

Exclusive meson pair production in proton-proton collisions

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Introduction

The 4-body reactions $pp \rightarrow p \pi^+ \pi^- p$ and $pp \rightarrow p K^+ K^- p$ constitutes an irreducible background to 3-body processes $pp \rightarrow p M p$, where e.g. $M = \sigma, \rho^0, f_0(980), \phi, f_2(1270), f_0(1500), f_2'(1525), \chi_{c0}$, glueball $\rightarrow$ these resonances are seen (or will be seen) "on" the $\pi\pi$ and/or KK continuum

Measurement of χ_c at Tevatron (CDF Collaboration)

$$\chi_c \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) + \gamma, \quad \left. \frac{d\sigma_{\chi_c}}{dy} \right|_{y=0} = (76 \pm 14) \text{ nb}$$

[T. Aaltonen et al., Phys. Rev. Lett. **102** (2009) 242001]

$M(J/\psi\gamma)$ resolution does not allow a separation of the different χ_{cJ} states!

Channel	$\mathcal{B}(\chi_{c0})$	$\mathcal{B}(\chi_{c1})$	$\mathcal{B}(\chi_{c2})$
$J/\psi\gamma$	$(1.16 \pm 0.08)\%$	$(34.4 \pm 1.5)\%$	$(19.5 \pm 0.8)\%$

but $\sigma(\chi_{c0})$ obtained within the k_t -factorization is much bigger than for χ_{c1} and χ_{c2}

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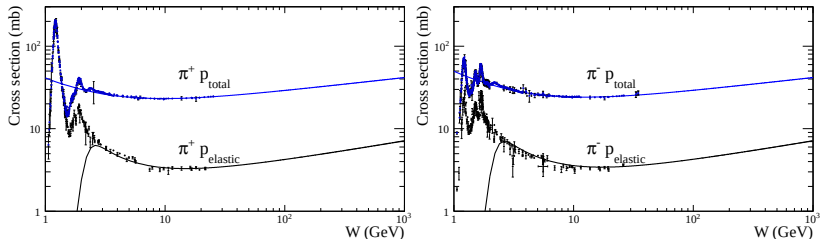
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Could other decay channels be used ?

Channel	$\mathcal{B}(\chi_{c0})$	$\mathcal{B}(\chi_{c1})$	$\mathcal{B}(\chi_{c2})$
$\pi^+ \pi^-$	$(0.56 \pm 0.03)\%$	—	$(0.16 \pm 0.01)\%$
$K^+ K^-$	$(0.610 \pm 0.035)\%$	—	$(0.109 \pm 0.008)\%$
$p\bar{p}$	$(0.0228 \pm 0.0013)\%$	$(0.0073 \pm 0.0004)\%$	$(0.0072 \pm 0.0004)\%$
$\pi^+ \pi^- \pi^+ \pi^-$	$(2.27 \pm 0.19)\%$	$(0.76 \pm 0.26)\%$	$(1.11 \pm 0.11)\%$
$\pi^+ \pi^- K^+ K^-$	$(1.80 \pm 0.15)\%$	$(0.45 \pm 0.10)\%$	$(0.92 \pm 0.11)\%$

Exclusive meson pair production in proton-proton collisions

πp cross sections



- Donnachie-Landshoff parametrization for total πN cross section

($\sigma_{tot}^{\pi p} = C_i s^{\alpha_i(0)-1}$, $i = IP, IR$):

$$\sigma_{tot}^{\pi^+ p}: 13.63s^{0.0808} + 27.56s^{-0.4525}$$

$$\sigma_{tot}^{\pi^- p}: 13.63s^{0.0808} + 36.02s^{-0.4525}$$

- The optical theorem: $\sigma_{tot}^{\pi p} \simeq \frac{1}{s} \text{Im} M_{el}^{\pi p}(s, t=0)$ (when s is large)

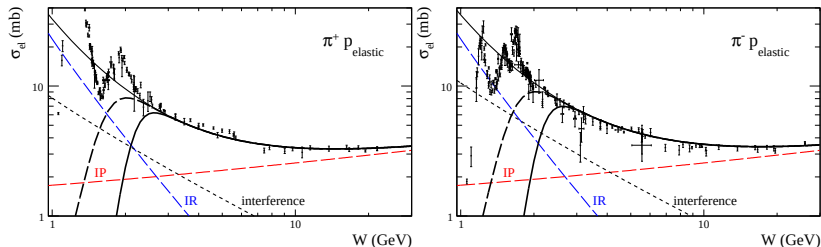
- $M_{\pi \pm p}(s, 0) = A_{IP}(s) + A_{f_2}(s) \mp A_\rho(s)$

- $M_{\pi p \rightarrow \pi p}(s, t) = \eta_i s C_i \left(\frac{s}{s_0}\right)^{\alpha_i(t)-1} \exp\left(\frac{B_i^{\pi p}}{2} t\right)$

the values of pomeron and reggeon couplings to πp :

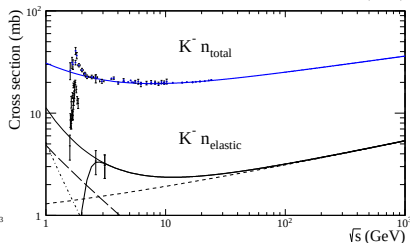
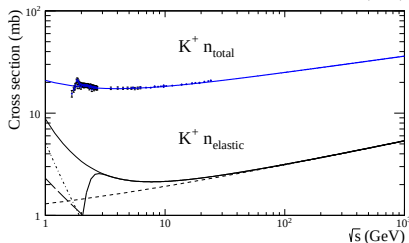
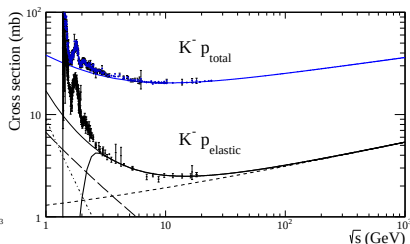
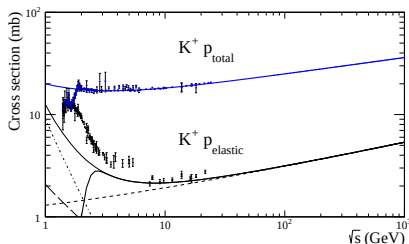
$$C_{IP} = 13.63 \text{mb}, C_{f_2} = 31.79 \text{mb}, C_\rho = 4.23 \text{mb}$$

πp elastic scattering



- nicely describes the $\pi p_{elastic}$ data for $\sqrt{s} > 2.5$ GeV with slope parameters $B(s) = B_i^{\pi p} + 2\alpha'_i \ln(\frac{s}{s_0})$: $B_{IP}^{\pi p} = 5.5 \text{ GeV}^{-2}$ and $B_{IR}^{\pi p} = 4 \text{ GeV}^{-2}$
- smooth cut-off correction factor $f_{cont}^{\pi N}(W) = \exp\left(\frac{W - W_{cut}}{a_{cut}}\right) / (1 + \exp\left(\frac{W - W_{cut}}{a_{cut}}\right))$
where $W_{cut} = 1.5 \text{ GeV}$ (dashed line) and 2 GeV (solid line), $a_{cut} = 0.2 \text{ GeV}$
- model includes absorption effects in an effective way

Kp and Kn cross sections



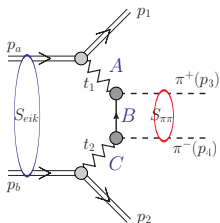
$$M_{K^\pm p}(s, 0) = A_{IP}(s) + A_{f_2}(s) + A_{a_2}(s) \mp A_\omega(s) \mp A_\rho(s)$$

$$M_{K^\pm n}(s, 0) = A_{IP}(s) + A_{f_2}(s) - A_{a_2}(s) \mp A_\omega(s) \pm A_\rho(s)$$

Absorption corrections

$$\mathcal{M}_{pp \rightarrow pp\pi\pi}^{\text{full}} = \mathcal{M}^{\text{Born}} + \mathcal{M}^{\text{pp-rescatt.}} + \mathcal{M}^{\text{\pi\pi-rescatt.}}$$

$$\mathcal{M}^{\text{Born}} = M_{13}(s_{13}, t_1) \frac{F_{\pi}^2(\hat{t})}{\hat{t} - m_{\pi}^2} M_{24}(s_{24}, t_2) + M_{14}(s_{14}, t_1) \frac{F_{\pi}^2(\hat{u})}{\hat{u} - m_{\pi}^2} M_{23}(s_{23}, t_2)$$



$$\mathcal{M}^{\text{pp-rescatt.}} = \frac{i}{8\pi^2 s} \int d^2 \mathbf{k}_t M_{NN}^{\text{el}}(s, k_t^2) \mathcal{M}^{\text{Born}}(\mathbf{p}_{a,t}^* - \mathbf{p}_{1,t}, \mathbf{p}_{b,t}^* - \mathbf{p}_{2,t})$$

where $p_a^* = p_a - k_t$ and $p_b^* = p_b + k_t$ with momentum transfer k_t

$$M_{NN}^{\text{el}}(s, k_t^2) = M_0(s) \exp(-B k_t^2/2)$$

from optical theorem: $\text{Im} M_0(s, t=0) = s \sigma_{\text{tot}}(s)$

$$B(s) = B_{IP}^{NN} + 2\alpha'_{IP} \ln\left(\frac{s}{s_0}\right)$$

where $s_0 = 1 \text{ GeV}^2$, $\alpha'_{IP} = 0.25 \text{ GeV}^{-2}$, $B_{IP}^{NN} = 9 \text{ GeV}^{-2}$

$\pi\pi$ -rescatt.

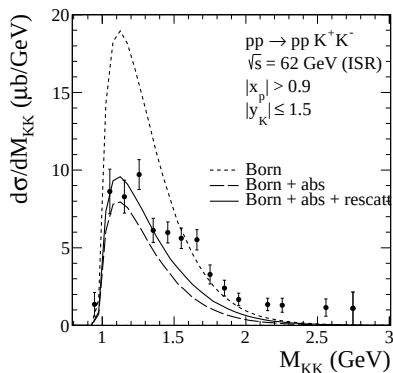
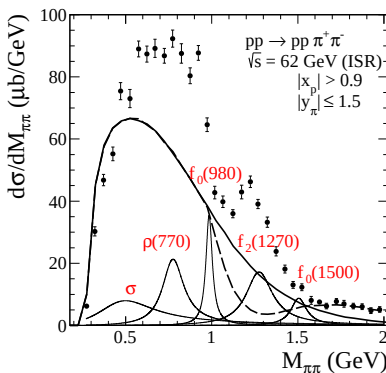
$$\frac{F_{\pi}^2(\hat{t})}{\hat{t} - m_{\pi}^2} \rightarrow \frac{i}{16\pi^2 \hat{s}} \int d^2 \kappa \frac{F_{\pi}^2(\hat{t}_1)}{\hat{t}_1 - m_{\pi}^2} M_{\pi^+ \pi^- \rightarrow \pi^+ \pi^-}(\hat{s}, \hat{t}_2)$$

$$\frac{F_{\pi}^2(\hat{u})}{\hat{u} - m_{\pi}^2} \rightarrow \frac{i}{16\pi^2 \hat{s}} \int d^2 \kappa \frac{F_{\pi}^2(\hat{u}_1)}{\hat{u}_1 - m_{\pi}^2} M_{\pi^- \pi^+ \rightarrow \pi^- \pi^+}(\hat{s}, \hat{u}_2)$$

$$\text{Regge-type interaction: } M_{\pi\pi \rightarrow \pi\pi}^{\text{Regge}}(\hat{s}, \hat{t}/\hat{u}) = \eta_i \hat{s} C_i^{\pi\pi} \left(\frac{\hat{s}}{\hat{s}_0}\right)^{\alpha_i(\hat{t}/\hat{u})-1} \exp\left(\frac{B_i^{\pi\pi}}{2} \hat{t}/\hat{u}\right),$$

$$\text{where } C_i^{\pi\pi} = \frac{(C_i^{\pi N})^2}{C_i^{NN}}, \quad i = IP, f_2, \rho$$

Our model of continuum vs ISR data



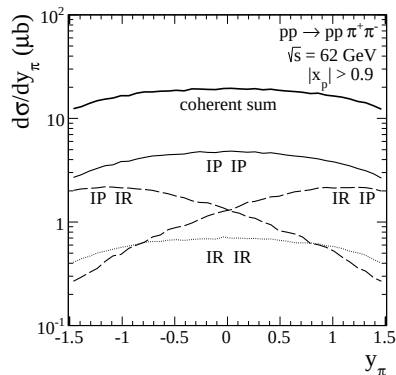
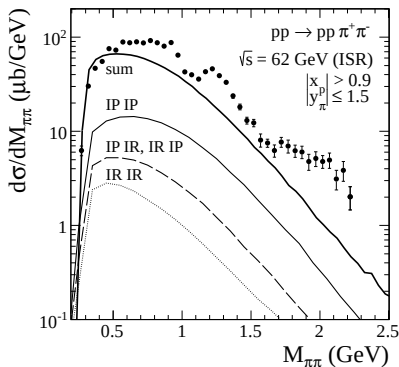
data from A. Breakstone *et al.* (ABCDHW Collaboration), Z. Phys. **C48** (1990) 569; **C42** (1989) 387

exp. cross sections: $\sigma_{pp \rightarrow pp \pi^+ \pi^-} = (79 \pm 13) \mu\text{b}$ and $\sigma_{pp \rightarrow pp K^+ K^-} = (6.5 \pm 1.7) \mu\text{b}$

where in $\mathcal{M}^{KK - rescatt.}$ we have $M_{KK \rightarrow KK} = \beta_M(\hat{s}) M^{\rho, \omega, \phi - meson \text{ exch.}} + \beta_R(\hat{s}) M^{Regge}$

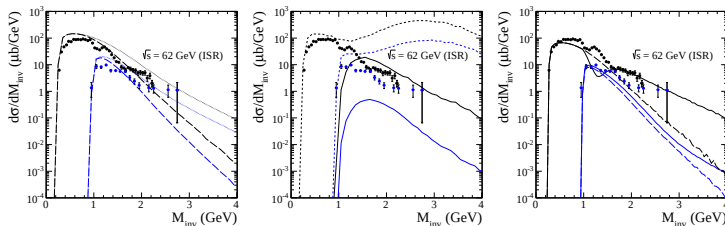
with $\beta_M(\hat{s}) = \exp(-(\hat{s} - 4m_K^2)/\Delta\hat{s})$, $\beta_R(\hat{s}) = 1 - \beta_M(\hat{s})$, $\Delta\hat{s} = 9 \text{ GeV}^2$

Our model of continuum vs ISR data



Decomposition of cross section in $M_{\pi\pi}$ and y_{π}
when all (upper line) and only some components in the amplitude are included

Our model vs ISR data



Black lines - $\pi^+\pi^-$ distributions, blue lines - K^+K^- distributions.

Left: born, mesonic propagator (dotted lines), mesonic + regge propagator (dashed lines).

We see that at $W = 4$ GeV, where secondary reggeons are small, we have a factor $(g_{IP}^{\pi\pi} / g_{IP}^{KK})^4 \approx 2$ suppression of cross section.

Central: born, $\pi\pi$ - and KK -rescat. contribution with smooth cut correction factor $S_{thr}(\hat{s})$ (solid lines).

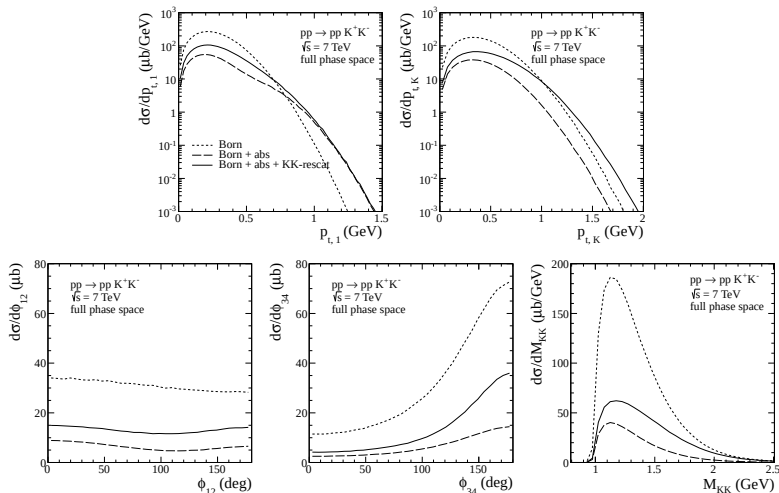
We see 2 orders of magnitude difference between the $\pi\pi$ and KK cross sections $\rightarrow$ role of formfactors !

$$S_{thr}(\hat{s}) = \begin{cases} 0, & \hat{s} \leq \hat{s}_{thr} = 4m_K^2, \\ 1 - \exp(-(\hat{s} - \hat{s}_{thr})/\Delta\hat{s}), & \hat{s} > \hat{s}_{thr} = 4m_K^2, \quad \Delta\hat{s} = 9 \text{ GeV}^2 \end{cases}$$

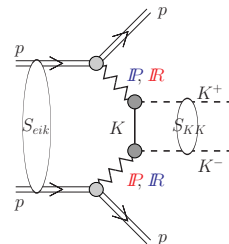
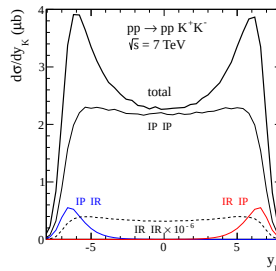
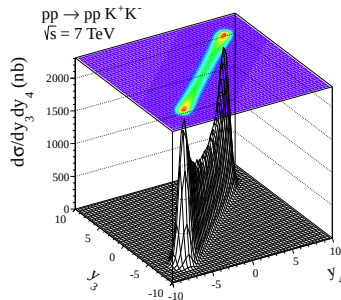
Right: born+abs (dashed lines), born+abs+rescat (solid lines) with cut correction factor $f_{thr}(s)$ for $\pi^+\pi^-$ -rescat. contribution.

At KK -rescat. contribution we included also vector meson exchanges.

Differential cross section at $\sqrt{s} = 7$ TeV

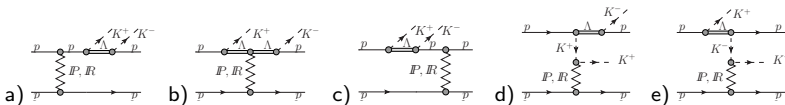


Differential cross section in rapidity space at $\sqrt{s} = 7$ TeV

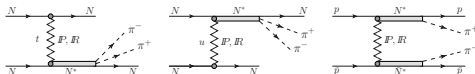
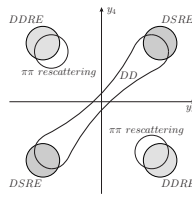
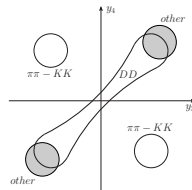
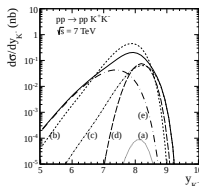
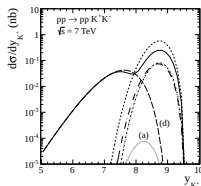


Center panel: Decomposition of cross section in ($y_K = y_3 \cong y_4$)
when all (upper line) and only some components in the amplitude are included
($IP \otimes IR$ and $IR \otimes IP$ peaks at backward and forward y_K)

Other diffractive processes

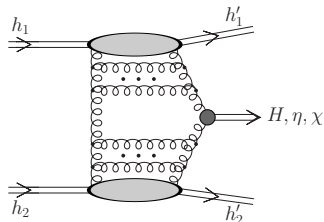


(+ diagrams with emission of kaons from second proton line)



(DSRE and DDRE)

Diffractive QCD mechanism



- QCD mechanism proposed by Kaidalov, Khoze, Martin, Ryskin (KKMR approach)

V.A. Khoze, A.D. Martin and M.G. Ryskin, Phys. Lett **B401** (1997) 330; Eur. Phys. J. **C23** (2002) 311

A.B. Kaidalov, V.A. Khoze, A.D. Martin and M.G. Ryskin, Eur. Phys. J. **C23** (2003) 387; **C33** (2004) 261

- to apply KKMR QCD mechanism to heavy quarkonia production ($H \rightarrow \chi_c$)

R.S. Pasechnik, A. Szczurek and O.V. Teryaev, Phys. Rev. **D78** (2008) 014007 (χ_{c0} meson)

R.S. Pasechnik, A. Szczurek and O.V. Teryaev, Phys. Lett. **B680** (2009) 62 (χ_{c1} meson)

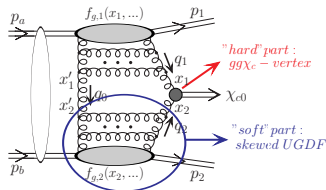
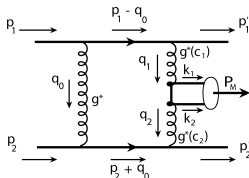
R.S. Pasechnik, A. Szczurek and O.V. Teryaev, Phys. Rev. **D81** (2010) 034024 (χ_{c2} meson)

L.A. Harland-Lang, V.A. Khoze, M.G. Ryskin and W.J. Stirling, Eur. Phys. J. **C65** (2010) 433

L.A. Harland-Lang, V.A. Khoze, M.G. Ryskin and W.J. Stirling, Eur. Phys. J. **C71** (2011) 1545

- It is interesting to test KKMR approach for diffractive light mesons production at high energies
 - a good probe of nonperturbative dynamics of partons described by UGDFs.

Amplitude for exclusive process $pp \rightarrow pp\chi_{c0}$



decomposition of gluon momenta

$$q_{1,2} = x_{1,2}p_{1,2} + q_{1/2\perp}, \quad 0 < x_{1,2} < 1$$

$$q_0 = x'_1 p_1 + x'_2 p_2 + q_{0\perp} \approx q_{0\perp}, \quad x'_1 \sim x'_2 = x' \ll x_{1,2}$$

$$\mathcal{M}_{pp \rightarrow pp\chi_c}^{\text{Born}} \sim \Im \int d^2 q_{0,t} V(\mathbf{q}_{1,t}, \mathbf{q}_{2,t}) \frac{f_{g,1}^{\text{off}}(x_1, x'_1, q_{0,t}^2, q_{1,t}^2, t_1) f_{g,2}^{\text{off}}(x_2, x'_2, q_{0,t}^2, q_{2,t}^2, t_2)}{q_{0,t}^2 q_{1,t}^2 q_{2,t}^2}$$

$$V(\mathbf{q}_{1,t}, \mathbf{q}_{2,t}) = K_{\text{NLO}} \frac{8ig_s^2}{M_\chi} \frac{\mathcal{R}'(0)}{\sqrt{\pi M_\chi N_c}} \frac{3M_\chi^2 \mathbf{q}_{1,t} \mathbf{q}_{2,t} - 2\mathbf{q}_{1,t}^2 \mathbf{q}_{2,t}^2 - (\mathbf{q}_{1,t} \mathbf{q}_{2,t})(\mathbf{q}_{1,t}^2 + \mathbf{q}_{2,t}^2)}{(M_\chi^2 + \mathbf{q}_{1,t}^2 + \mathbf{q}_{2,t}^2)^2}$$

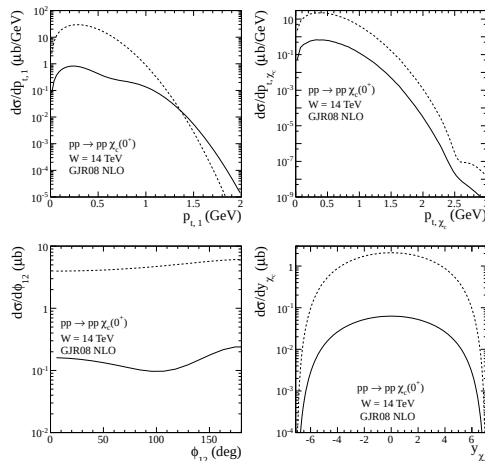
$gg \rightarrow \chi_{c0}$ vertex [Pasechnik, Szczurek and Teryaev] where active gluon virtualities (transverse momenta) are explicitly taken into account, $g_s^2 = 4\pi\alpha_s(M_\chi^2)$ - Shirkov-Solovtsov,

$$\mathcal{R}'_{\chi_{cJ}}(0) = \sqrt{0.075} \text{ GeV}^{5/2}, \quad K_{\text{NLO}} \simeq 1.68$$

$$\begin{aligned} & \text{effective f.f.} \\ & F(t) = \exp(bt/2), \\ & b = 4 \text{ GeV}^{-2} \end{aligned}$$

- $$x_{1,2} = \frac{M_{\perp}}{\sqrt{s}} \exp(\pm y)$$

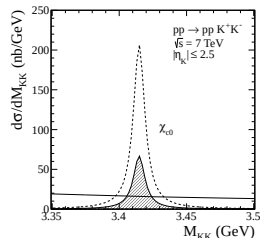
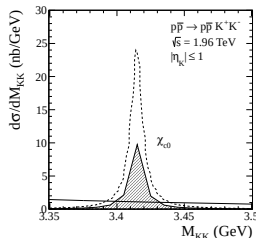
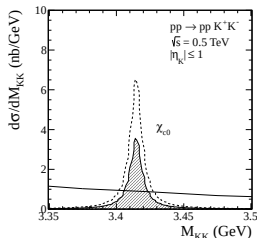
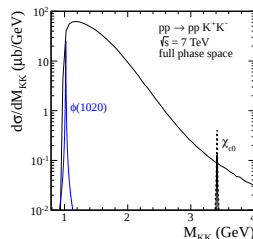
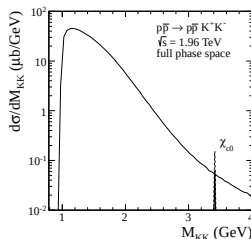
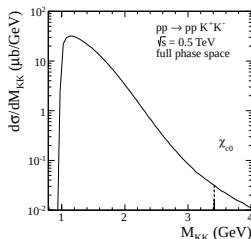
Differential cross sections for the $pp \rightarrow pp\chi_{c0}$ reaction



at $\sqrt{s} = 14 \text{ TeV}$

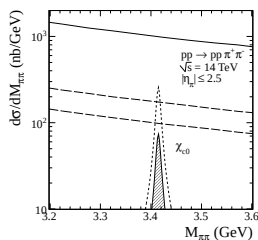
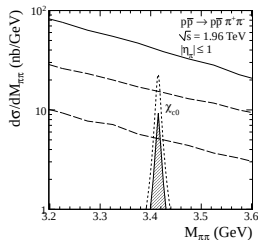
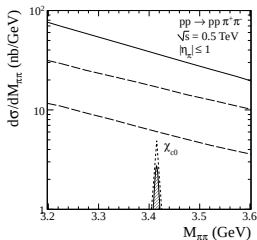
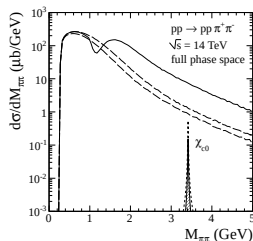
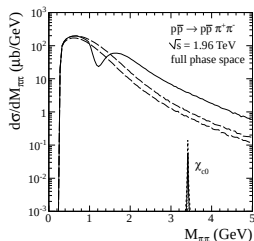
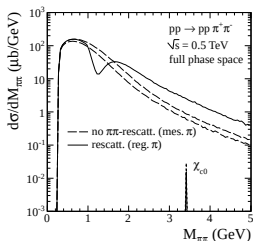
without (upper lines) and with (lower lines) absorption effects.

$M_{K^+K^-}$ distribution at $\sqrt{s} = 0.5, 1.96, 7$ TeV



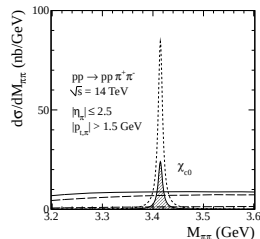
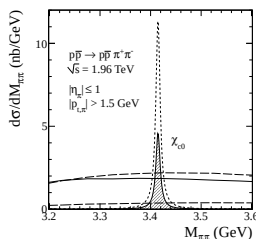
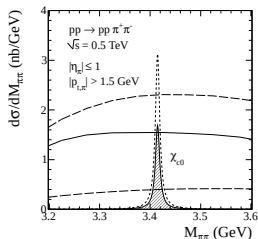
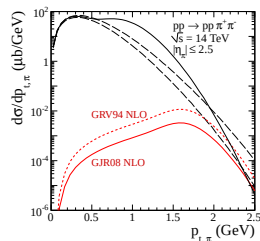
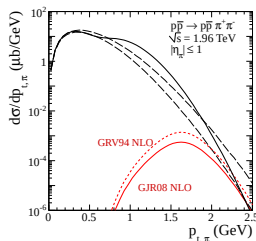
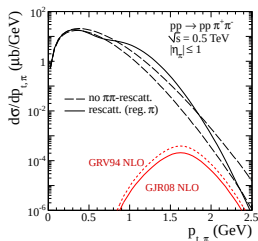
$$\frac{d\sigma_{\chi_{c0}}}{dM_{KK}} = \mathcal{B}(\chi_{c0} \rightarrow K^+ K^-) \sigma_{pp \rightarrow pp \chi_{c0}} 2M_{KK} \frac{1}{K} \frac{M_{KK} \Gamma}{(M_{KK}^2 - M^2)^2 + (M_{KK} \Gamma)^2}$$

$M_{\pi^+\pi^-}$ distribution at $\sqrt{s} = 0.5, 1.96, 14$ TeV



$p_{t,\pi}$ and $M_{\pi^+\pi^-}$ distributions at $\sqrt{s} = 0.5, 1.96, 14$ TeV

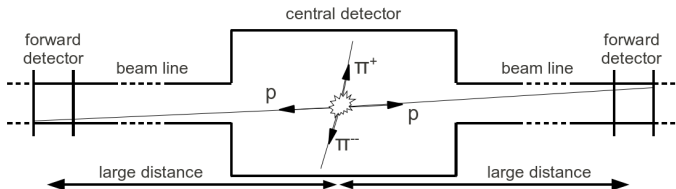
Pions from χ_{c0} decay are placed at slightly larger p_t



Exclusive $\pi^+\pi^-$ Production at the LHC with Forward Proton Tagging

R. Staszewski, P. Lebiedowicz, M. Trzebiński, J. Chwastowski, A. Szczurek,
Acta Phys. Polon. B 42 (2011) 1861

Huge total cross-section for $pp \rightarrow pp\pi^+\pi^-$: more than $200 \mu b$ for $\sqrt{s} = 7 \text{ TeV}$
(see P. Lebiedowicz, A. Szczurek, Phys. Rev. **D81** (2010) 036003)

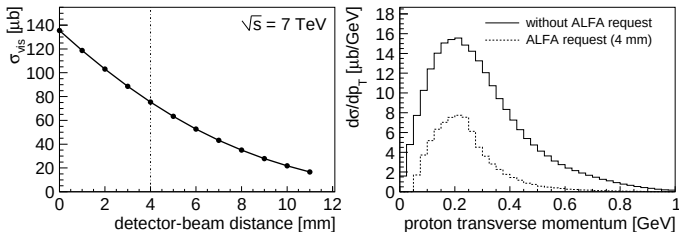


Pions detected in the ATLAS detector (tracker or calorimeter).

Protons tagged in the ALFA stations ($\sim 240 \text{ m}$ far from IP).

Calculations done for $\beta^* = 90 \text{ m}$ LHC optics, $\sqrt{s} = 7 \text{ TeV}$.

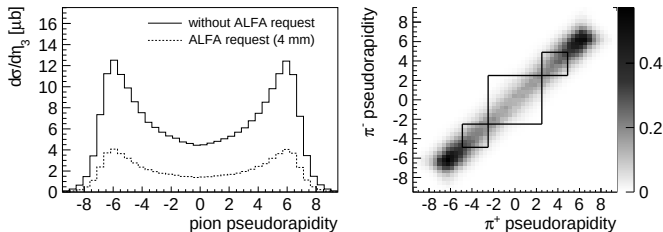
Exclusive $\pi^+\pi^-$ Production at the LHC with Forward Proton Tagging



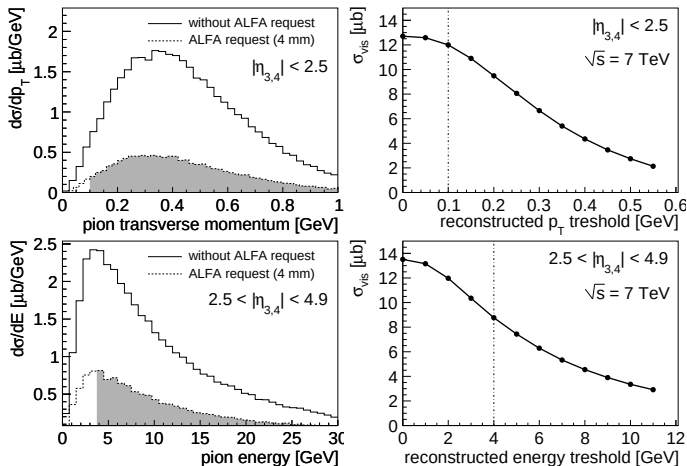
Left: Cross section visible in the ALFA detectors (both protons tagged) as a function of the distance between the detectors and the beam centre. Distance of 4mm corresponds to 75 μb of cross-section visible in the ALFA detectors.

Right: The proton p_T distribution; the dotted line marks the distribution for the events with both protons tagged by ALFA detectors positioned at 4 mm.

Most of outgoing protons are in ALFA acceptance region!



Exclusive $\pi^+\pi^-$ Production at the LHC with Forward Proton Tagging

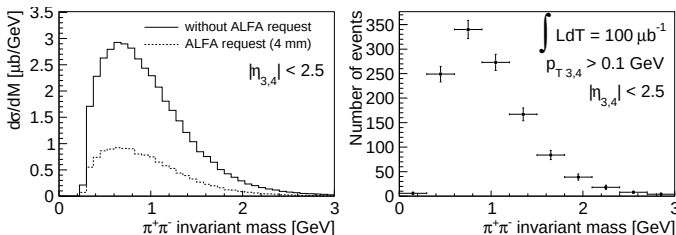


The grey area and the vertical dash-dotted line marks the lower boundary of the region accessible by ATLAS.

Clearly, the cross section falls very steeply with increasing thresholds values.

$\sigma_{\text{vis}} = 21 \mu\text{b}$ (with detector-beam distance 4 mm and $p_{t,\pi} = 0.1 \text{ GeV}$, $E_\pi = 4 \text{ GeV}$).

Exclusive $\pi^+\pi^-$ Production at the LHC with Forward Proton Tagging



Right: Possible measurement of the $\pi^+\pi^-$ invariant mass distribution for $L = 100 \mu b^{-1}$ (luminosity: $10^{27} \text{ cm}^{-2}\text{s}^{-1}$, data collecting time: 30h). Only the statistical errors are plotted.

With enough statistic it should be possible to see:

$f_2(1270)$, glueball candidates (e.g. $f_0(1500)$), charmonia (e.g. χ_{c0}).

→ Measurements of exclusive $\pi^+\pi^-$ is possible!

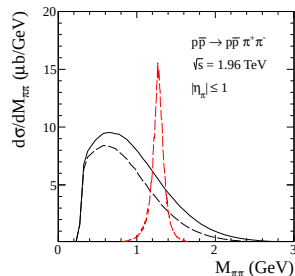
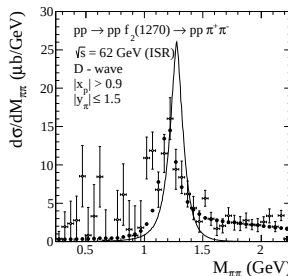
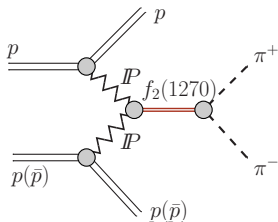
→ It requires ALFA trigger and low- p_t tracking.

→ Similar production of K^+K^- and $p\bar{p}$

$f_2(1270)$ production in the reaction: $pp \rightarrow (\text{tensor } IP) (\text{tensor } IP) \rightarrow pp\pi^+\pi^-$

see O. Nachtmann talk "A model for high-energy soft reactions", ECT* Trento, Exclusive and diffractive processes in high energy proton-proton and nucleus-nucleus collisions, February 27 - March 2, 2012

preliminary results:



data from A. Breakstone *et al.* (ABCDHW Collaboration), Z. Phys. **C48** (1990) 569

see talk M. Žurek

Conclusions

- Difficulty to separate $\chi_c(0^+)$, $\chi_c(1^+)$, $\chi_c(2^+)$ in the $J/\psi\gamma$ channel
- Possible in the $\pi^+\pi^-$, K^+K^- channels (at RHIC, Tevatron and LHC)
 → $pp\chi_{c0}$ grows much faster with $\sqrt{s}$ than $pp\pi^+\pi^-$, ppK^+K^-
 P. Lebiedowicz, R. Pasechnik and A. Szczurek, Phys. Lett. **B701**, 434 (2011)
 P. Lebiedowicz and A. Szczurek, Phys. Rev. **D85**, 014026 (2012)
- χ_c amplitudes can be written in terms of off-diagonal UGDF's
- Several differential distributions for $pp \rightarrow pp\chi_{c0}$, $pp\pi^+\pi^-$, ppK^+K^- processes including absorptive corrections are calculated
- With enough statistic it should be possible to see in $M_{\pi\pi}$:
 $f_2(1270)$, glueball candidates, charmonia (e.g. $\chi_c(0^+)$)
- Influence of kinematical cuts on the S/B ratio has been investigated