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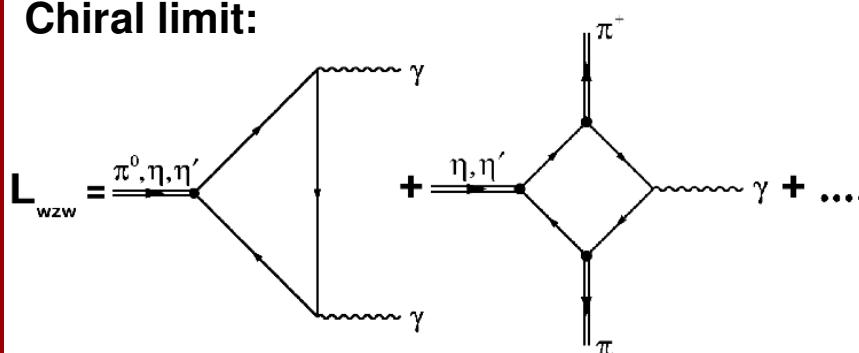
# Analysis of $\eta \rightarrow \pi^+ \pi^- \gamma$ measured with the WASA facility at COSY

June 14, 2010 | Christoph Florian Redmer  
for the WASA-at-COSY Collaboration



# Motivation

## Chiral limit:



Wess,Zumino, Phys.Lett. B 37 (1971) 95  
Witten, Nucl Phys B 223 (1983) 422

## Include FSI by unitarized extensions:

- momentum dependent VMD
- one loop corrections
- one loop + Omnes function
- Chiral Unitary Approach
- Hidden Local Symmetries

Picciotto  
Phys. Rev. D45 (1992) 1569

Bijnens  
Nucl. Phys. B637 (1991) 709

Holstein  
Phys Scr T99 (2002) 55

Borasoy,Nissler  
Nucl Phys A 740(2004) 362

Benayoun et al  
EPJ C 31 (2003) 525

## Previous Measurements:

7250 events

M. Gormley et al. Phys.Rev. D2 (1970) 501

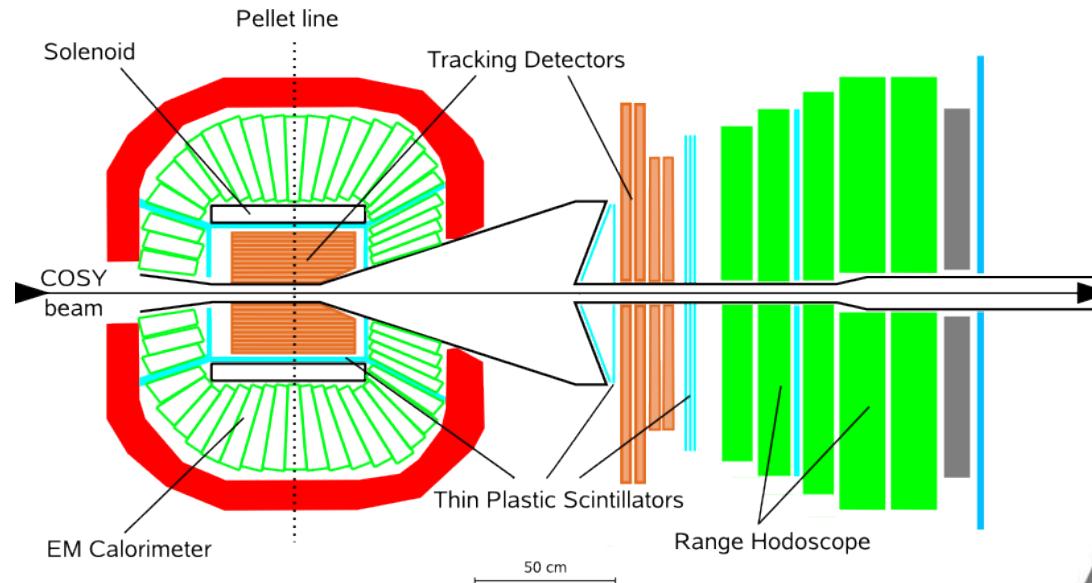
18150 events

J. G. Layter et al. Phys.Rev. D7 (1973) 2565

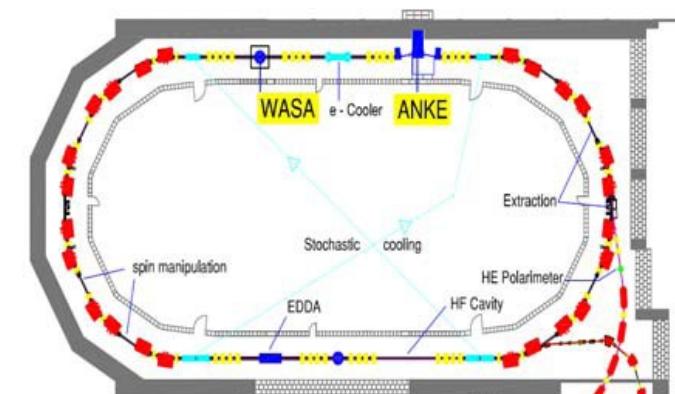
- low in statistics
  - largest samples not efficiency corrected
  - ambiguous theoretical interpretation of the samples
- new measurement



# The WASA facility at COSY



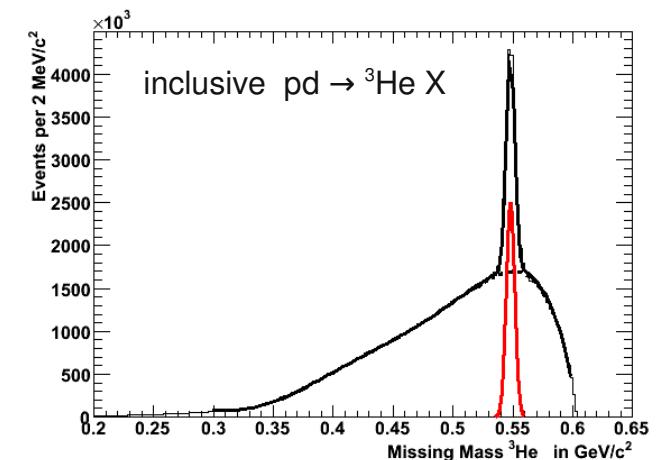
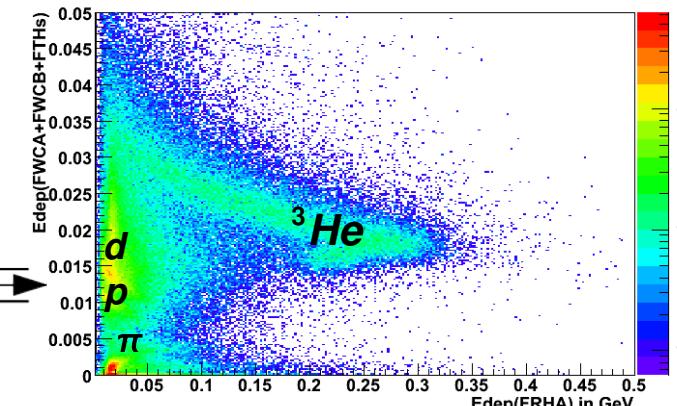
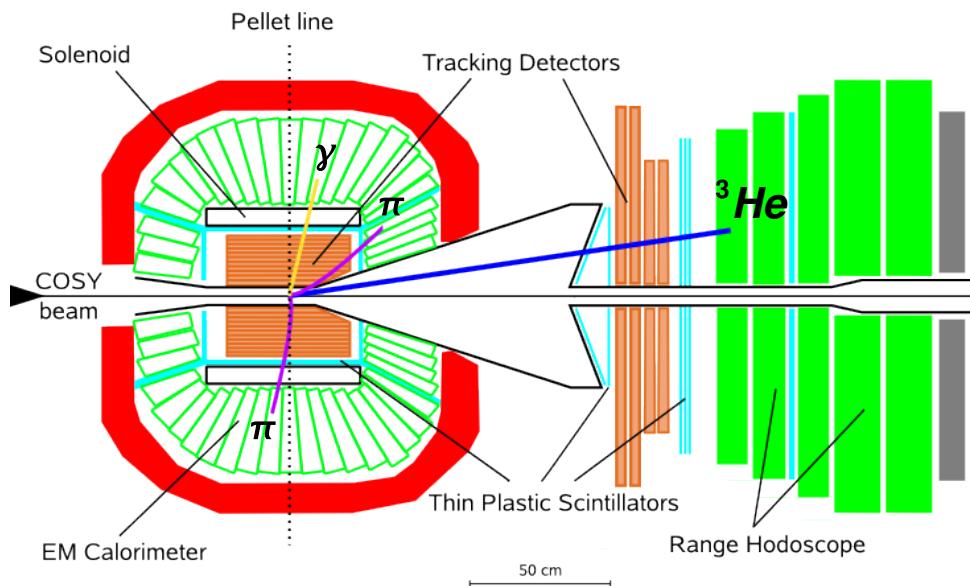
- high density pellet target
- $4\pi$  - acceptance
- charged and neutral particle detection



- p, d beams up to 3.7 GeV/c
- high intensity
- phase space cooling



# $\eta \rightarrow \pi^+ \pi^- \gamma$ at WASA



- $\text{pd} \rightarrow ^3\text{He} \eta$  (October 2008)
- $10^7$  tagged  $\eta$  mesons on disk
- exclusive measurement (Acceptance: 70%)

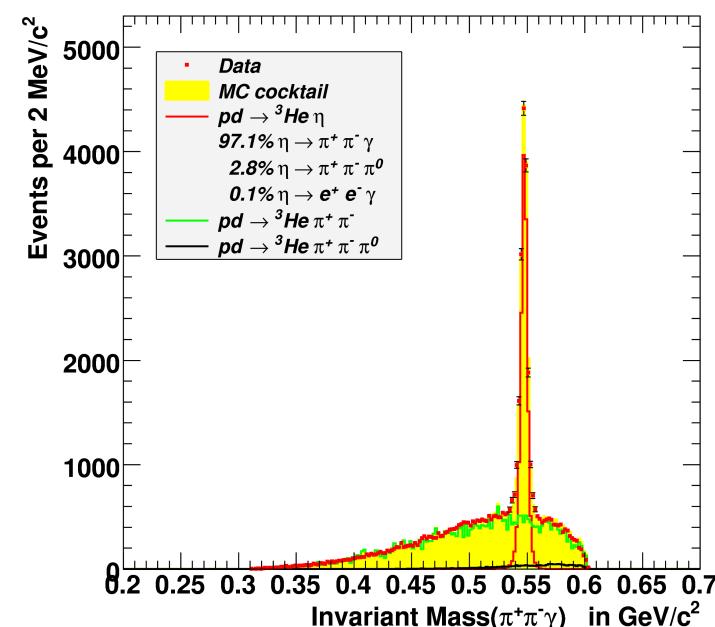
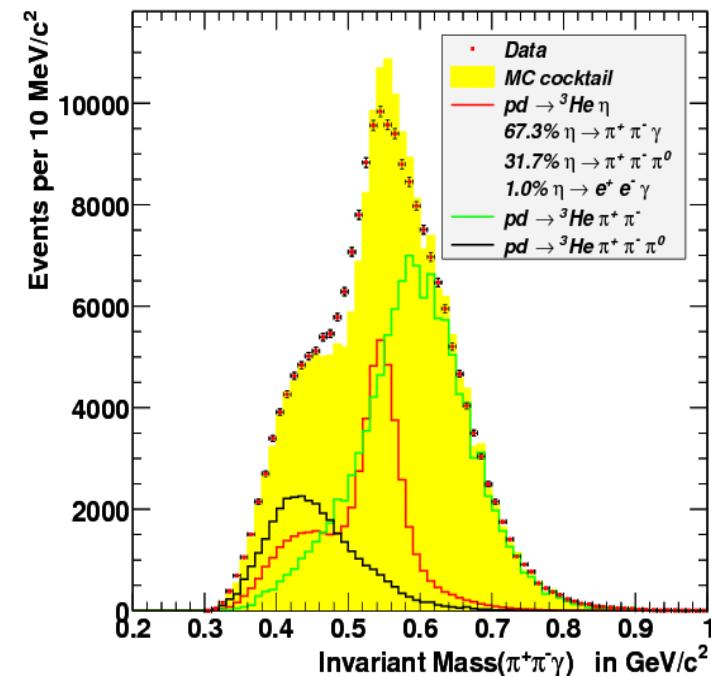


# Event Selection

- $\pi$  and  $\gamma$  candidates selected
- Missing Mass ( ${}^3\text{He}\gamma$ )  $\geq 2 m_\pi$
- reduction of hadronic splitoffs
- cut on  $\pi^0$  in Missing Mass ( ${}^3\text{He}\pi^+\pi^-$ )

dominated by  $\text{pd} \rightarrow {}^3\text{He} \pi^+ \pi^-$

- Kinematic Fit
  - $4C$  (energy and momentum)
  - cut on probability  $P(\chi_{KF}, N) > 0.1$
  - resolution improved by factor 10





# Background Subtraction

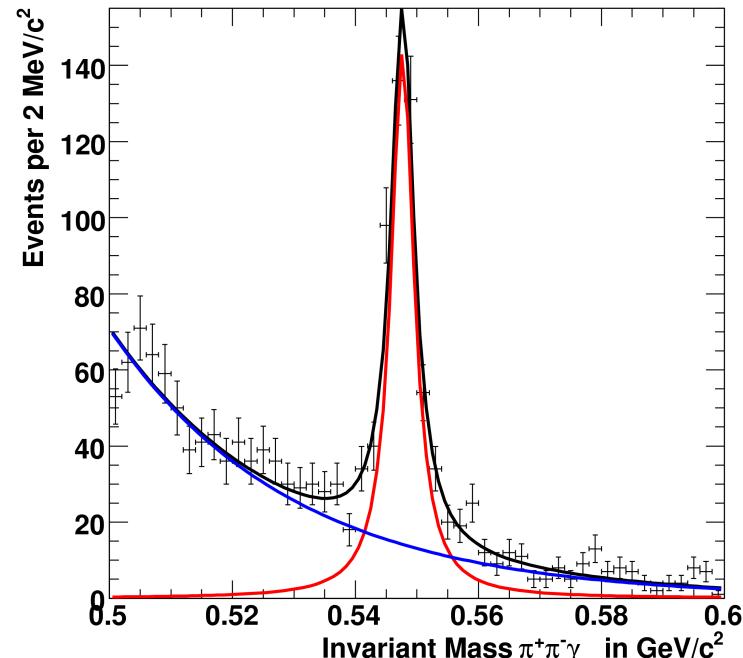
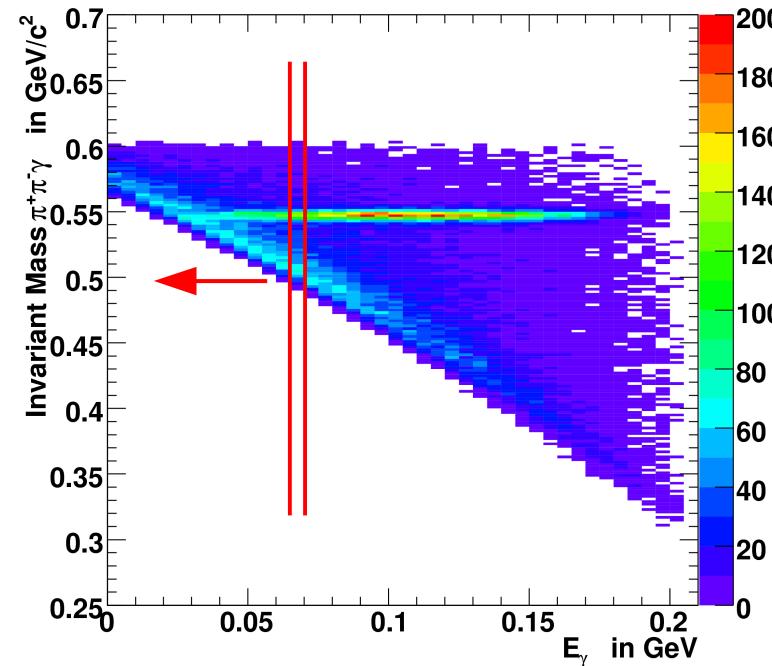
For each bin of a distribution:

- calculate invariant mass of  $\pi^+\pi^-\gamma$
- fit signal and background
- count signal events

Background from  $\eta$  decays is subtracted using Monte Carlo distributions

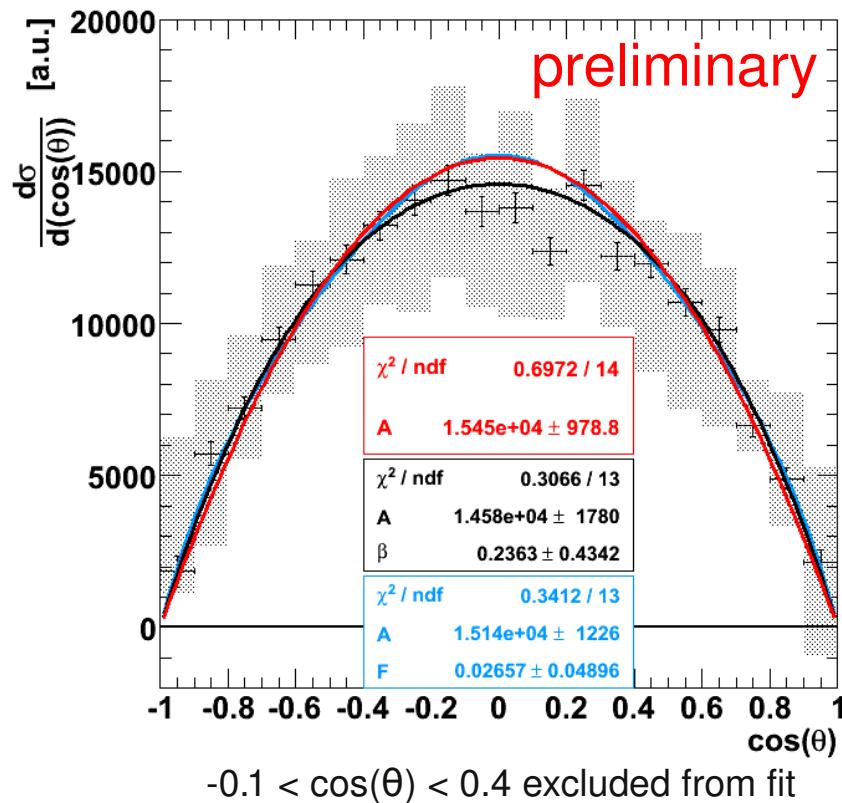
After background subtraction:

$13738 \pm 136$  events





# Dalitz Plot Distributions



$\cos(\theta)$ : Angle between  $\gamma$  and  $\pi^+$   
in the pion-pion rest frame

*p – wave:*

$$\frac{d\sigma}{d(\cos\theta)} = A \cdot \sin^2\theta$$

*p – wave + d – wave:*

$$\frac{d\sigma}{d(\cos\theta)} = A \cdot \sin^2\theta \cdot (1 + \beta \cos^2\theta)$$

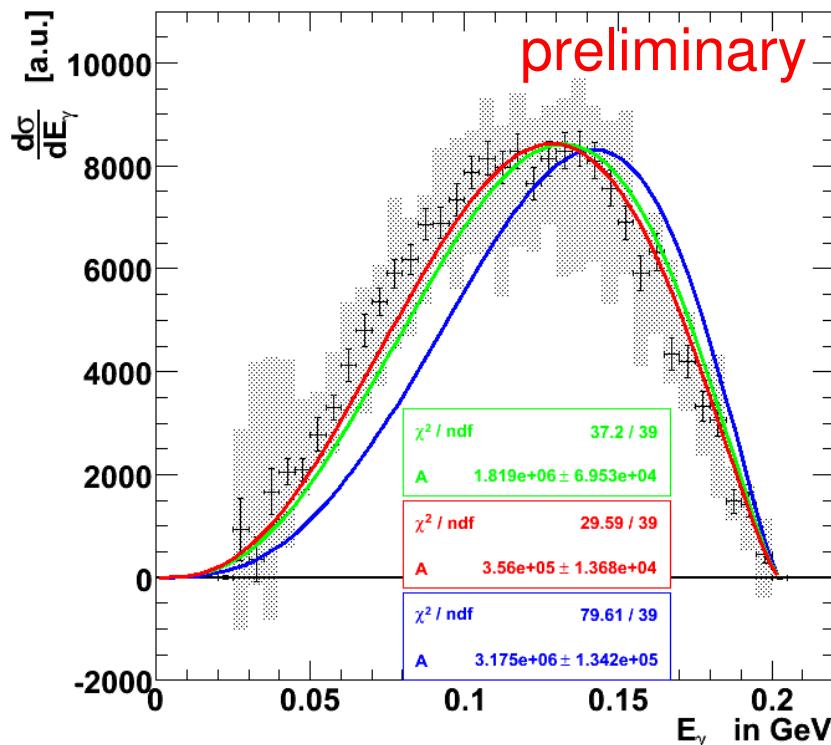
*p – wave + f – wave:*

$$\frac{d\sigma}{d(\cos\theta)} = A \cdot \sin^2\theta \cdot (1 + F(5\cos^2\theta - 1)^2)$$

- $\pi^+\pi^-$  system in relative *p – wave*
- contributions of higher partial waves negligible



# Dalitz Plot Distributions



$E_\gamma$ : Photon momentum  
in the  $\eta$  - rest frame

simplest matrix element:

$$\frac{d\sigma}{dE_\gamma} = A \cdot \left( \frac{E_\gamma}{m_\eta} \right)^3 \cdot \sqrt{1 - \frac{2E_\gamma}{m_\eta} - \frac{4m_\pi^2}{m_\eta^2}}^3 \cdot \frac{1}{\sqrt{1 - \frac{2E_\gamma}{m_\eta}}}$$

VMD with box anomaly term:

$$|A_\eta(s_{\pi\pi})|^2 = |A_\eta(0,0,0) \cdot \left( -1 + \frac{3m_\rho^2}{m_\rho^2 - s_{\pi\pi} - im_\rho \Gamma_\rho(s_{\pi\pi})} \right)|^2$$

without box anomaly term:

$$|A_\eta(s_{\pi\pi})|^2 = |A_\eta(0,0,0) \cdot \left( \frac{m_\rho^2}{m_\rho^2 - s_{\pi\pi} - im_\rho \Gamma_\rho(s_{\pi\pi})} \right)|^2$$

- simplest matrix element does not describe data
- description of FSI important



## Summary

Published data of low statistics, significant sets not efficiency corrected

WASA-at-COSY has a clean, high statistics sample of  $\eta \rightarrow \pi^+ \pi^- \gamma$

Studies of Dalitz plot distributions show:

- pions in relative p-wave, no evidence for higher partial waves
- FSI important to describe photon energy spectrum
  - *test of effective theories*



## Outlook

- three times more statistics available ( $\text{pd} \rightarrow {}^3\text{He } \eta$ )
- an 8 week production run just finished ( $\text{pp} \rightarrow \text{pp } \eta$ )
  - *the statistics of this work corresponds to 2 – 3 days of  $\text{pp} \rightarrow \text{pp } \eta$*
- ongoing improvements on systematic errors:
  - efficiency correction with VMD based distributions
  - alternative / additional means of multi pion suppression
  - charged particle reconstruction
- determination of the box anomaly contribution
- gain insight into anomalies of QCD with  $\eta \rightarrow \pi^+ \pi^- \gamma$

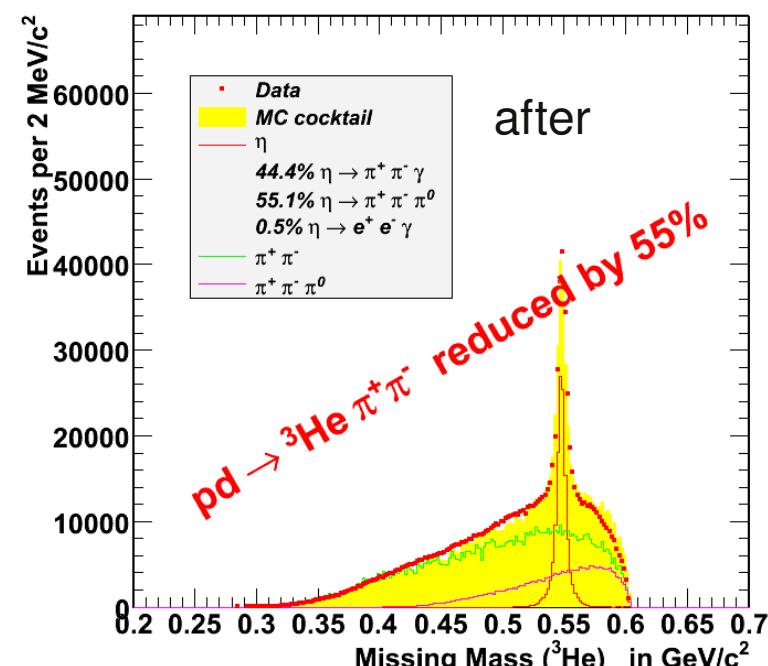
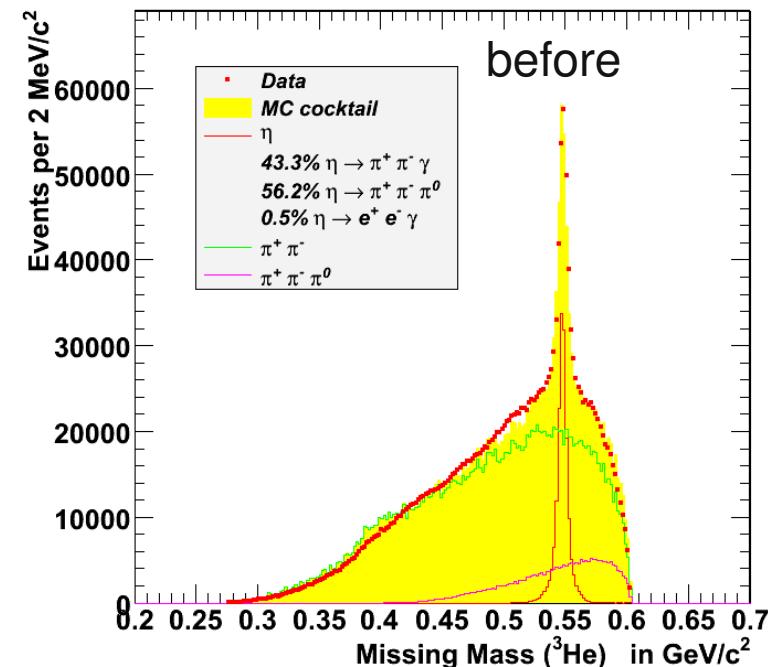
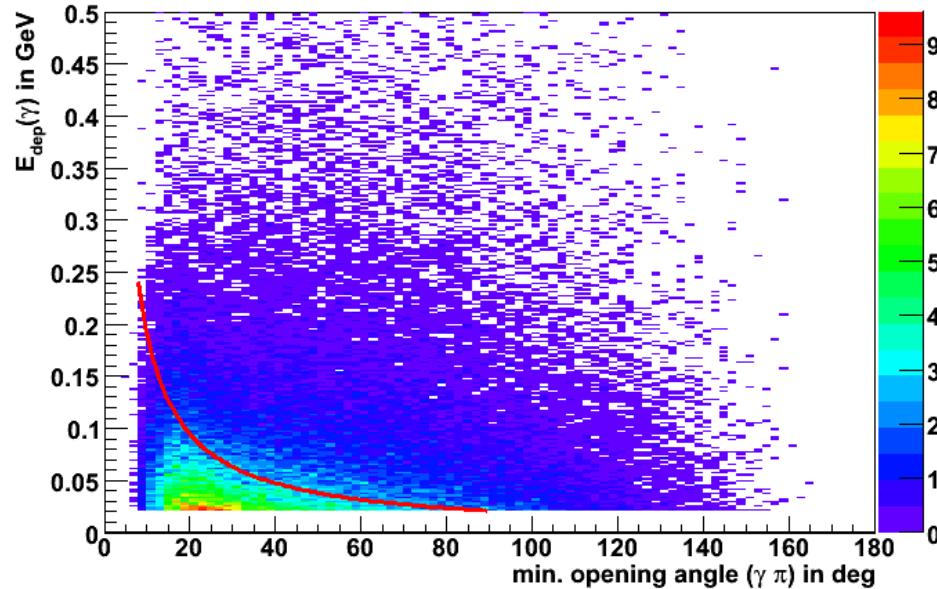


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# Backup



# Splitoff Suppression



## Characteristics:

- small distance to tracks
- small energy deposits



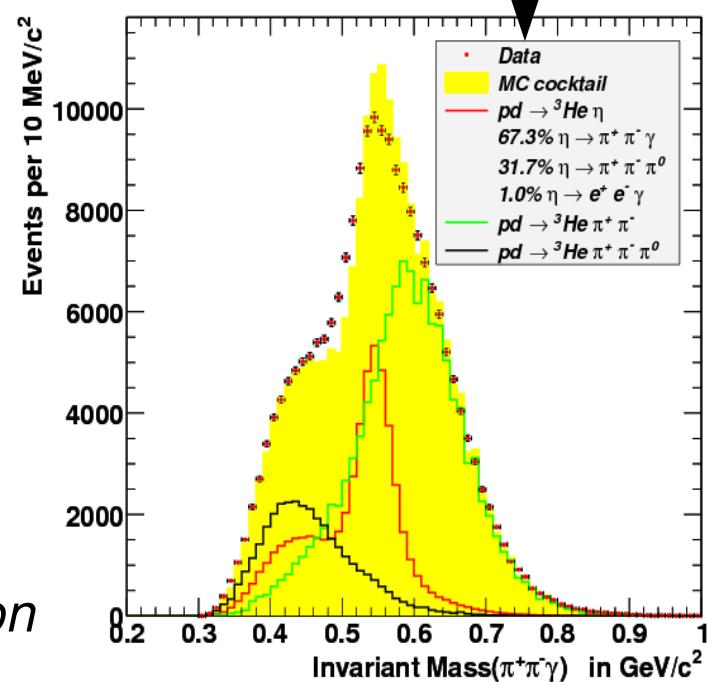
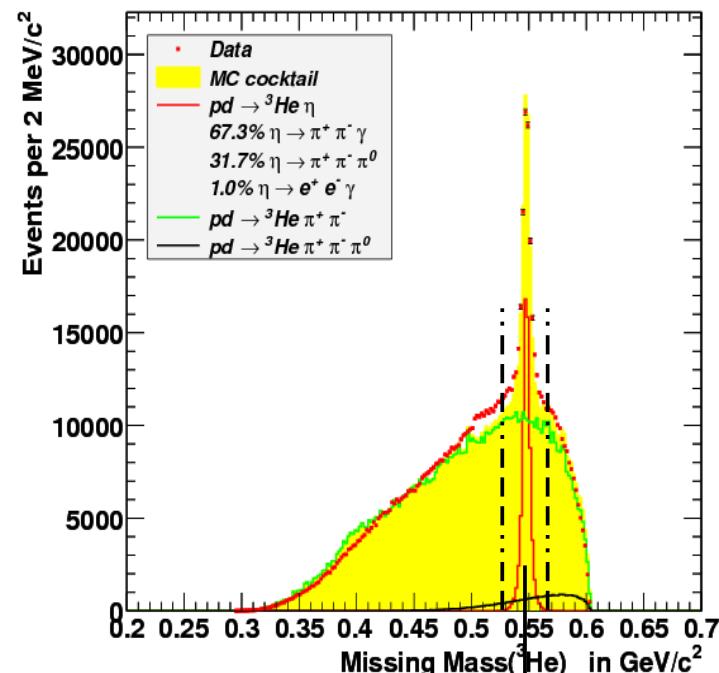
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dominated by  $\text{pd} \rightarrow {}^3\text{He} \pi^+ \pi^-$

→ use Kinematic Fit

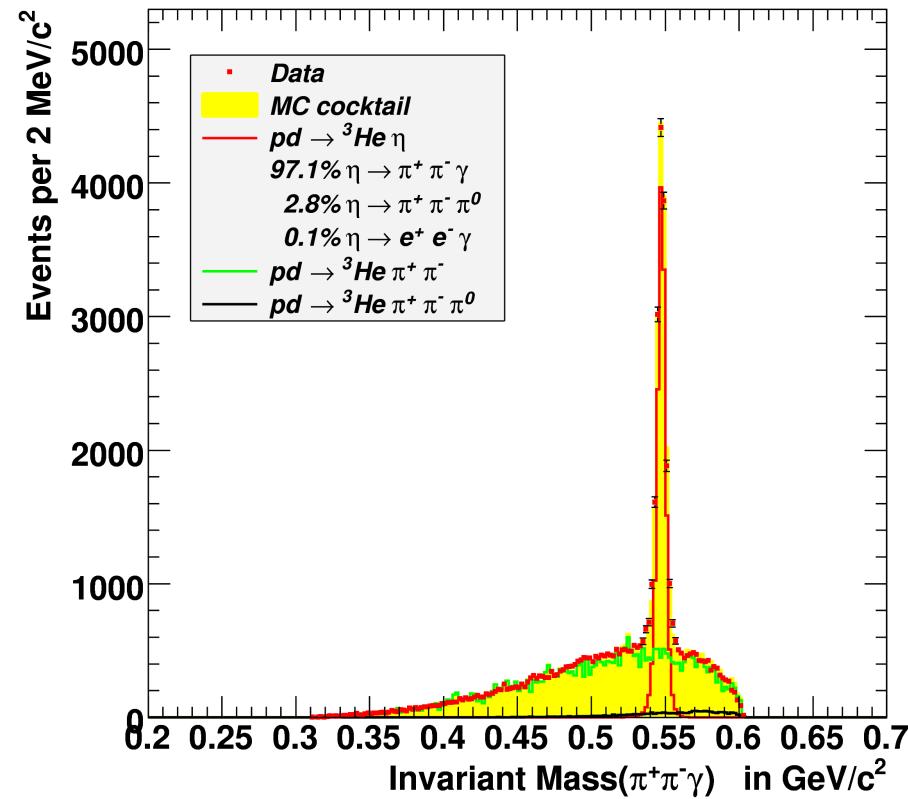
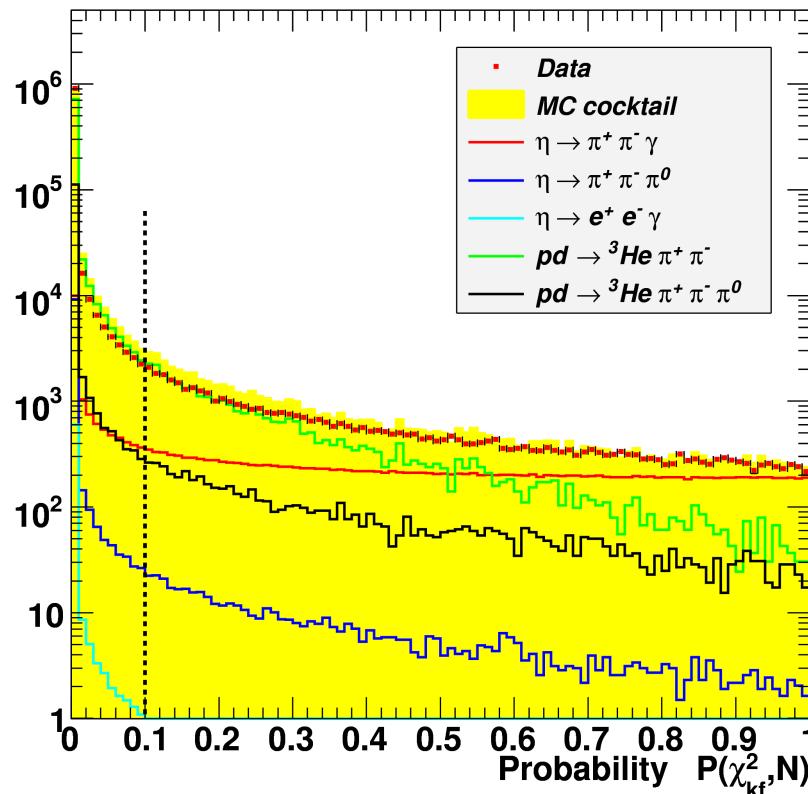
- *gain in resolution*
- *additional background suppression*





## Kinematic Fit

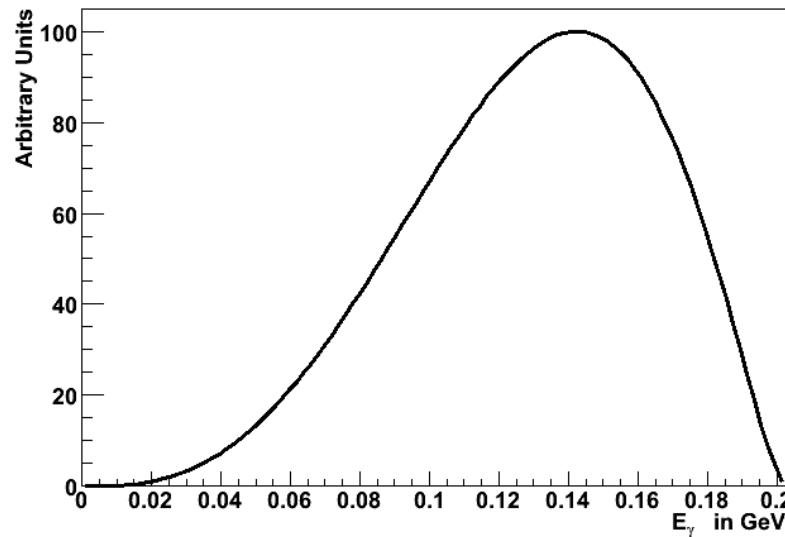
- 4C – Fit (four-momentum conservation, no  $\eta$  mass constraint)
- Cut on Probability  $> 10\%$
- Invariant Mass resolution improved from 80 MeV to 9 MeV (FWHM)



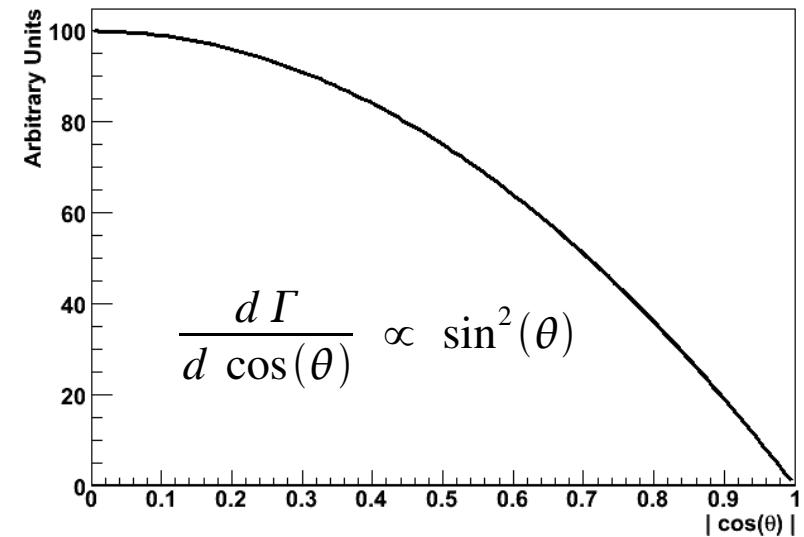


# Parametrization of the Dalitz Plot

$E_\gamma$ : Photon momentum  
in the  $\eta$  - rest frame



$\cos(\theta)$ : Angle between  $\gamma$  and  $\pi^+$   
in the pion-pion rest frame



Here:

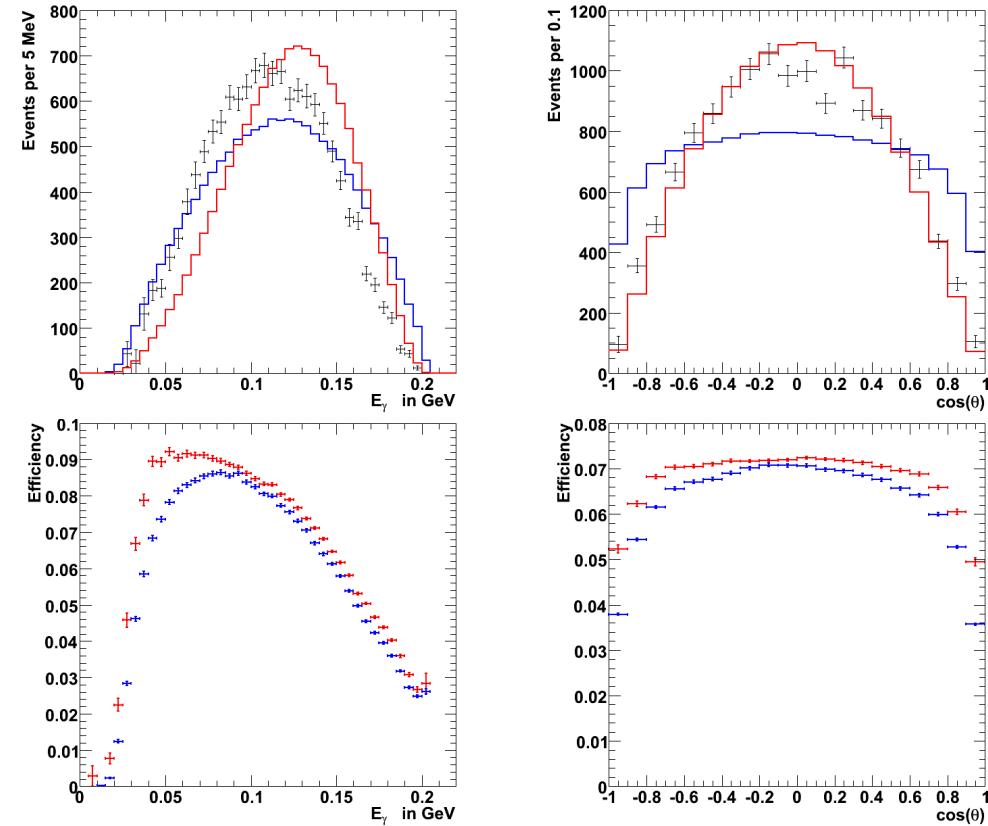
simplest gauge invariant matrix element with p-wave interaction of the pions



# Efficiency

- average efficiency: 7%

- Monte Carlo distributions:
  - phase space
  - simplest matrix element



- corrections based on the simplest gauge invariant matrix element
  - *matches observed angular distribution of the pions*
- regions without acceptance due to cut on splitoffs



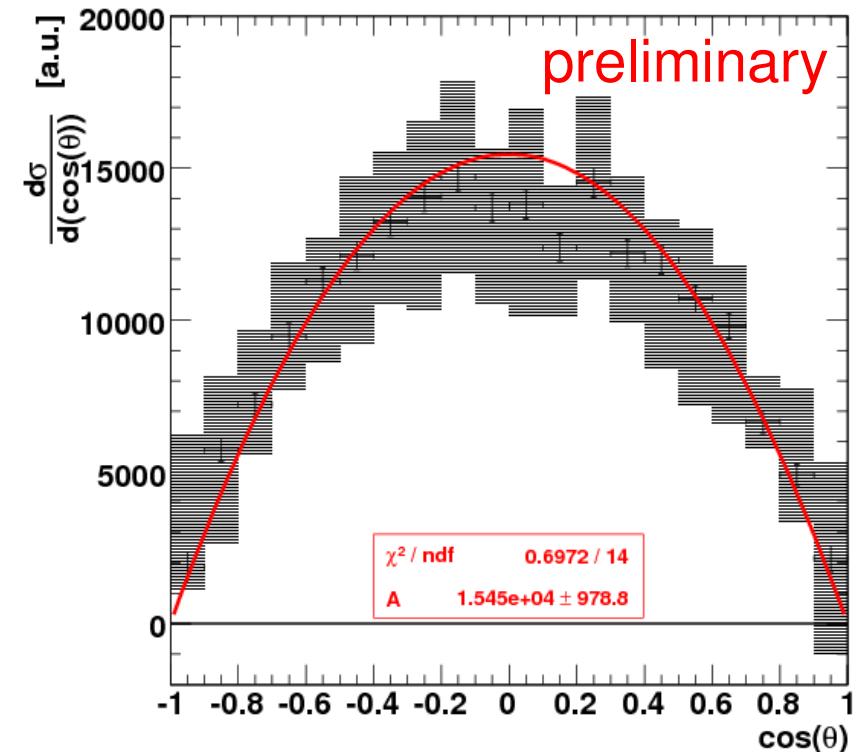
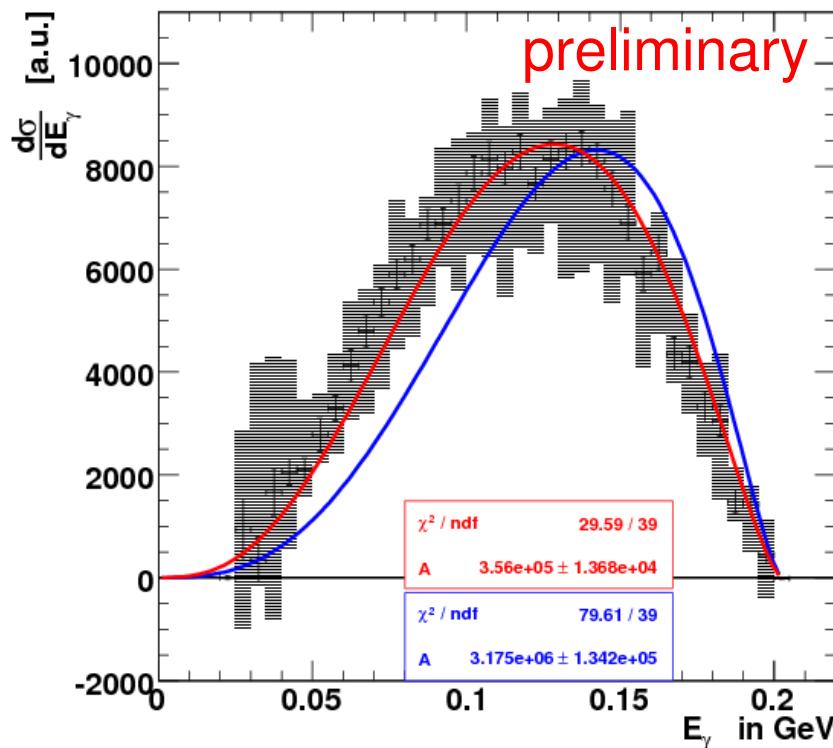
# Systematic Checks

- conditions on energy-momentum conservation prior to kinematic fit
- suppression of hadronic splitoffs
- probability distribution of the kinematic fit
- background subtraction
- efficiency correction
- accelerator mode
- luminosity

→ conditions for background suppression most influential



# Dalitz Plot Distributions



- simplest matrix element does not describe data (blue)
- better agreement with VMD (red)
- p – wave interaction
- higher partial waves negligible