$|K_S\rangle \quad (t = 0.9 \cdot 10^{-10} \text{ s}; ct = 2.68 \text{ cm})$$

$$|K_L\rangle \quad (t = 5.1 \cdot 10^{-8} \text{ s}; ct = 15.5 \text{ m})$$

- The main hadronic decay modes:

$$\begin{aligned} |K_S\rangle &\rightarrow \pi^+ \pi^- \\ |K_S\rangle &\rightarrow 2\pi^0 \end{aligned} \quad (\text{CP} = 1)$$

$$\begin{aligned} |K_L\rangle &\rightarrow \pi^0 \pi^+ \pi^- \\ |K_L\rangle &\rightarrow 3\pi^0 \end{aligned} \quad (\text{CP} = -1)$$





- But K_S and K_L are not CP eigenstates:

$$\text{BR}(K_L \rightarrow \pi^+ \pi^-) = 1.97 \cdot 10^{-3}$$

$$\text{BR}(K_L \rightarrow \pi^0 \pi^0) = 8.65 \cdot 10^{-4}$$

(K. Nakamura et al. (Particle Data Group), J. Phys. G 37, 075021 (2010))

- CP violation in mixing ($\Delta S=2$):

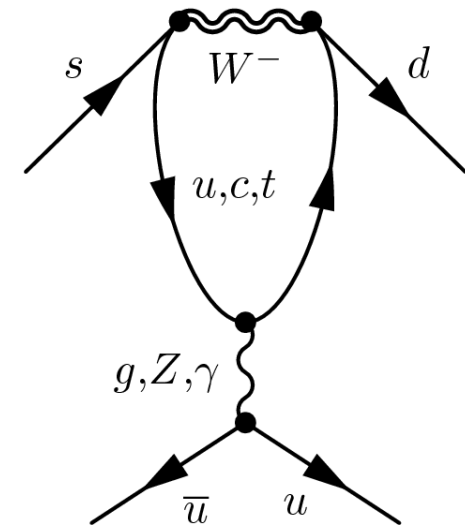
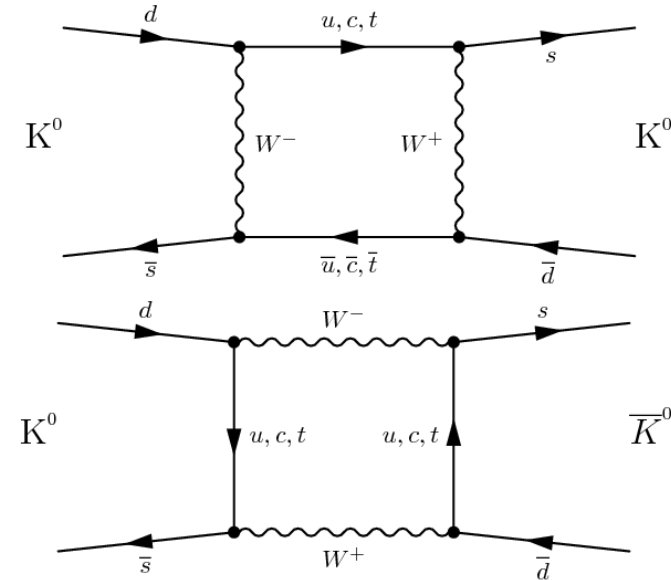
$$|K_S\rangle = \frac{1}{\sqrt{1+|\varepsilon_S|^2}} (|K_1\rangle + \varepsilon_S |K_2\rangle)$$

$$|K_L\rangle = \frac{1}{\sqrt{1+|\varepsilon_L|^2}} (|K_2\rangle + \varepsilon_L |K_1\rangle)$$

$\varepsilon_S \neq \varepsilon_L \Rightarrow \text{CPTV}$

- CP violation directly in the decay ($\Delta S=1$):

$$|K_1\rangle \rightarrow 2\pi, \quad |K_2\rangle \rightarrow 3\pi$$





- We can define the following amplitude ratios (assuming the CPT invariance):

$$\eta_{+-} = \frac{\langle \pi^+ \pi^- | H | K_L \rangle}{\langle \pi^+ \pi^- | H | K_S \rangle} = \varepsilon + \varepsilon' \qquad \eta_{00} = \frac{\langle \pi^0 \pi^0 | H | K_L \rangle}{\langle \pi^0 \pi^0 | H | K_S \rangle} = \varepsilon - 2\varepsilon'$$

- These parameters can be measured using the interference between $K_S \rightarrow \pi^+ \pi^-$ and $K_L \rightarrow \pi^+ \pi^-$ decay:

$$N_{\pi^+ \pi^-} \sim [e^{-\Gamma_S t} + |\eta_{+-}|^2 e^{-\Gamma_L t} + 2|\eta_{+-}| \cos(\Delta m \cdot t + \varphi_{+-}) e^{-\frac{1}{2}(\Gamma_S + \Gamma_L)t}]$$

$$|\eta_{+-}| = (2.232 \pm 0.011) \cdot 10^{-3}; \qquad \varphi_{+-} = (43.51 \pm 0.05)^\circ$$

$$|\eta_{00}| = (2.221 \pm 0.011) \cdot 10^{-3}; \qquad \varphi_{00} = (43.52 \pm 0.05)^\circ$$

(K. Nakamura et al. (Particle Data Group), J. Phys. G 37, 075021 (2010))



- For the $|K_S \rangle \rightarrow 3\pi$ decay modes:

$$\eta_{000} = \frac{\langle \pi^0 \pi^0 \pi^0 | H | K_S \rangle}{\langle \pi^0 \pi^0 \pi^0 | H | K_L \rangle} = \varepsilon + \varepsilon'_{000} \qquad \eta_{+-0} = \frac{\langle \pi^+ \pi^- \pi^0 | H | K_S \rangle}{\langle \pi^+ \pi^- \pi^0 | H | K_L \rangle} = \varepsilon + \varepsilon'_{+-0}$$

- In the lowest order of the χ PT: $\varepsilon'_{000} = \varepsilon'_{+-0} = -2\varepsilon'$

$$\text{Im}(\eta_{+-0}) = -0.002 \pm 0.009; \qquad \text{Im}(\eta_{000}) = (-0.1 \pm 1.6) \cdot 10^{-2}$$

$$|\eta_{000}| = \sqrt{\frac{\tau_L \text{BR}(K_S \rightarrow 3\pi^0)}{\tau_S \text{BR}(K_L \rightarrow 3\pi^0)}} < 0.018 \text{ @ } 90\% \text{ C.L.}$$

(F. Ambrosino et al., Phys. Lett. B 619, 61 (2005))

- Previous measurements of η_{000} :

SND (direct search) :

$$\text{BR}(K_S \rightarrow 3\pi^0) < 1.4 \cdot 10^{-5}$$

NA48 (interference measurement):

$$\text{BR}(K_S \rightarrow 3\pi^0) < 7.4 \cdot 10^{-7}$$

KLOE

$$\text{BR}(K_S \rightarrow 3\pi^0) < 1.2 \cdot 10^{-7}$$

Standard Model prediction:

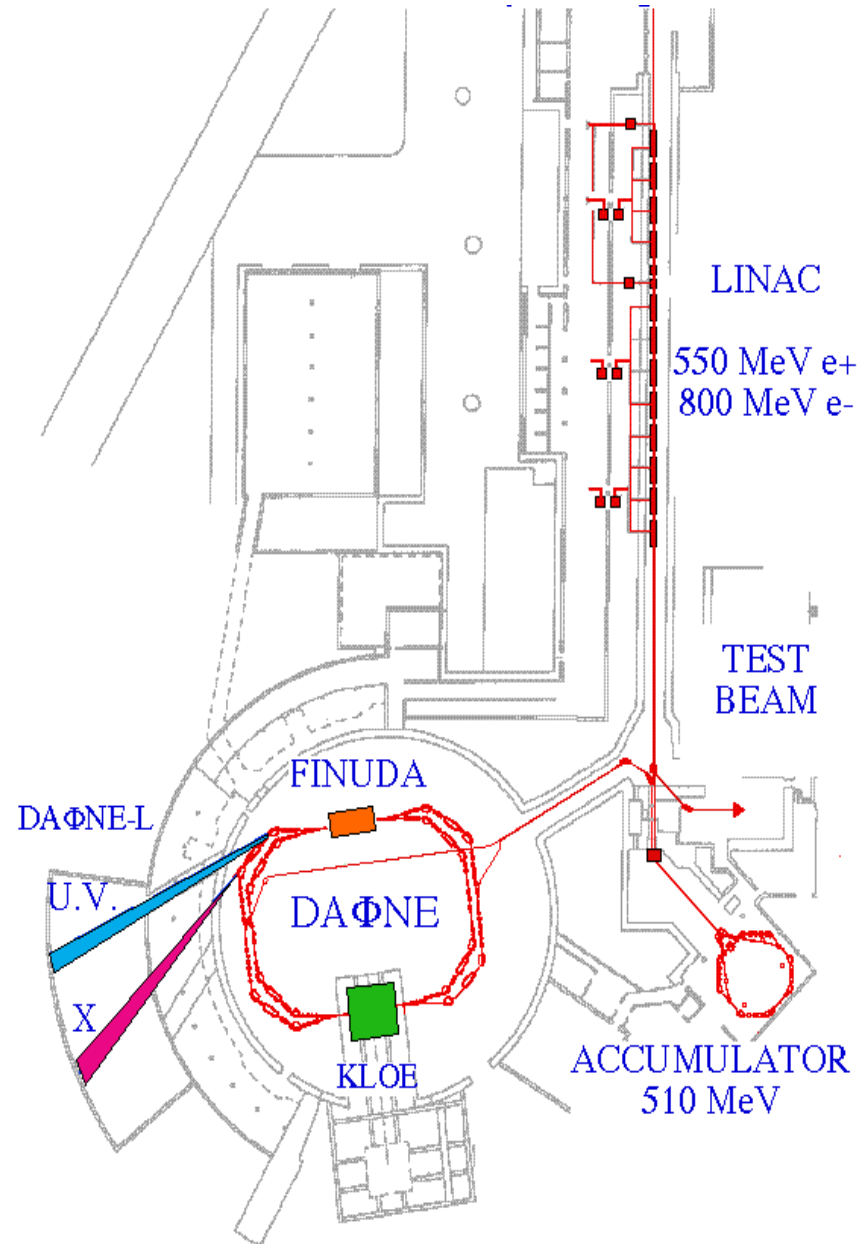
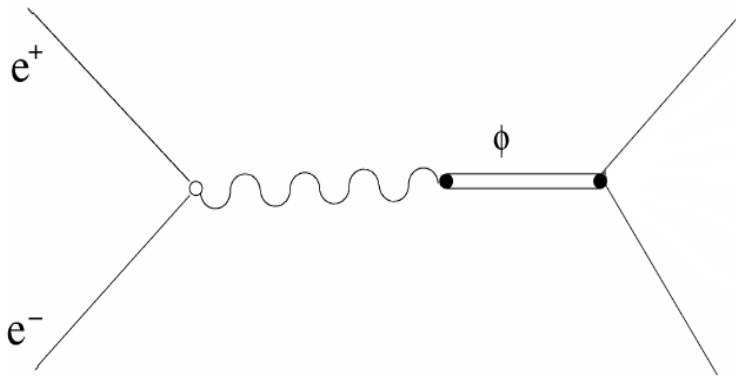
$$\text{BR}(K_S \rightarrow 3\pi^0) = 1.9 \cdot 10^{-9}$$



The DAFNE ϕ -factory

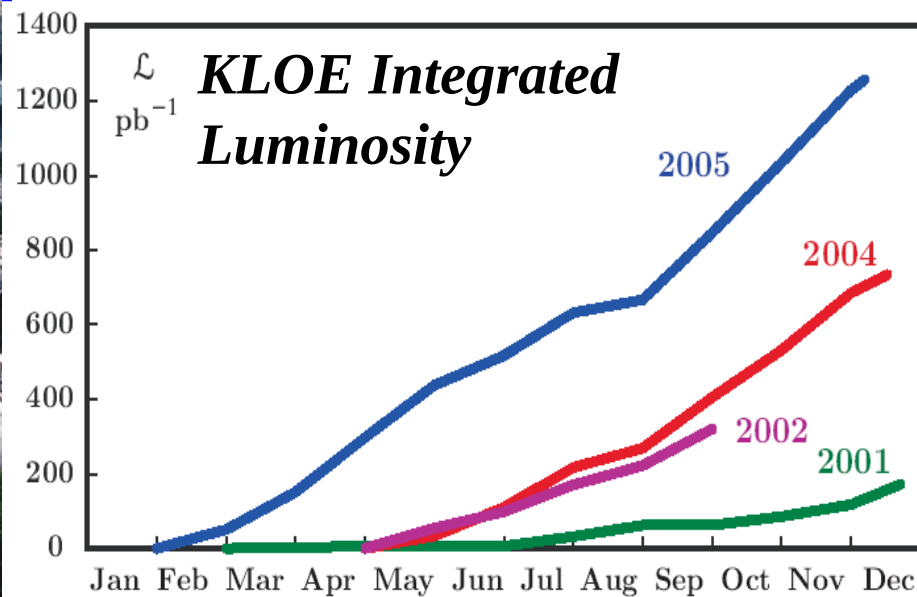


- ❑ e^+e^- collider @ $\sqrt{s} = M_\phi = 1019.4$ MeV
- ❑ LAB momentum $p_\phi \sim 13$ MeV/c
- ❑ $\sigma_{\text{peak}} \sim 3 \mu\text{b}$
- ❑ Separate e^+e^- rings to reduce beam-beam interaction
- ❑ Beams crossing angle: 12.5 mrad
- ❑ Peak luminosity $1.5 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$





DAΦNE Luminosity history



KLOE run:

- ❑ Daily performance: $7\text{--}8 \text{ pb}^{-1}$
- ❑ Best month $\int \mathcal{L} dt \sim 200 \text{ pb}^{-1}$
- ❑ Total KLOE $\int \mathcal{L} dt \sim 2400 \text{ pb}^{-1}$ at ϕ mass peak
+ 250 pb^{-1} off peak (@ 1 GeV)

BR's for selected Φ decays

K^+K^-	49.1%
$K_S K_L$	34.1%
$\rho\pi + \pi^+\pi^-\pi^0$	15.5%



Large cylindrical drift chamber

- ❑ Uniform tracking and vertexing in all volume
- ❑ Helium based gas mixture (90% He – 10% IsoC₄H₁₀)
- ❑ Stereo wire geometry

$$\sigma_p/p = 0.4 \%$$

$$\sigma_{xy} = 150 \mu\text{m}; \sigma_z = 2 \text{ mm}$$

$$\sigma_{\text{vtx}} \sim 3 \text{ mm}$$

$$\sigma(M_{\pi\pi}) \sim 1 \text{ MeV}$$

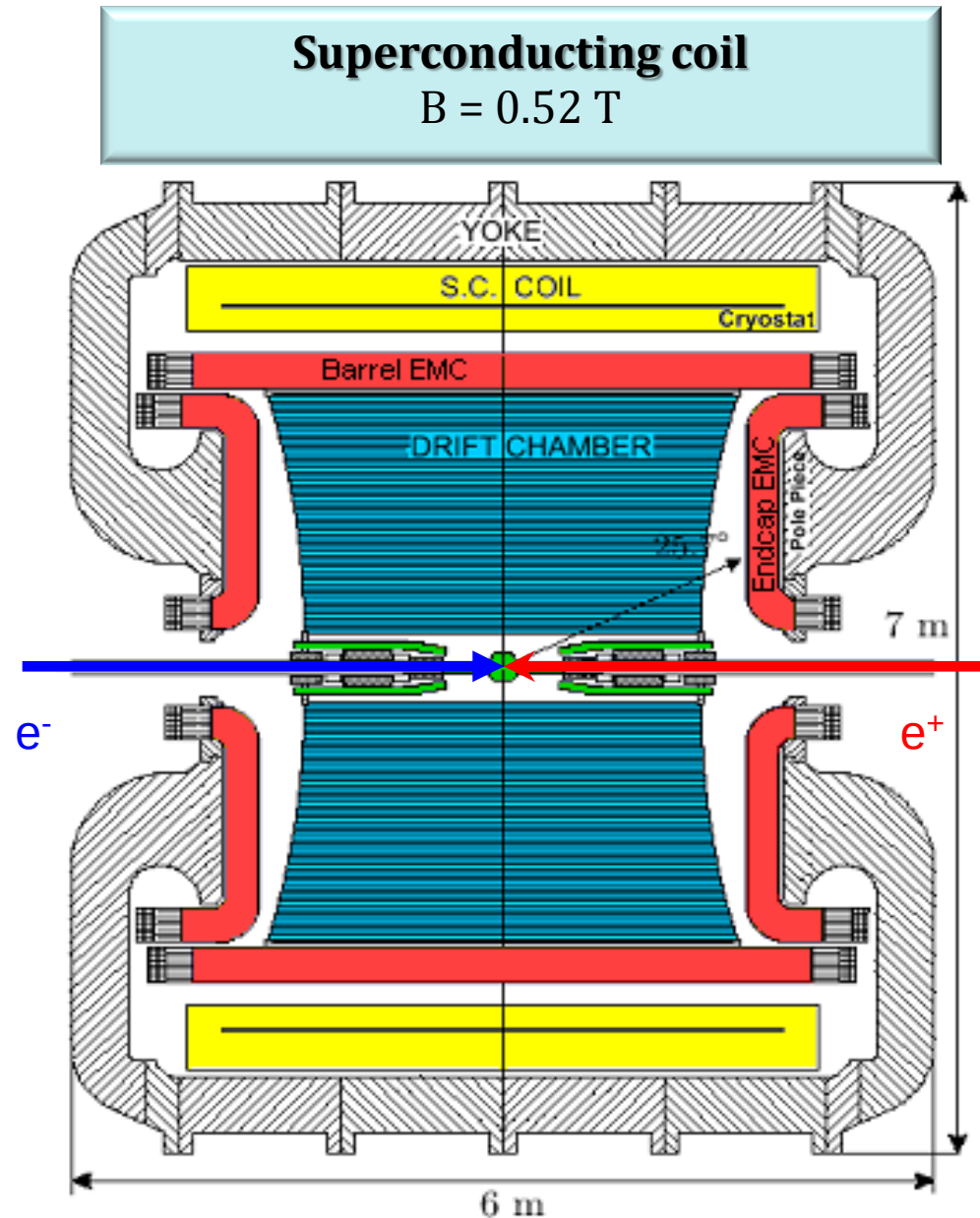
Lead/scintillating-fiber calorimeter

- ❑ Hermetical coverage
- ❑ High efficiency for low energy photons

$$\sigma_E/E = 5.7\% / \sqrt{E(\text{GeV})}$$

$$\sigma_t = 57 \text{ ps} / \sqrt{E(\text{GeV})} \oplus 140 \text{ ps}$$

$$\sigma_{\text{vtx}}(\gamma\gamma) \sim 1.5 \text{ cm}$$

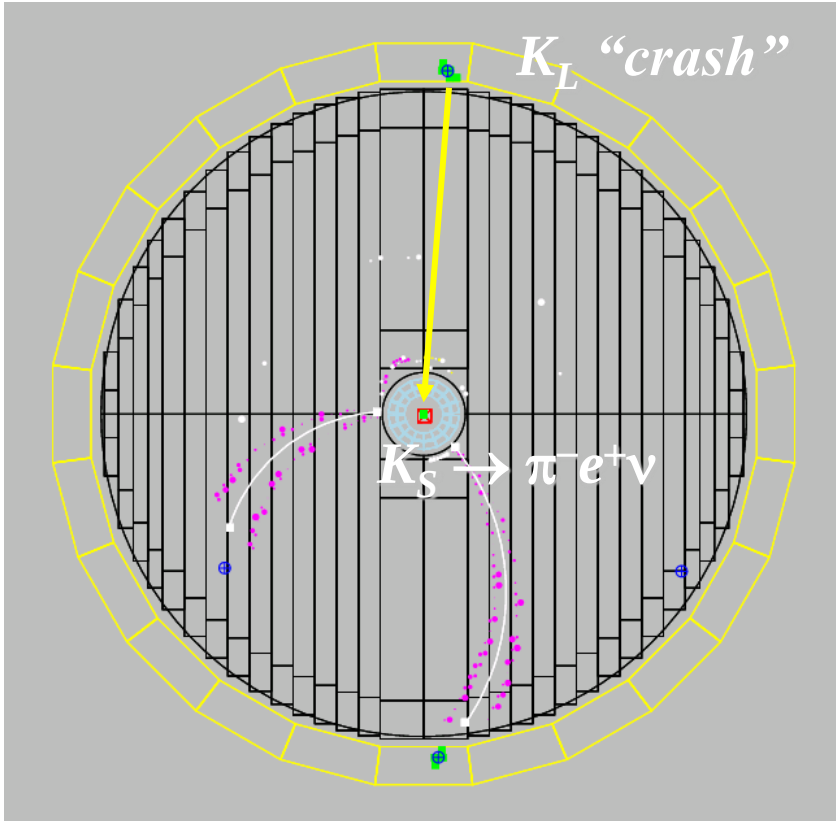




K_S and K_L tagging



A Φ -factory offers the possibility to select pure kaon beams:

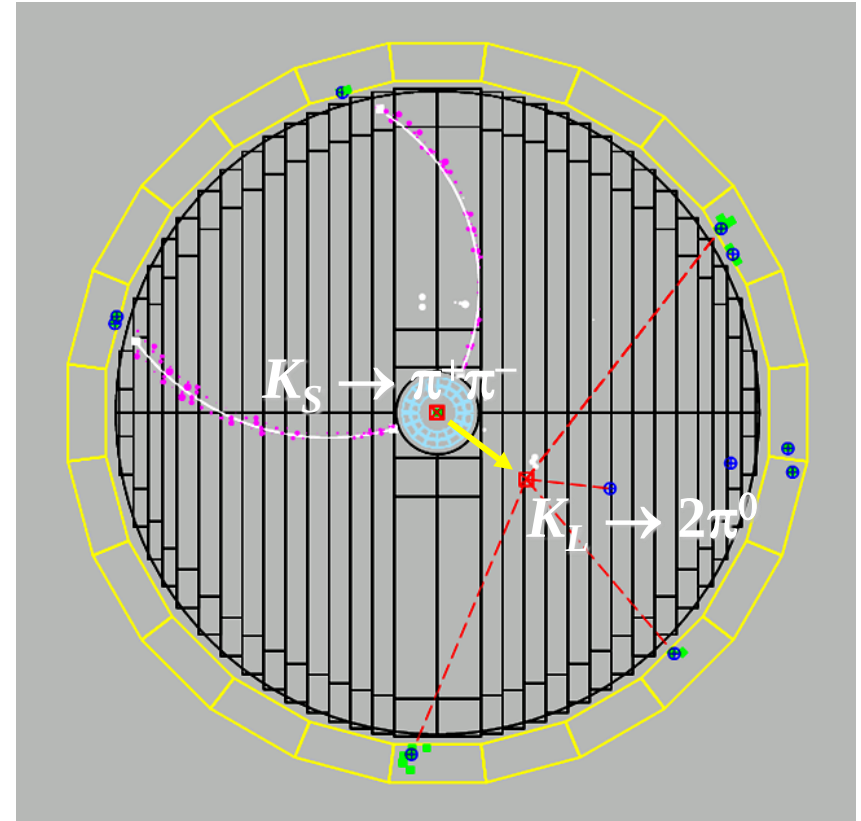


K_S tagged by K_L interaction in EmC

Efficiency $\sim 30\%$

K_S angular resolution: $\sim 1^\circ$ (0.3° in φ)

K_S momentum resolution: ~ 2 MeV



K_L tagged by $K_S \rightarrow \pi^+\pi^-$ vertex at IP

Efficiency $\sim 70\%$

K_L angular resolution: $\sim 1^\circ$

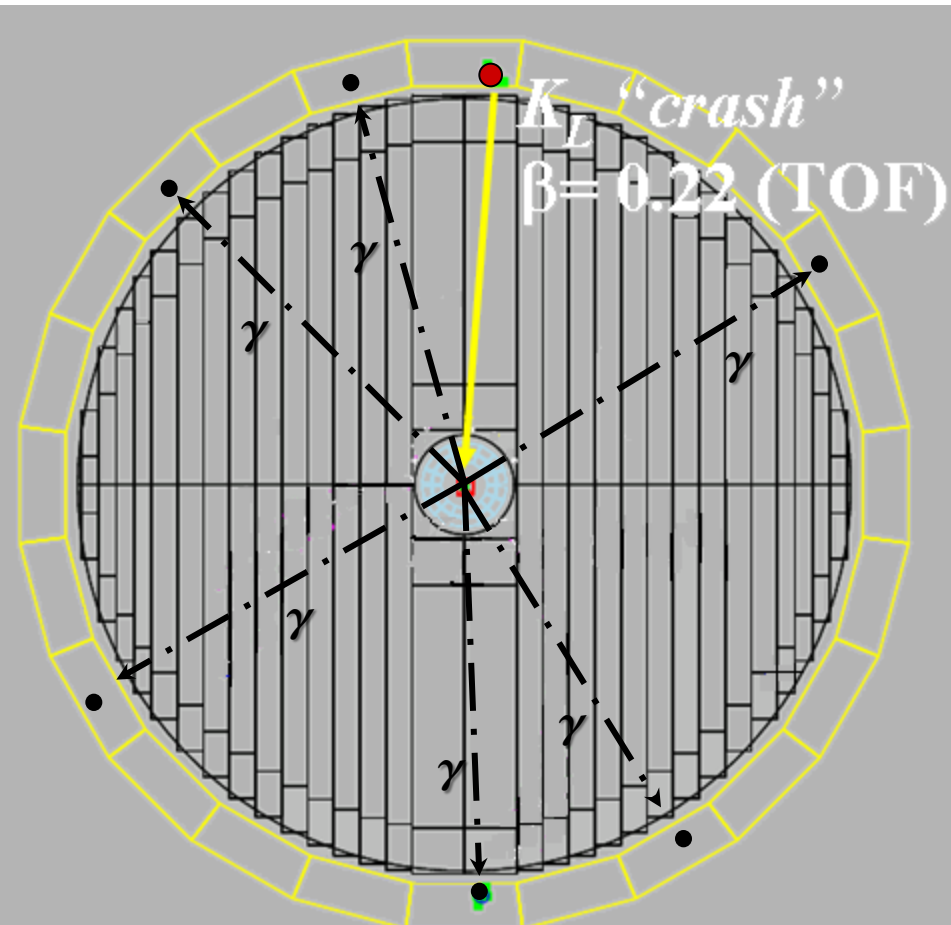
K_L momentum resolution: ~ 2 MeV



Search for the $K_S \rightarrow \pi^0 \pi^0 \pi^0$ decay

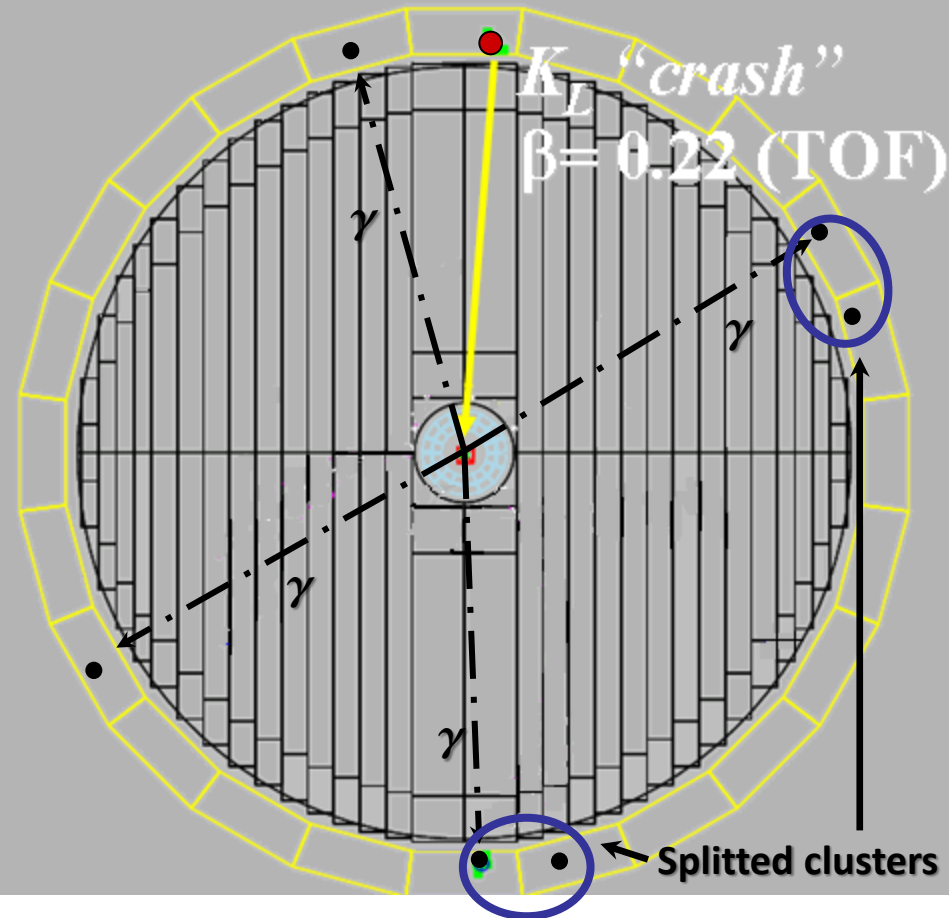


SIGNAL



$$K_S \rightarrow 3\pi^0 \rightarrow 6\gamma$$

BACKGROUND



$$K_S \rightarrow 2\pi^0 + \text{accidental/splitted clusters}$$
$$K_L \rightarrow 3\pi, K_S \rightarrow \pi^+ \pi^- \text{ („fake } K_L \text{-crash”)}$$



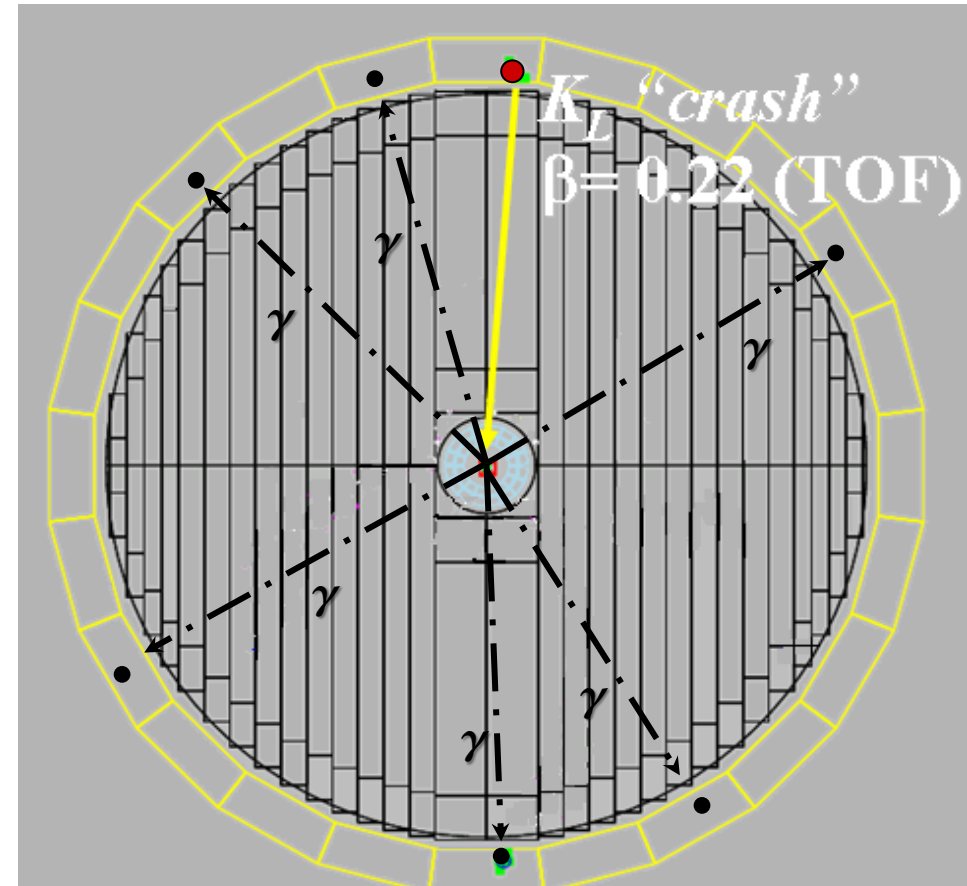
Search for the $K_S \rightarrow \pi^0 \pi^0 \pi^0$ decay



- ❑ 2004-2005 data ($\sim 7.53 \cdot 10^7$ K_L tags) & MC ($\sim 1.59 \cdot 10^8$ K_L tags)
- ❑ Expected number of the $K_S \rightarrow 3\pi^0$ decays: $N_{SM} \sim 3.8$
- ❑ Preselected signal sample (K_L -crash + 6 photons) $\sim$ **56000 events**

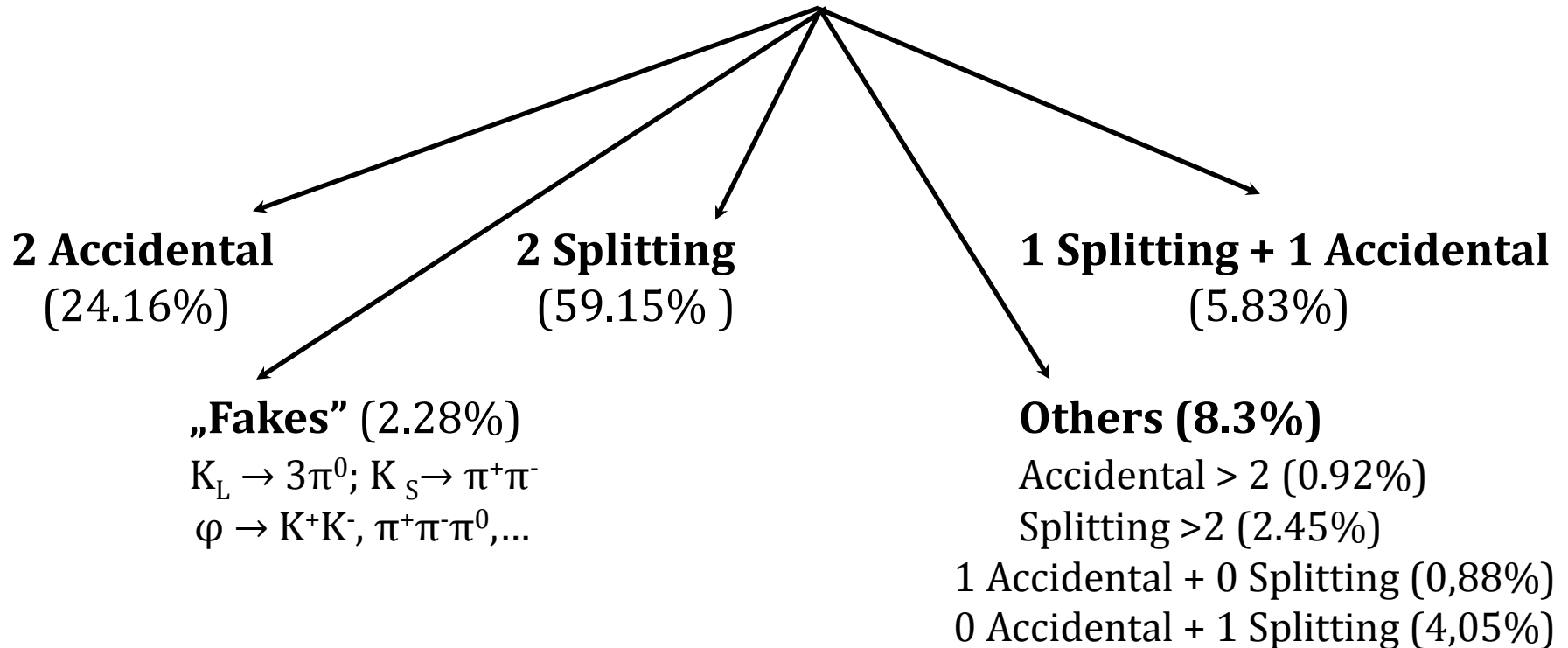
- ❑ Acceptance cuts:

- ❑ K_L -crash: $\varepsilon \approx 28\%$
- ❑ prompt photon: $\varepsilon \approx 48\%$



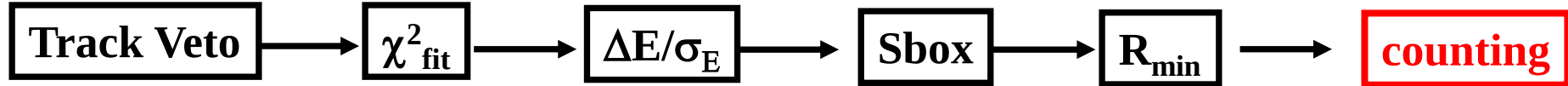


Background composition





Search for the $K_S \rightarrow \pi^0 \pi^0 \pi^0$ decay



❑ Rejection of events with charged particles

events with at least one track from the Interaction

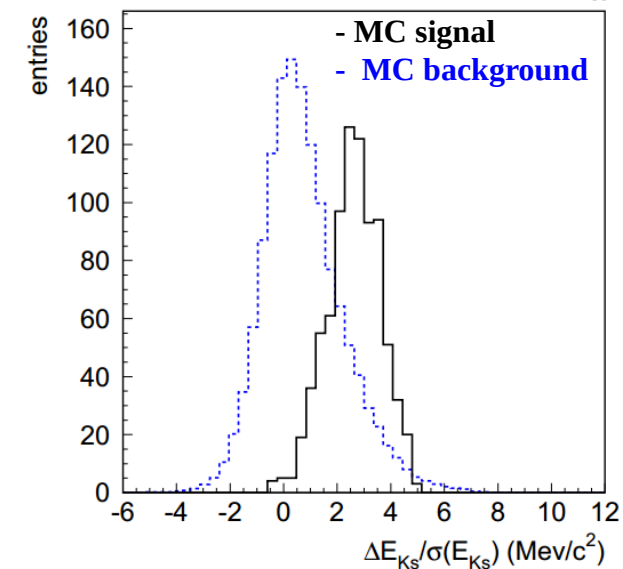
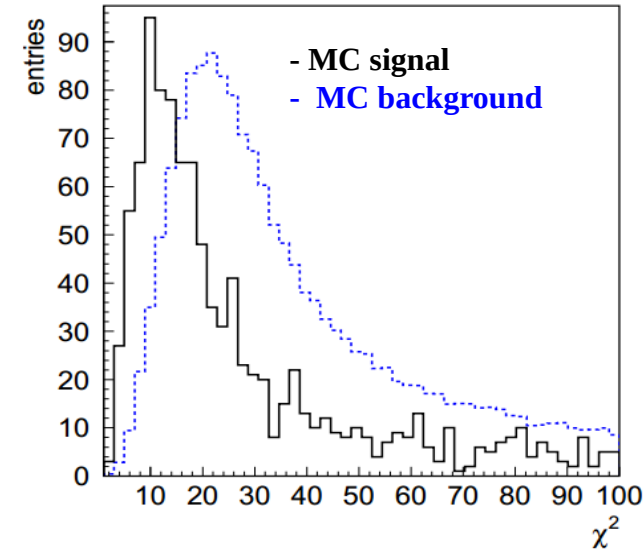
Point ($\rho_{PCA} < 4 \text{ cm}$ & $|z_{PCA}| < 10 \text{ cm}$)

❑ Kinematical fit

K_S mass, total 4-momentum conservation, consistency between the measured time and position of each cluster

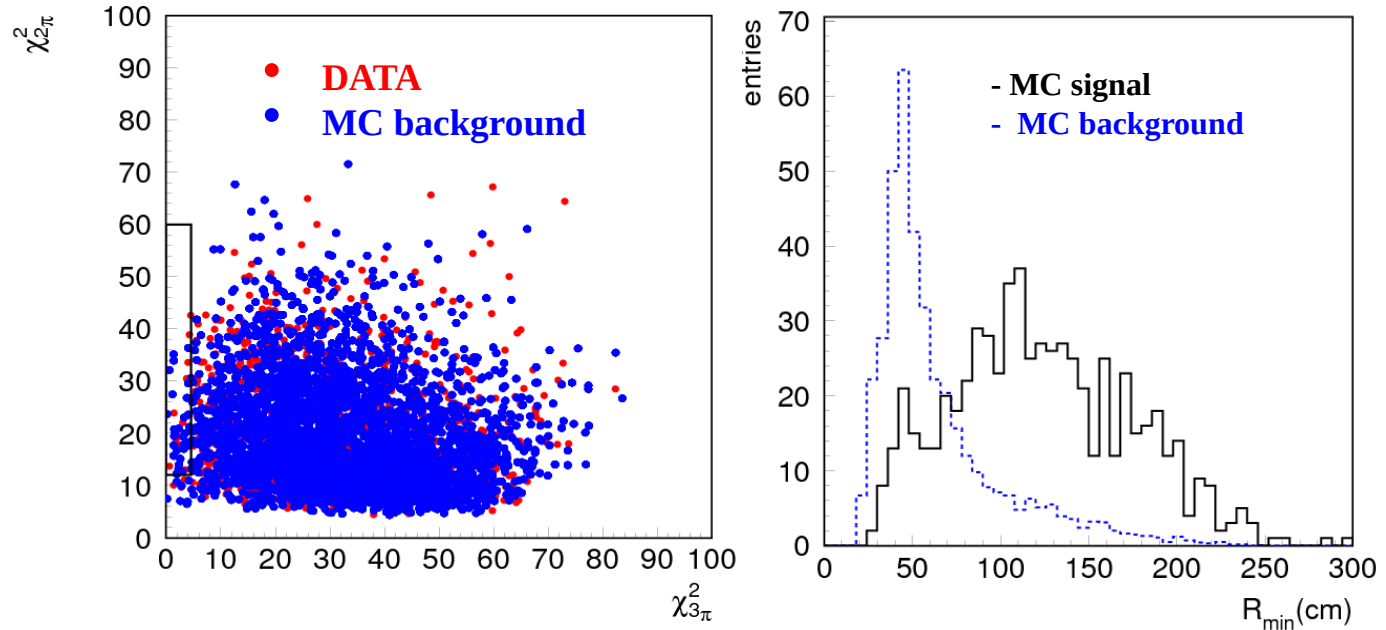
❑ $\Delta E/\sigma_E$ cut

$$\Delta E = E_{K_S} - \sum E_\gamma$$





Search for the $K_S \rightarrow \pi^0 \pi^0 \pi^0$ decay



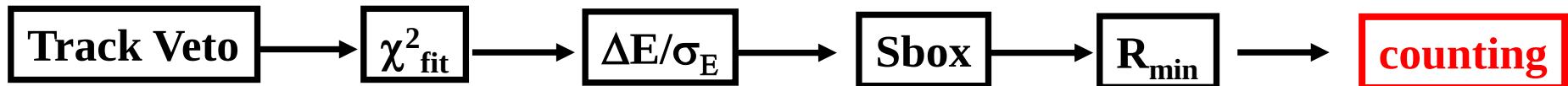
□ Signal region definition

$\chi^2_{2\pi}$: pairing of 4 out of 6 photons (π^0 masses, E_{K_S} , P_{K_S} , angle between π^0 's)

$\chi^2_{3\pi}$: pairing of 6 clusters with best π^0 mass estimates

□ $R_{\min}$

The minimum distance between clusters

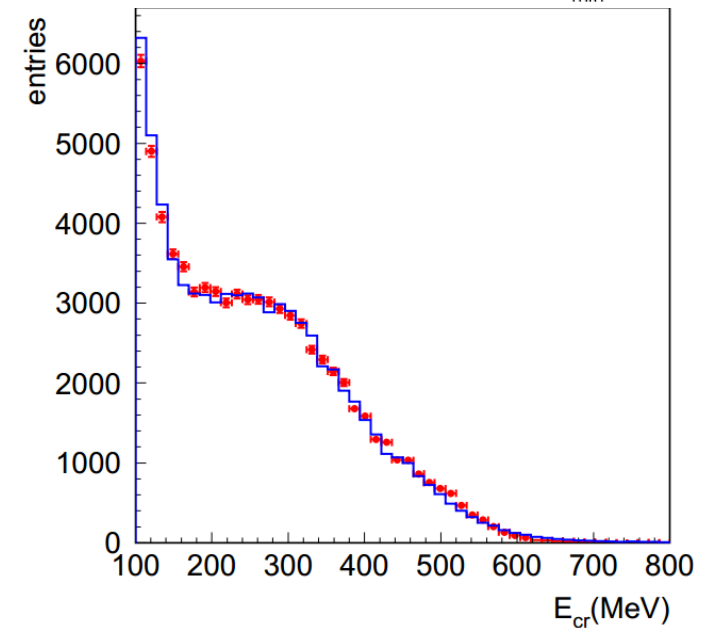
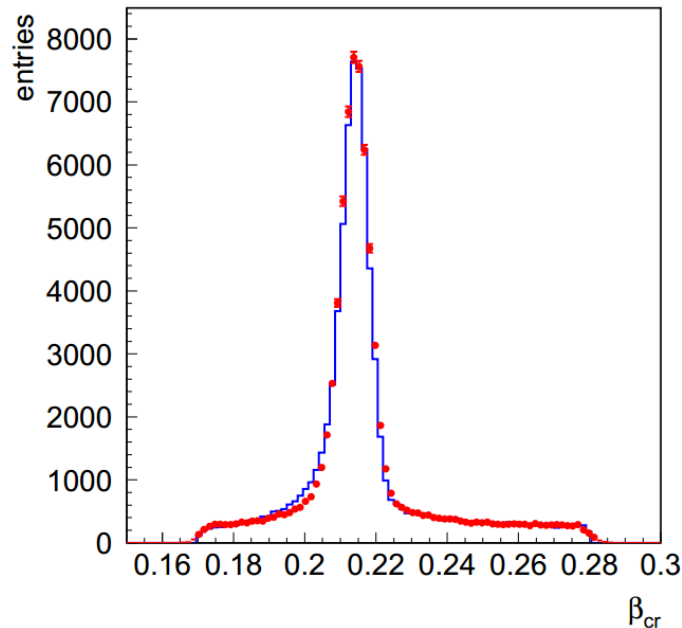
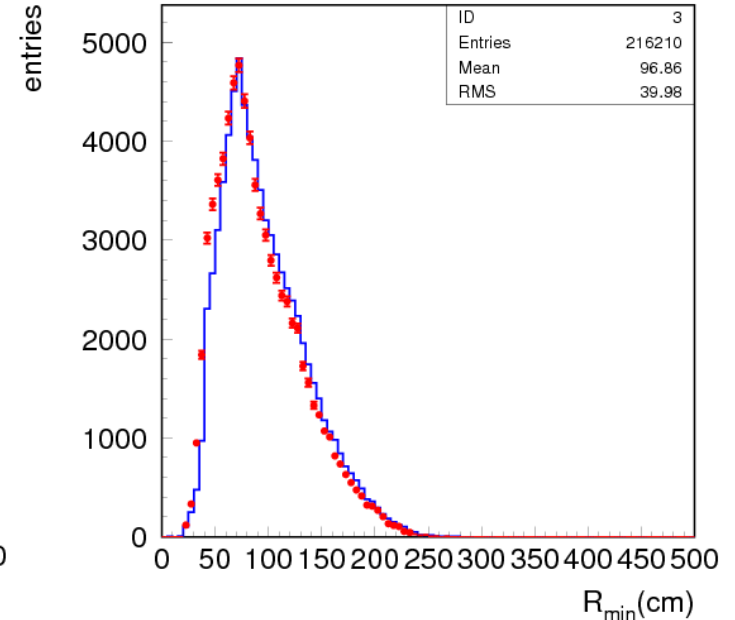
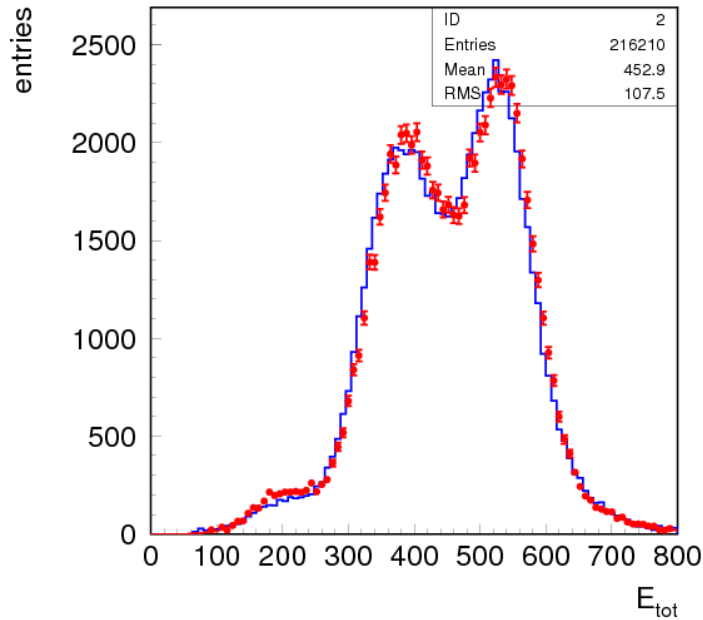




Monte Carlo calibration



● DATA
● MC

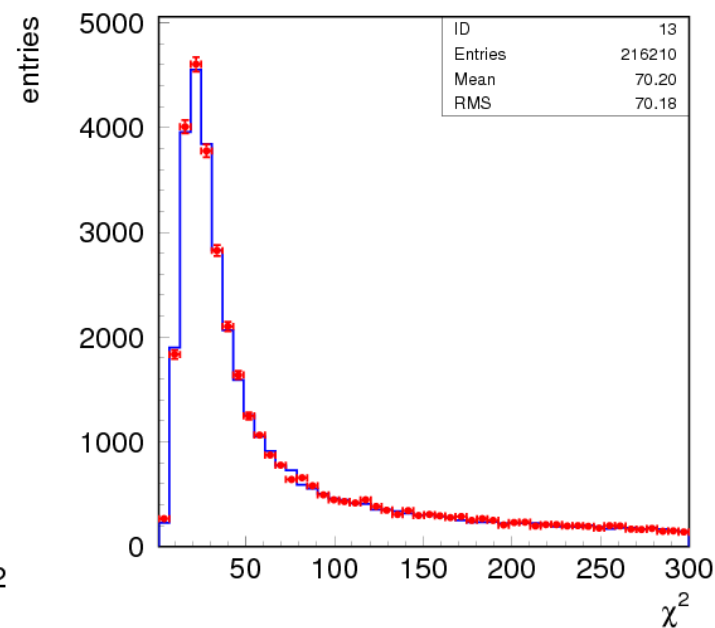
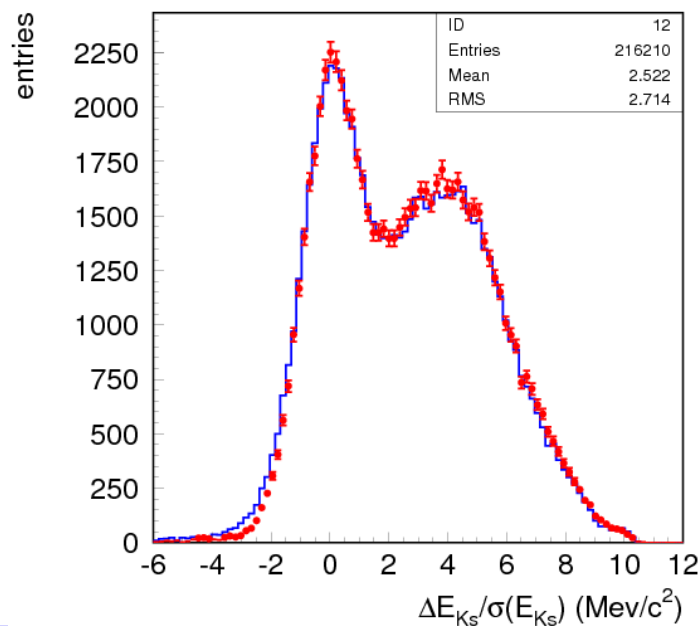
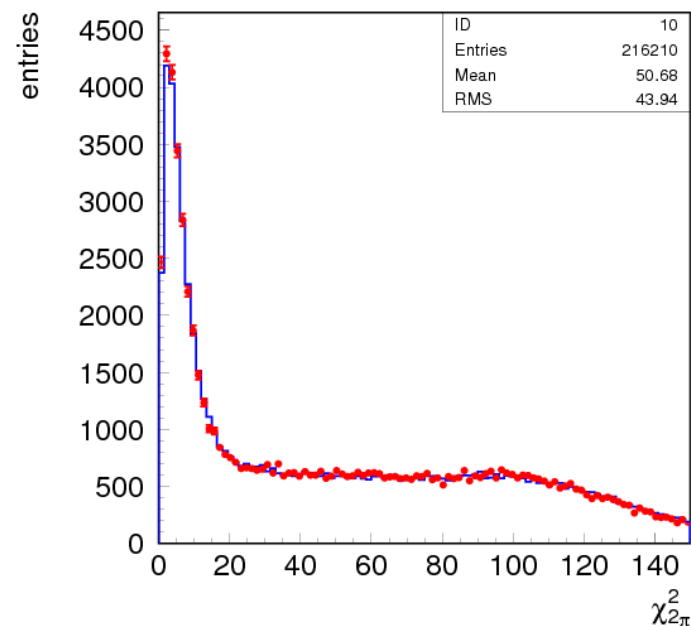
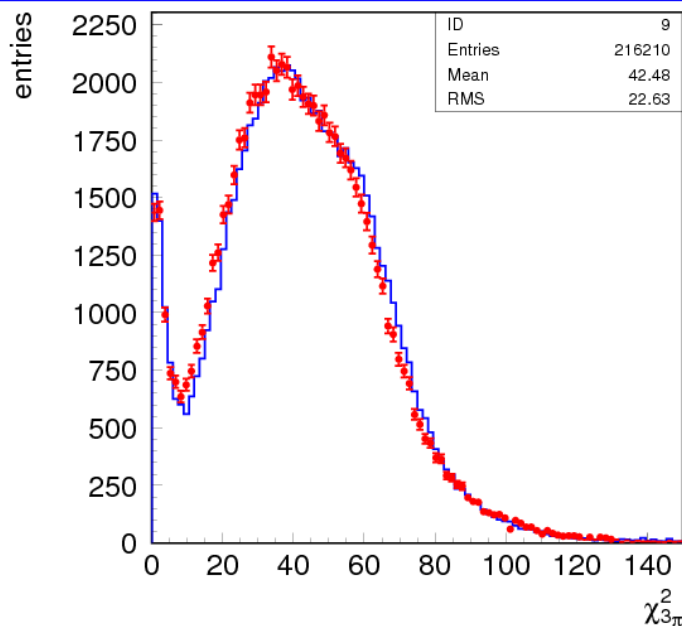




Monte Carlo calibration



● DATA
● MC





- ❖ At the end of the analysis we count $N_{\text{obs}} = 0$ event selected as a signal and $N_{\text{exp}} = 0$ events in MC
- ❖ **SM prediction:** 1 event after tagging $\Rightarrow$ 0.2 after selection
- ❖ The selection efficiency for $K_S \rightarrow 2\pi^0$ decay: $\varepsilon_{2\pi} \sim 0.66$
- ❖ Normalization sample: $N_{2\pi} = 1.36 \cdot 10^8$
- ❖ The selection efficiency for $K_S \rightarrow 3\pi^0$ signal: $\varepsilon_{3\pi} = 0.19 \pm 0.012$
- ❖ Upper limit on signal events: $N_{3\pi} < 13$ (90% C.L.)

PRELIMINARY

$$BR(K_S \rightarrow 3\pi^0) = \frac{N_{3\pi} / \varepsilon_{3\pi}}{N_{2\pi} / \varepsilon_{2\pi}} \times BR(K_S \rightarrow 2\pi^0) < 2.9 \times 10^{-8}$$

PRELIMINARY



- With the whole KLOE statistic we have obtained **the best upper limit on the $\text{BR}(K_s \rightarrow 3\pi^0) \leq 2.9 \cdot 10^{-8}$**
- **This result points to the feasibility of the first observation at KLOE-2**
- Future: KLOE-2 @ Upgraded DAφNE (talk by A. Kupść)



THANK YOU
FOR
ATTENTION



SPARES



- We can define the following amplitude ratios (assuming the CPT invariance):

$$\eta_{+-} = \frac{\langle \pi^+ \pi^- | H | K_L \rangle}{\langle \pi^+ \pi^- | H | K_S \rangle} = \varepsilon + \varepsilon' \quad \eta_{00} = \frac{\langle \pi^0 \pi^0 | H | K_L \rangle}{\langle \pi^0 \pi^0 | H | K_S \rangle} = \varepsilon - 2\varepsilon'$$

where $\varepsilon = \frac{\langle \pi\pi(I=0) | H | K_L \rangle}{\langle \pi\pi(I=0) | H | K_S \rangle}$ and $\varepsilon' = \frac{\langle \pi\pi(I=2) | H | K_L \rangle}{\langle \pi\pi(I=2) | H | K_S \rangle} = i e^{i(\delta_2 - \delta_0)} \frac{A_2}{\sqrt{2}A_0} \left(\frac{\text{Im}A_2}{A_2} - \frac{\text{Im}A_0}{A_0} \right)$

- These parameters can be measured using the interference between $K_S \rightarrow \pi^+ \pi^-$ and $K_L \rightarrow \pi^+ \pi^-$ decay:

$$N_{\pi^+ \pi^-} \sim [e^{-\Gamma_S t} + |\eta_{+-}|^2 e^{-\Gamma_L t} + 2|\eta_{+-}| \cos(\Delta m \cdot t + \varphi_{+-}) e^{-\frac{1}{2}(\Gamma_S + \Gamma_L)t}]$$

$$|\eta_{+-}| = (2.232 \pm 0.011) \cdot 10^{-3}; \quad \varphi_{+-} = (43.51 \pm 0.05)^\circ$$

$$|\eta_{00}| = (2.221 \pm 0.011) \cdot 10^{-3}; \quad \varphi_{00} = (43.52 \pm 0.05)^\circ$$

(K. Nakamura et al. (Particle Data Group), J. Phys. G 37, 075021 (2010))



- ❑ 2004-2005 data ($\sim 7.53 \cdot 10^7$ tags) & MC ($\sim 1.59 \cdot 10^8$ tags)
- ❑ Expected number of the $K_S \rightarrow 3\pi^0$ decays: $N_{SM} \sim 3.8$
- ❑ Acceptance cuts:

- K_L -crash:

$$\left. \begin{array}{l} E_{cr} > 129 \text{ MeV} \\ 0.196 \leq \beta_{cr} \leq 0.25 \\ 40^\circ \leq \theta_{cr} \leq 140^\circ \end{array} \right\} \varepsilon \approx 28\%$$

- prompt photon:

$$\left. \begin{array}{l} E_{cl} > 7 \text{ MeV} \\ |\cos \theta_{cl}| \leq 0.915 \\ |\Delta T_{cl}| \leq \text{Min}(3.5 \cdot \sigma_T(E_{cl}), 2 \text{ ns}) \end{array} \right\} \varepsilon \approx 48\%$$

- ❑ Preselected signal sample (K_L -crash + 6 photons) $\sim$ **56000 events**



Search for the $K_S \rightarrow \pi^0 \pi^0 \pi^0$ decay



□ Signal region definition

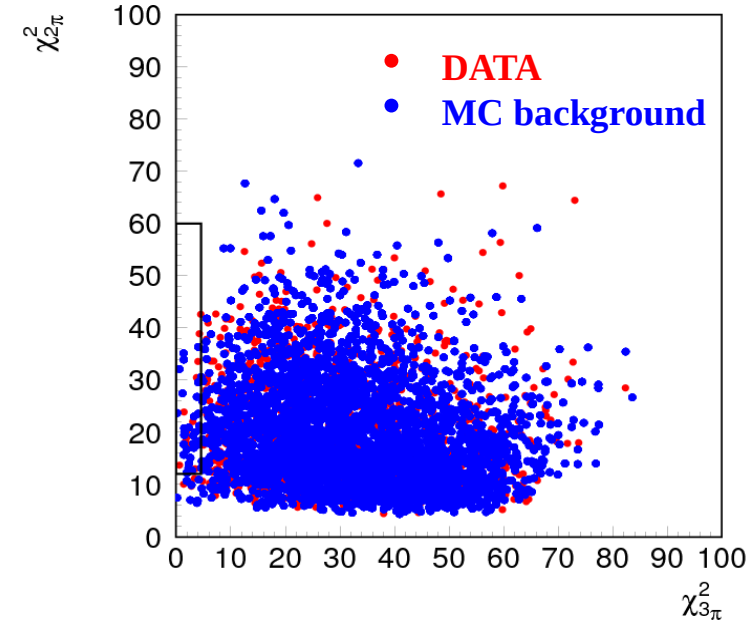
$\chi^2_{2\pi}$: pairing of 4 out of 6 photons

(π^0 masses, E_{K_S} , P_{K_S} , angle between π^0 's)

$\chi^2_{3\pi}$: pairing of 6 clusters with best π^0 mass estimates

$$\chi^2_{2\pi} = \frac{(M_{\pi_1} - M_{pdg})^2}{\sigma_{\pi_1}^2} + \frac{(M_{\pi_2} - M_{pdg})^2}{\sigma_{\pi_2}^2} + \frac{(E_{K_S} - \sum E_{\gamma_i})^2}{\sigma_E^2} + \frac{(P_{K_S}^x - \sum P_{\gamma_i}^x)^2}{\sigma_{P^x}^2} + \frac{(P_{K_S}^y - \sum P_{\gamma_i}^y)^2}{\sigma_{P^y}^2} + \frac{(P_{K_S}^z - \sum P_{\gamma_i}^z)^2}{\sigma_{P^z}^2} + \frac{(\pi - \vartheta_{\pi\pi})^2}{\sigma_{\vartheta_{\pi\pi}}^2}$$

$$\chi^2_{3\pi} = \sum_{i=1}^3 \frac{(M_{\pi_i} - M_{pdg})^2}{\sigma_{\pi_i}^2}$$



- MC signal
- MC background

□ $R_{\min}$

The minimum distance between clusters

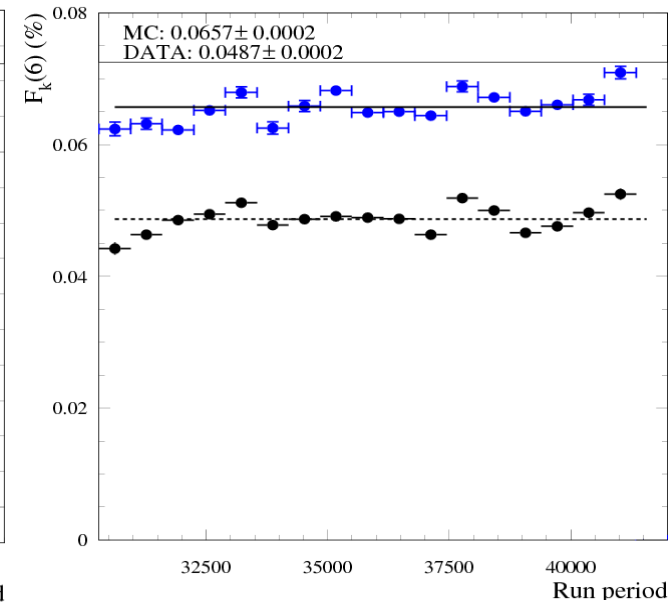
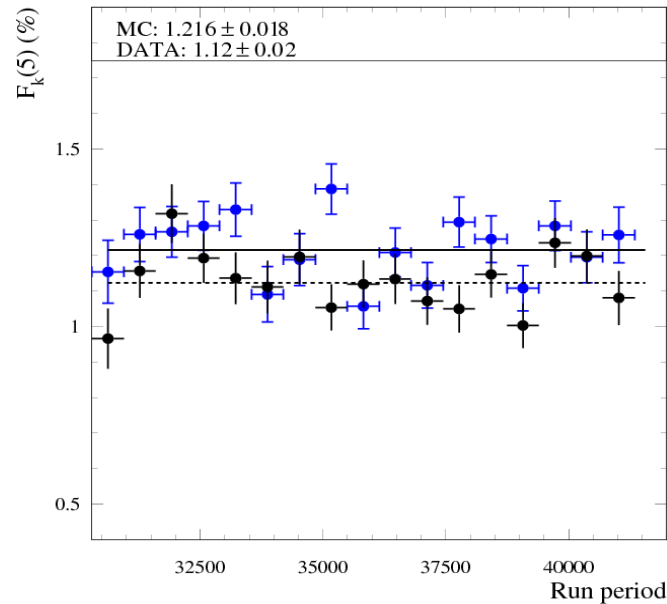
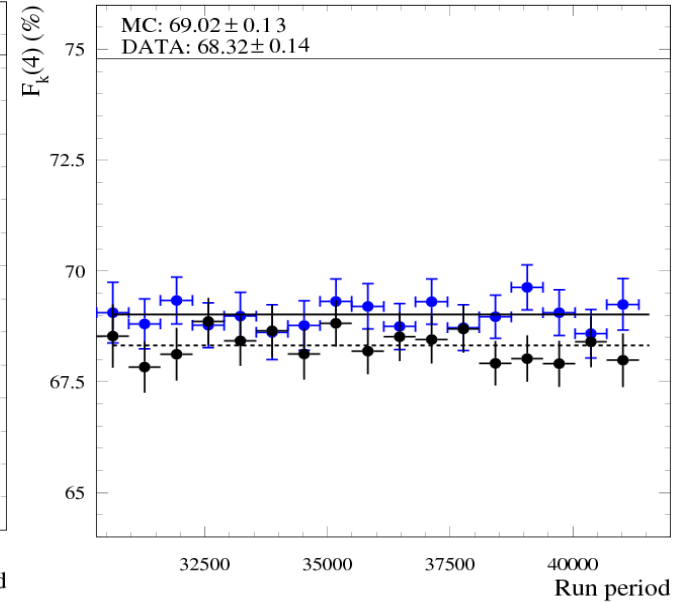
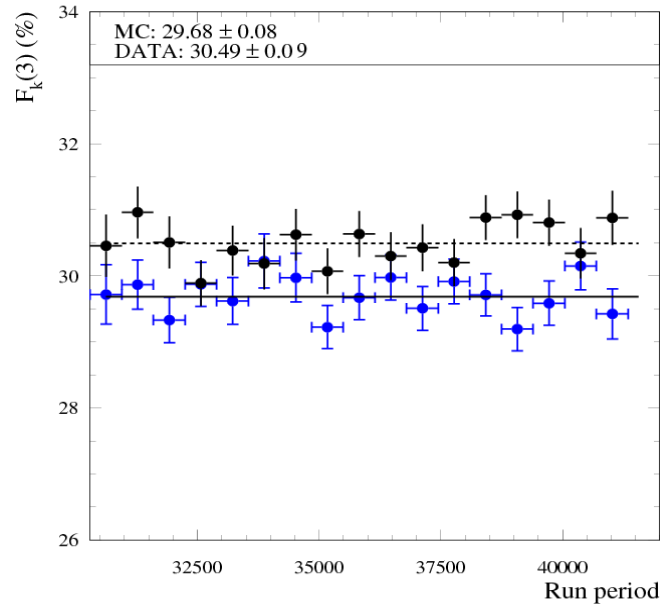


Background studies



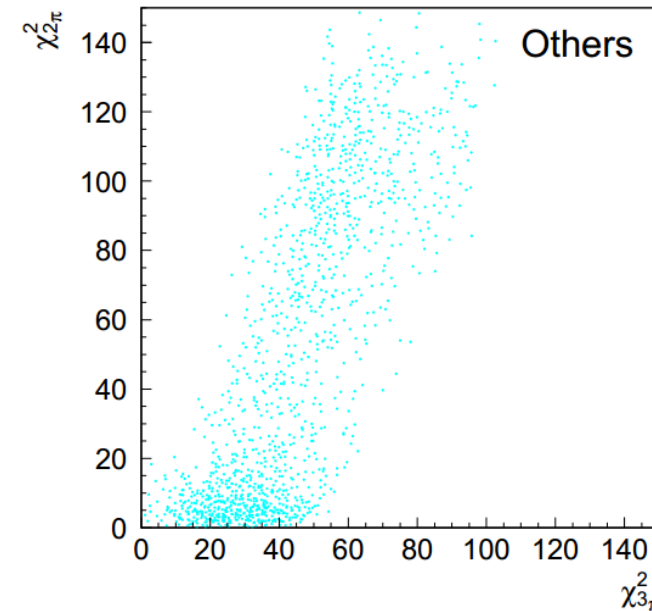
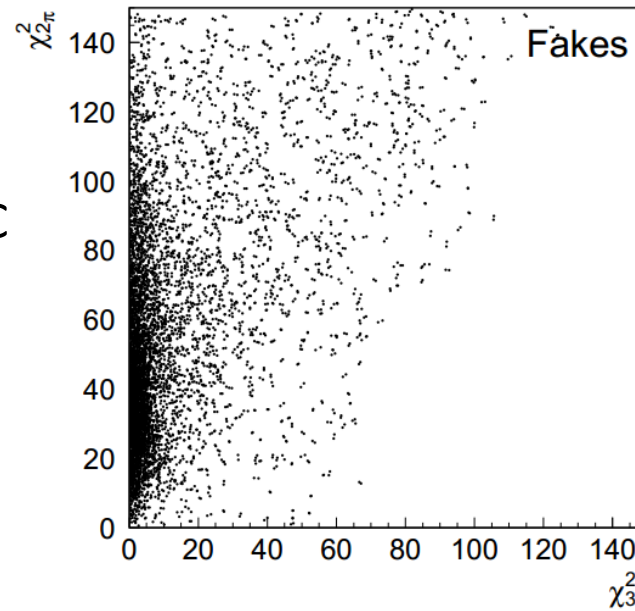
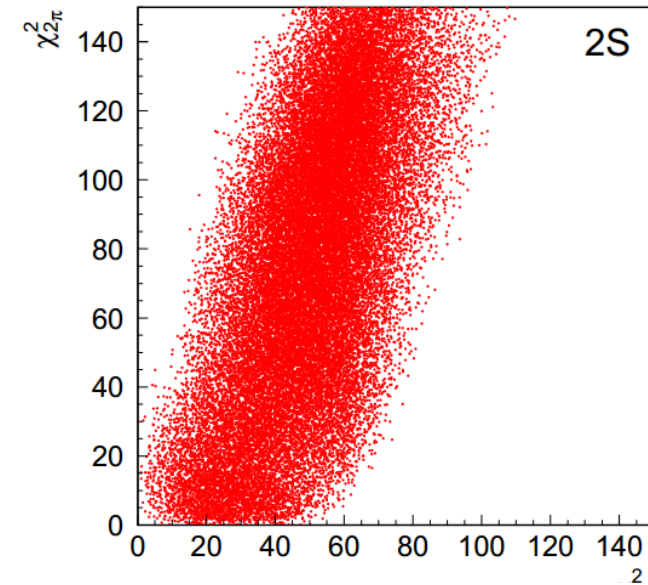
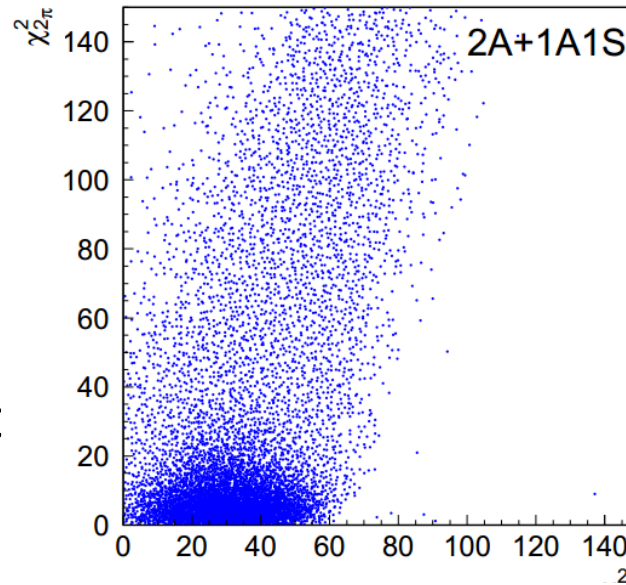
- DATA
- MC

$$F_k = \frac{N_{ev}(N_\gamma = k)}{\sum_{i=3}^6 N_{ev}(N_\gamma = i)}$$





- Using shapes of the MC categories we have fitted the $(\chi^2_{2\pi} \chi^2_{3\pi})$ distribution
- Results of the fit are then used to weight MC events

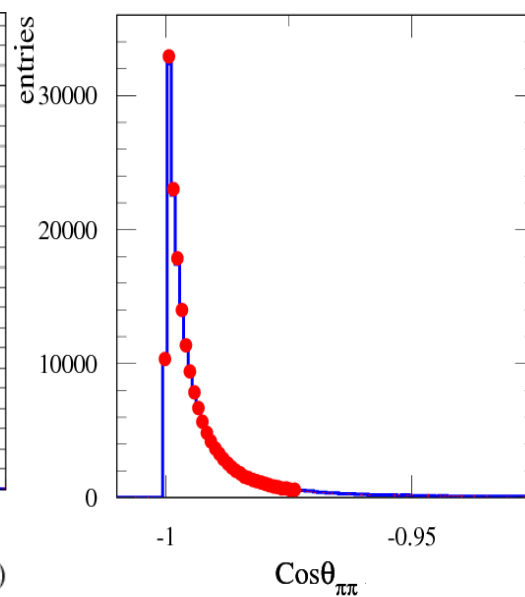
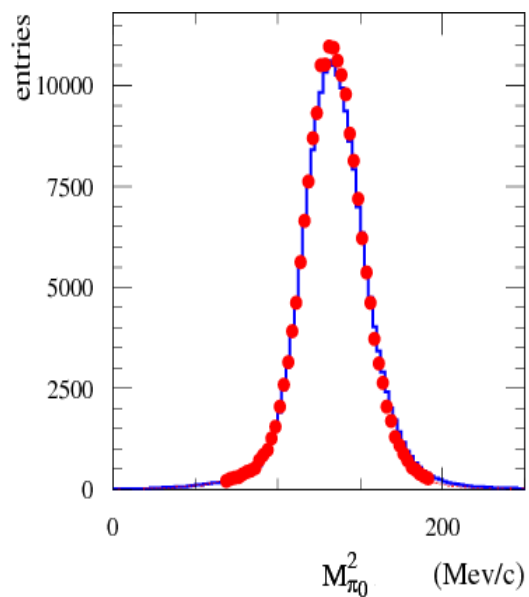
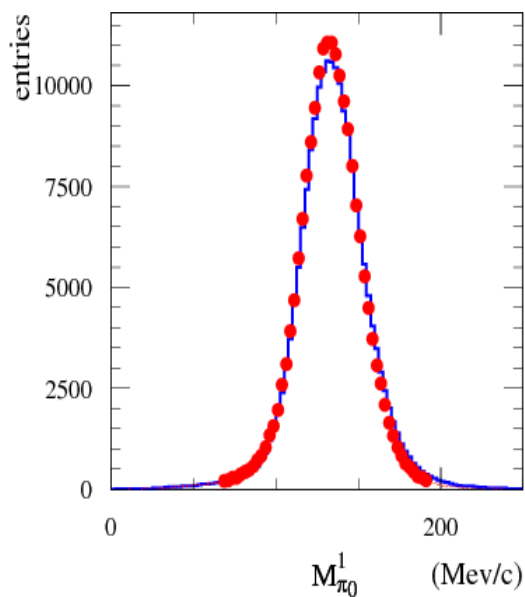
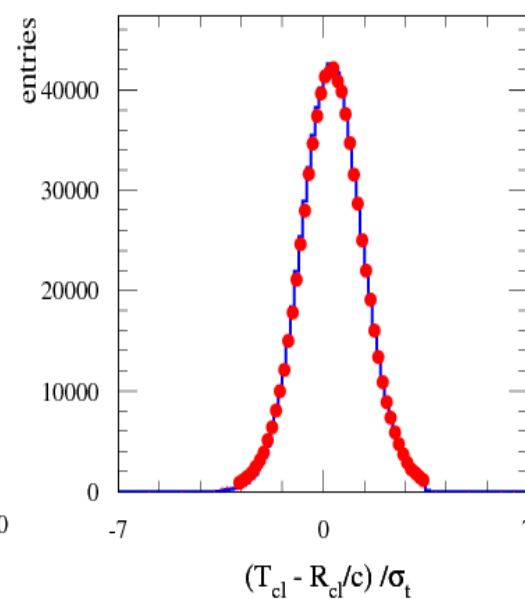
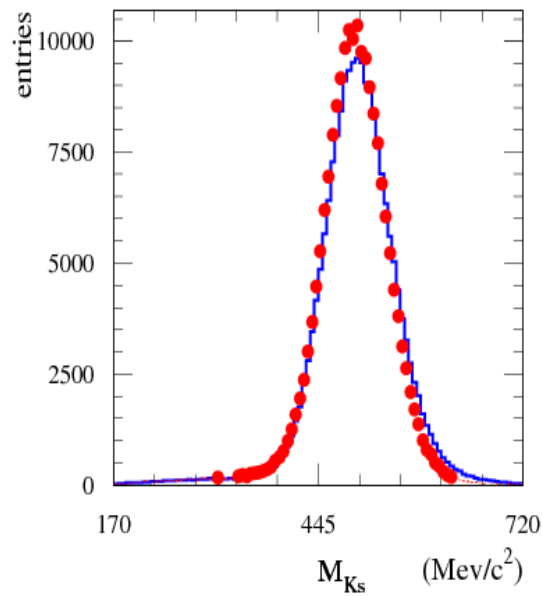
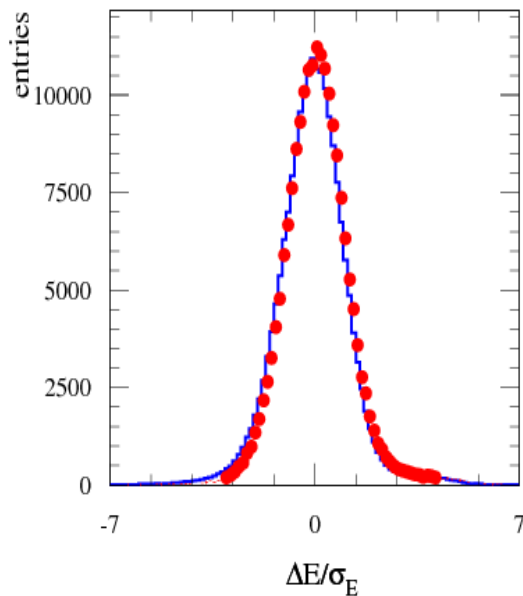




Monte Carlo calibration



● DATA
● MC





Search for the $K_S \rightarrow \pi^0 \pi^0 \pi^0$ decay



- Using the following set of cuts:

$$\left. \begin{array}{l} E_{\text{cr}} > 129 \text{ MeV} \\ 0.196 \leq \beta_{\text{cr}} \leq 0.25 \end{array} \right\} \varepsilon_{\text{cr}} \approx 28\% \quad \left. \begin{array}{l} \chi^2_{\text{fit}} < 35 \\ \Delta E / \sigma_E \geq 1.7 \\ 12.1 \leq \chi^2_{2\pi} \leq 60 \\ \chi^2_{3\pi} \leq 4.6 \\ R_{\text{min}} > 65 \text{ cm} \end{array} \right\} \varepsilon_{3\pi} = 0.19 \pm 0.012$$

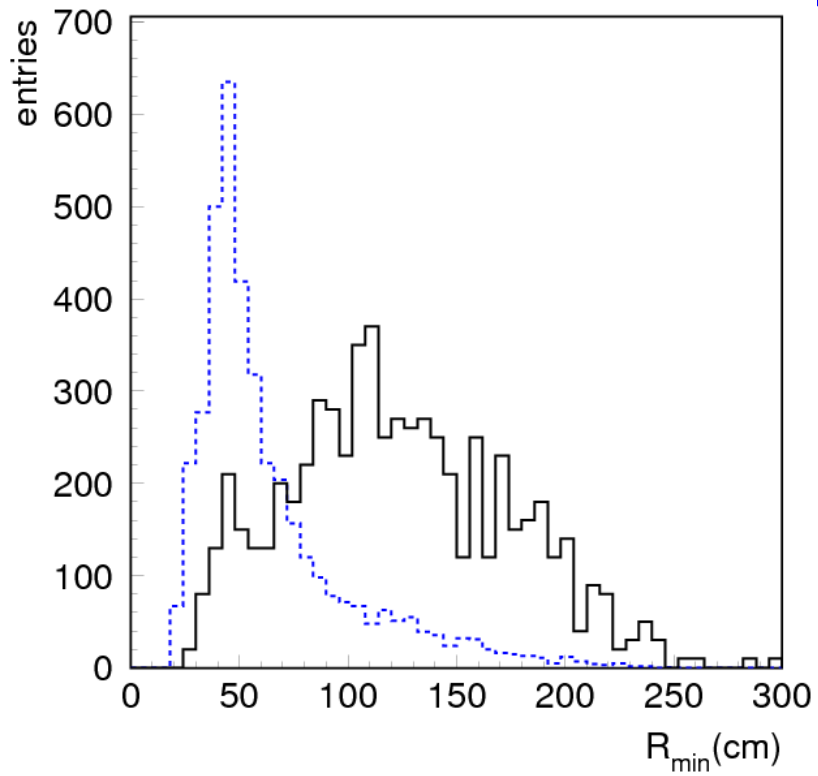
We count $N_{\text{obs}} = 0$ event selected as a signal and $N_{\text{exp}} = 0$ events in MC

- SM prediction:** 1 event after tagging $\Rightarrow$ 0.2 after selection
- The selection efficiency for $K_S \rightarrow 2\pi^0$ decay: $\varepsilon_{2\pi} \sim 0.66$
- Upper limit on signal events: $N_{3\pi} < 13$ (90% C.L.)
- Normalization sample: $N_{2\pi} = 90062000 / \varepsilon_{2\pi} = 1.4 \cdot 10^8$

PRELIMINARY

$$BR(K_S \rightarrow 3\pi^0) = \frac{N_{3\pi} / \varepsilon_{3\pi}}{N_{2\pi} / \varepsilon_{2\pi}} \times BR(K_S \rightarrow 2\pi^0) < 2.9 \times 10^{-8}$$

PRELIMINARY



- If the CP symmetry is conserved the allowed nonleptonic decays are:

$$K_S \rightarrow 2\pi \text{ and } K_L \rightarrow 3\pi$$

- Two pion system:

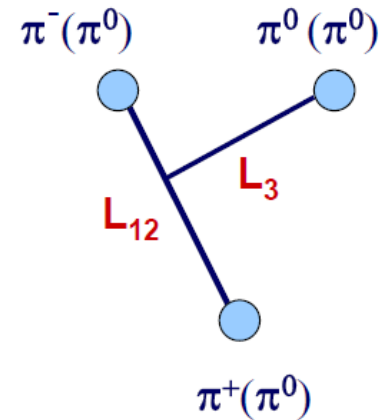
L - the angular momentum of the system

$$\mathbf{P}(\pi^0\pi^0) = P_\pi^2(-1)^L = 1 \text{ (spin of kaon is zero); } \mathbf{C}(\pi^0\pi^0) = C_\pi^2 = 1,$$

$$\mathbf{CP}(\pi^0\pi^0) = 1$$

$$\mathbf{P}(\pi^+\pi^-) = P_\pi^2(-1)^L; \mathbf{C}(\pi^+\pi^-) = (-1)^L = 1$$

$$\mathbf{CP}(\pi^+\pi^-) = 1$$



- Three pion system:

L12 - the angular momentum of a pair of pions in their center of mass frame

L3 - the angular momentum of the third pion on the rest frame of kaon

$$\mathbf{P}(\pi^0\pi^0\pi^0) = P_\pi^3(-1)^{L12}(-1)^{L3} = -1 \text{ (L12+L3 = 0); } \mathbf{C}(\pi^0\pi^0\pi^0) = C_\pi^3 = 1,$$

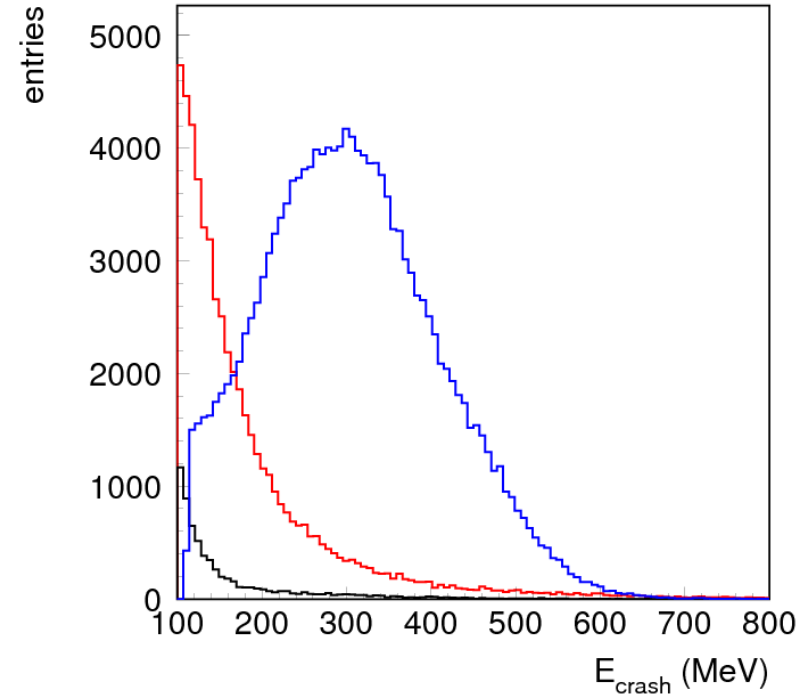
$$\mathbf{CP}(\pi^0\pi^0\pi^0) = -1$$

$$\mathbf{P}(\pi^+\pi^-\pi^0) = P_\pi^3(-1)^{L12}(-1)^{L3} = -1; \mathbf{C}(\pi^+\pi^-\pi^0) = \mathbf{C}(\pi^0) \mathbf{C}(\pi^+\pi^-) = (-1)^{L12}$$

$$\mathbf{CP}(\pi^+\pi^-) = (-1)^{L12+1} = -1 \text{ (L12=0)}$$



- We then fit to the energy distribution using shapes of **True K_L crash**, **K_L passed through** and Fake.
- For the Real K_L -crash events we apply a 12% correction to the energy
- The results of both fits:



	Weight	Number of events expected in data
2ACC+ 1A1S	$0,424 \pm 0,038$	27495 ± 247
2S	$0,314 \pm 0,023$	40160 ± 429
FAKE	$1,27 \pm 0,18$	7222 ± 158
OTHERS	$0,102 \pm 0,01$	1810 ± 432
True K_L crash	0.317 ± 0.024	49038 ± 318
K_L passed through	0.405 ± 0.037	22264 ± 260