

Recent Results on CP-Violation at the BaBar and Belle B-Factories

by Homer Neal (SLAC)

on

14 June 2010

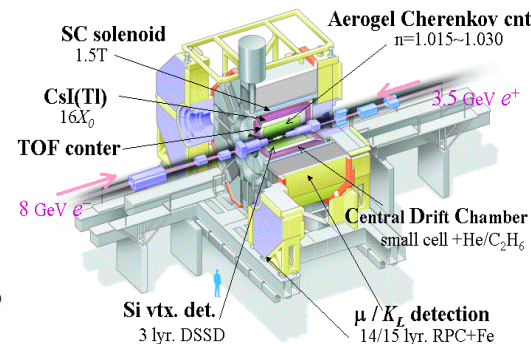
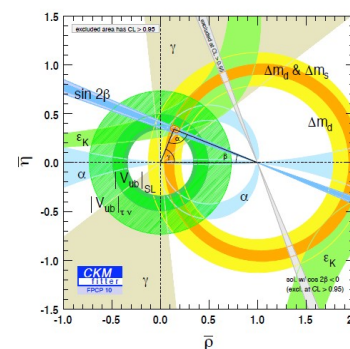
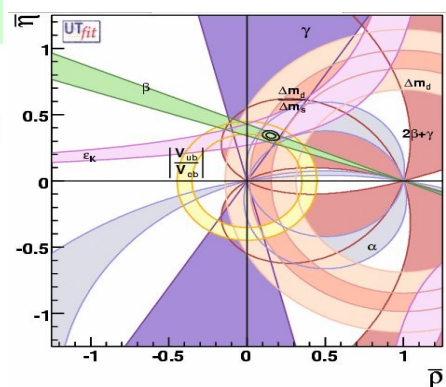
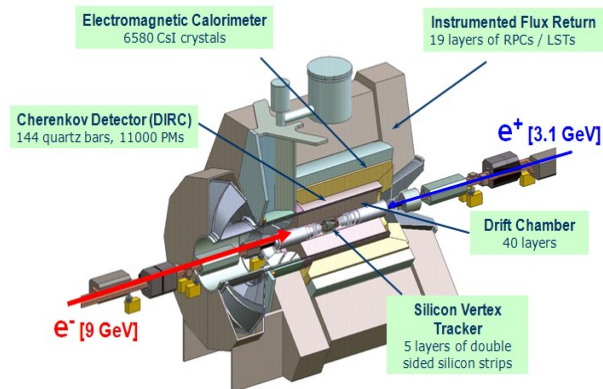
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in KRAKÓW, Poland

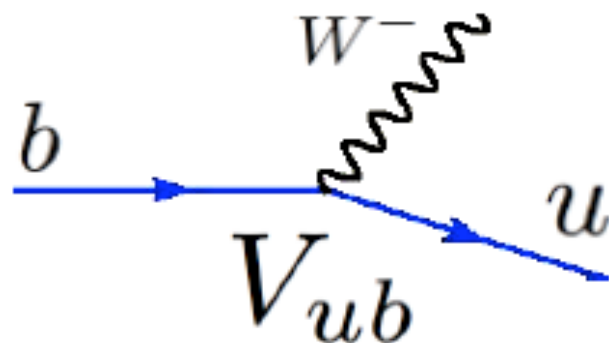


Belle Detector



CP violation and the CKM matrix

quark decay

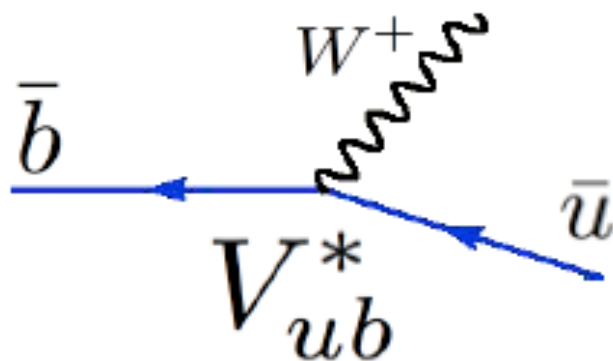


Cabibbo Kobayashi Maskawa matrix

(Wolfenstein parametrization)

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

anti-quark decay



Relative magnitudes

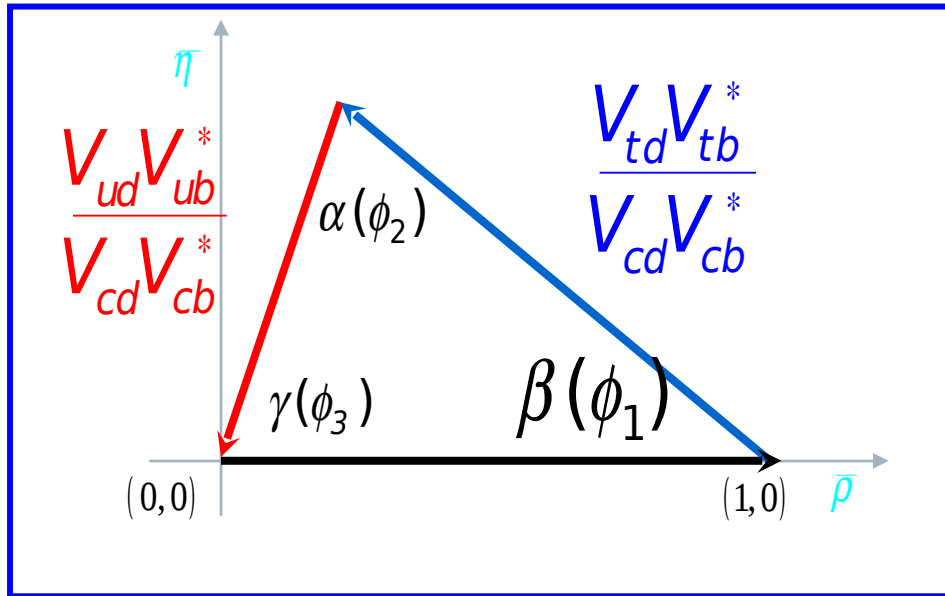
$$\begin{matrix} & d & s & b \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} \end{matrix}$$

The CP-violating phases

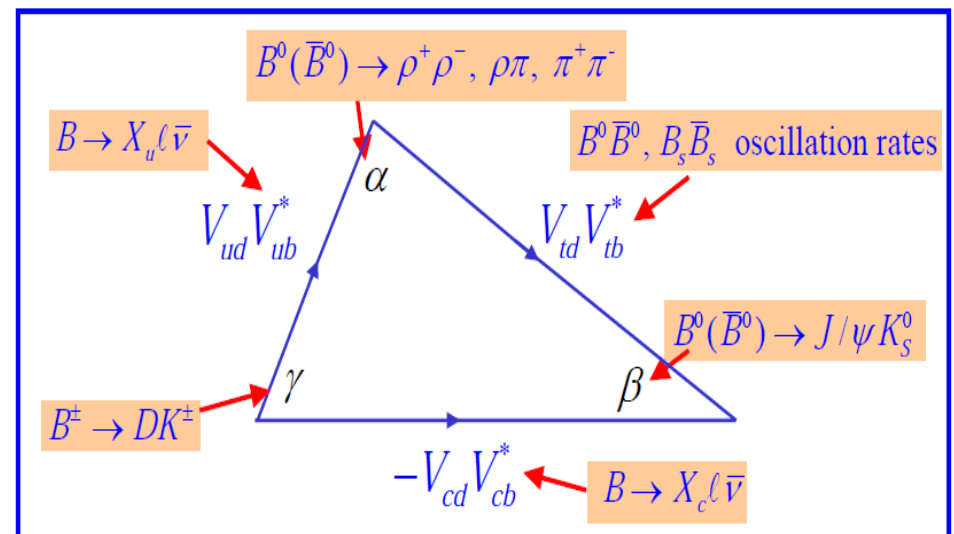
$$\begin{matrix} & d & s & b \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} 1 & 1 & e^{-i\gamma} \\ 1 & 1 & 1 \\ e^{-i\beta} & 1 & 1 \end{pmatrix} \end{matrix}$$

Non-trivial CP violating phases. Amplitude interference different for quark vs anti-quark decay. Observable rate differences.

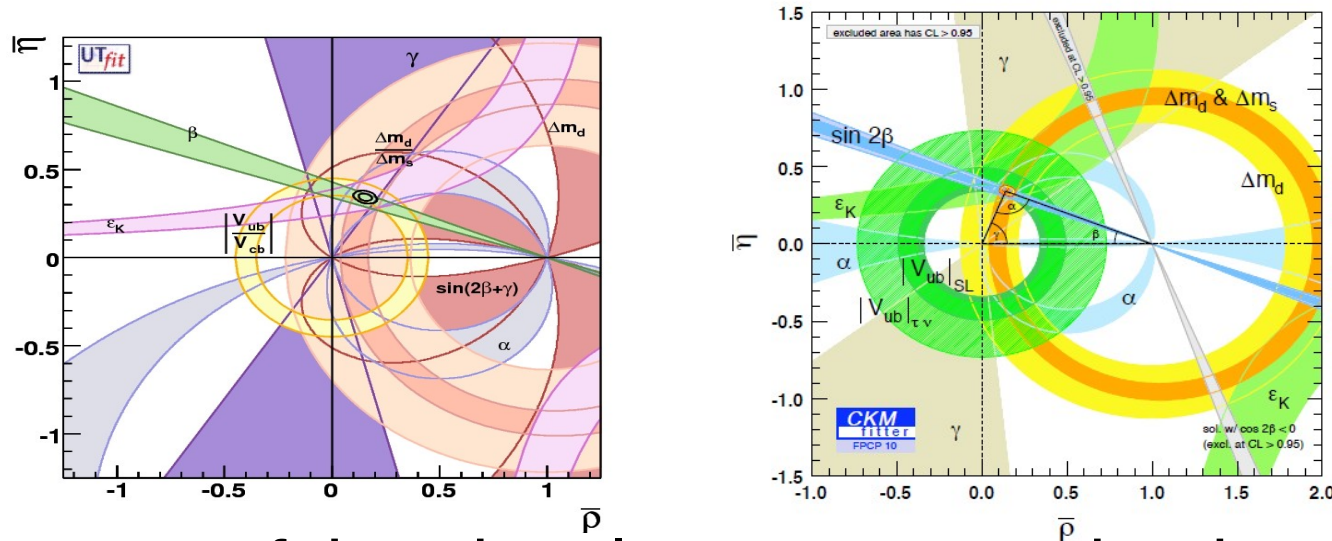
The Unitarity Triangle



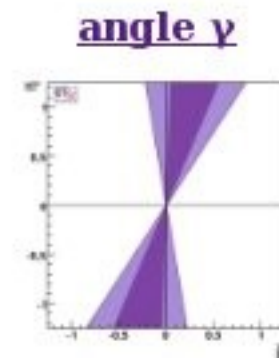
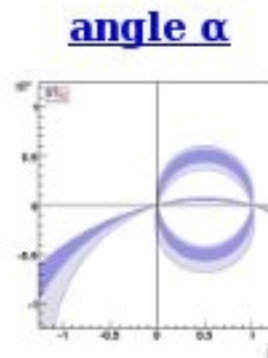
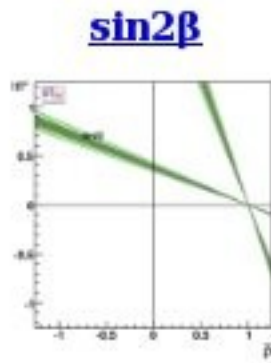
SM prediction: ALL measurements of W -mediated quark processes must be consistent with the CKM framework.



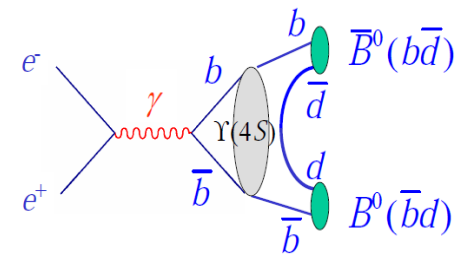
Overall Status of the triangle



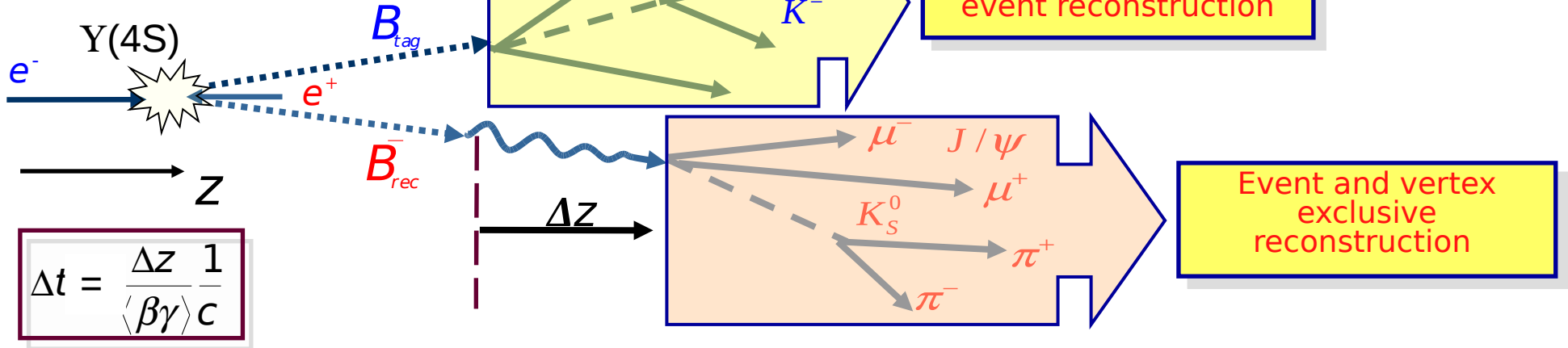
- Apex of the triangle over constrained
- More work needed on γ/ϕ_3
- γ constrained from $B^\pm \rightarrow D^{(*)} K^{(*)\pm}$



The experimental method



$$\beta\gamma_{Y(4S)} = \frac{0.425}{0.56}$$



• fighting main background ($e^+e^- \rightarrow q\bar{q}$)

- most important discriminating quantities:

$$m_{es} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$

$$\Delta E = E_B^* - E_{beam}^*$$

- topological cuts (Fisher discr. or neural net)

All B decays are CKM suppressed, with $b \rightarrow c$ decays dominant

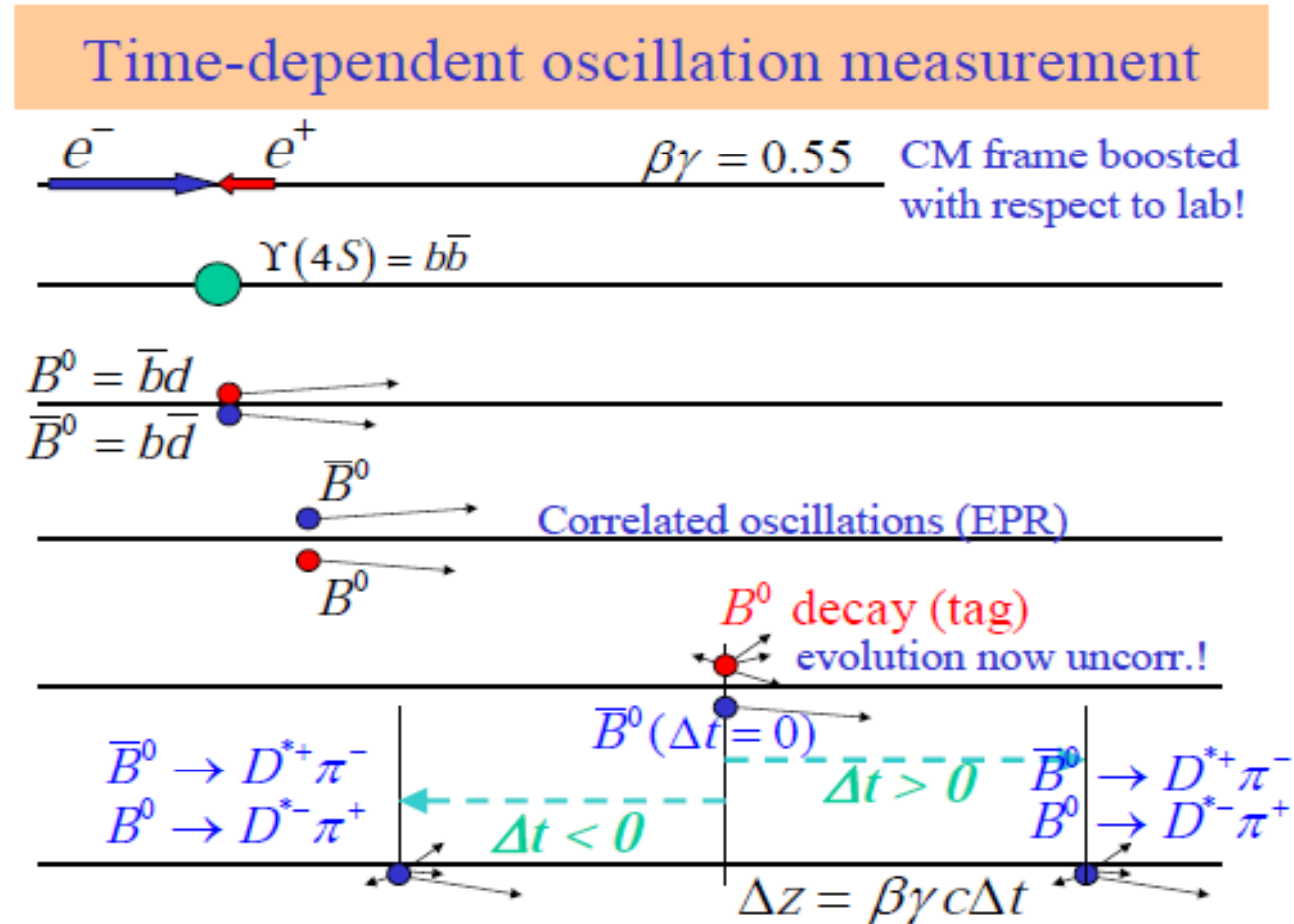
$$\Gamma \propto G_F^2 |V_{cb}|^2 m_b^5 \quad |V_{cb}| \approx 0.04 \quad |V_{cb}|^2 \approx 1.6 \times 10^{-3}$$

$$c\tau_B = (3 \times 10^8 \text{ ms}^{-1})(1.6 \times 10^{-12} \text{ s}) = 0.48 \text{ mm}$$

How far will B mesons travel before decaying?

$$\left. \begin{aligned} \Delta \ell_{\text{lab}} &= v \cdot \Delta t_{\text{lab}} = \beta c \cdot \Delta t_{\text{lab}} \\ \Delta t_{\text{lab}} &= \gamma \cdot \Delta t_{\text{B rest}} \\ \Rightarrow \Delta \ell_{\text{lab}} &= \beta \gamma \cdot c \Delta t_{\text{B rest}} \end{aligned} \right\} \begin{aligned} &\text{average over decays} \\ &\langle \Delta \ell_{\text{lab}} \rangle = \beta \gamma \cdot c \langle \Delta t_{\text{B rest}} \rangle \\ &= \beta \gamma \cdot c \tau_B \end{aligned}$$

$B^0\bar{B}^0$ correlated until one decays



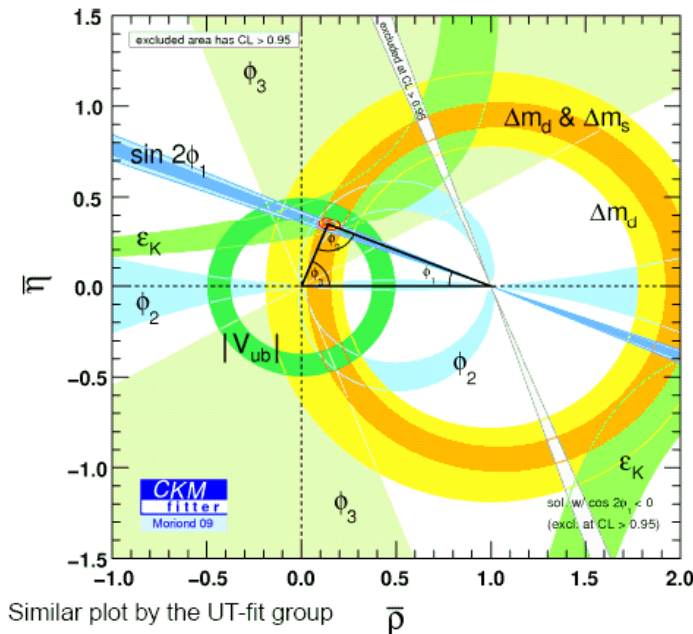
From Jeff Richman's Mexico Physics School Lectures (2008)

<http://hep.ucsb.edu/people/richman/richman.html>

The reward

Makoto Kobayashi and Toshihide Maskawa awarded 2008 Nobel Prize in Physics for their theory which simultaneously *explained the source of matter/antimatter asymmetries in particle interactions and predicted the existence of the third generation of fundamental particles.*

The **BaBar** experiment at the SLAC National Accelerator Laboratory in the U.S., together with the **Belle** experiment at KEK in Japan, recently provided experimental confirmation of the theory, some thirty years after it was published, *through precision measurements of matter/antimatter asymmetries.*



The Nobel Prize in Physics 2008



and the B FACTORIES **SLAC**



The Nobel Prize in Physics 2008 was awarded to

Makoto Kobayashi
High Energy Accelerator Research Organization (KEK),
Tsukuba, Japan



Toshihide Maskawa
Kyoto Sangyo University, Theoretical Physics (TTP)
Kyoto University, Kyoto, Japan

and to Makoto Hagiwara, Chuan-Tsun Tsun, and University of Chicago, U.S.A.
for the discovery of the mechanism of quark mixing and CP violation in subatomic physics

"for the discovery of the origin of the broken symmetry which predicts the existence of at least three families of quarks in nature"



Broken Symmetries Predicted Extra Quarks

Matter and antimatter are nearly exact opposites of each other. But this near-perfect symmetry is broken in nature as we observe it. In 1972, Kobayashi and Maskawa discovered that the root of the mystery could be explained by the properties of quarks, the fundamental constituents of protons and neutrons, but only if there were three more types of quarks than had previously been observed. At that time, experimenters had seen the up, down, and strange quarks, but the charm, bottom, and top would not be discovered until later.

BaBar

PEP-II



B Factory Experiments Confirmed the Predictions

Experiments of the B factories in the United States and Japan in the early 2000s made detailed investigations of billions of high-energy particles containing bottom quarks. International Collaborations of the B factories made numerous measurements of the parameters of the Cabibbo, Kobayashi, and Maskawa (CKM) mixing matrix and confirmed the precise links of these with the observed differences between matter and antimatter. The B factories each consist of an accelerator and a particle detector. At the SLAC National Accelerator Laboratory in California, USA, the PEP-II accelerator provides the collisions observed by the BaBar detector. At KEK in Tsukuba, Japan, the KEK-B accelerator supplies the Belle detector with the particles needed for these studies.

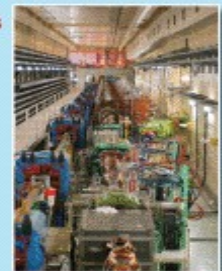
Belle



"Please accept our deepest respect and gratitude for the B factory achievements. In particular, the high-precision measurement of CP violation and the determination of the mixing parameters are great accomplishments, without which we would not have been able to earn the Prize."

小林 誠 (Makoto Kobayashi)
益川 敏英 (Toshihide Maskawa)

KEK-B



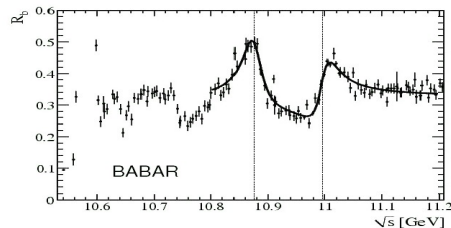


The BaBar experiment

Multipurpose particle detector at SLAC
used to observe collisions of e^+e^- PEP-II
beams of asymmetric energies
primarily at the Υ (4S) mass peak
(10.58 GeV)

Recorded Data Samples:

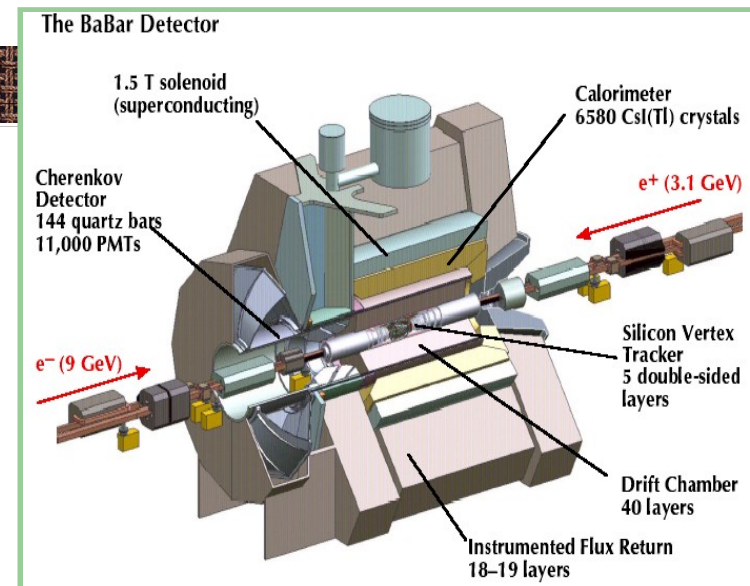
**$\Upsilon(4S)$: 432 fb^{-1}
(+ 10% off-peak data)**



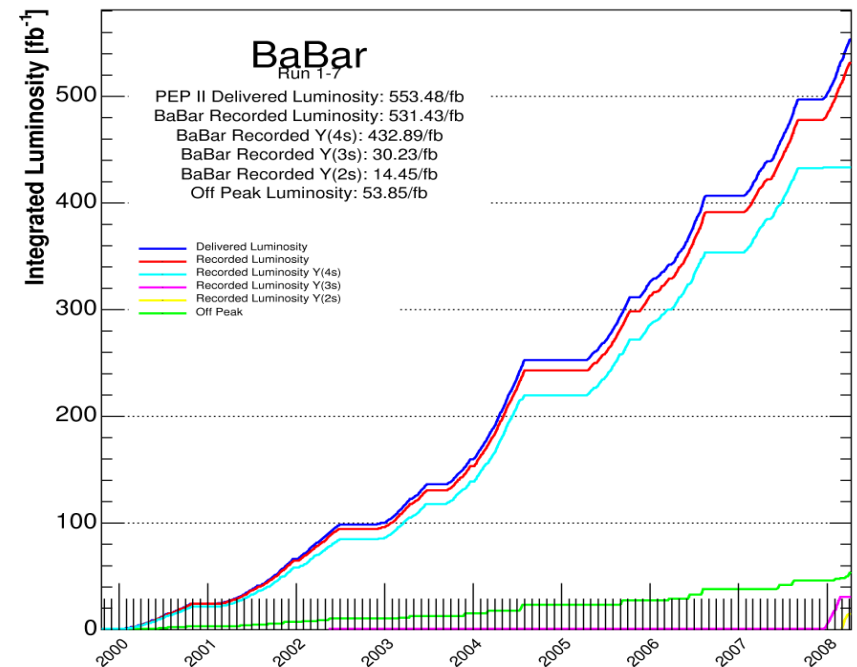
**$\Upsilon(3S)$: 30 fb^{-1}
 $\Upsilon(2S)$: 15 fb^{-1}**

**22 billion events (~9 billion after
filters applied)**

~470 million $B\bar{B}$ events



As of 2008/04/11 00:00



Belle detector records data delivered by KEKB asymmetric B-factory ($\beta \gamma = 0.425$) running at the $\Upsilon(4S)$ mass peak (10.58 GeV) at KEK.

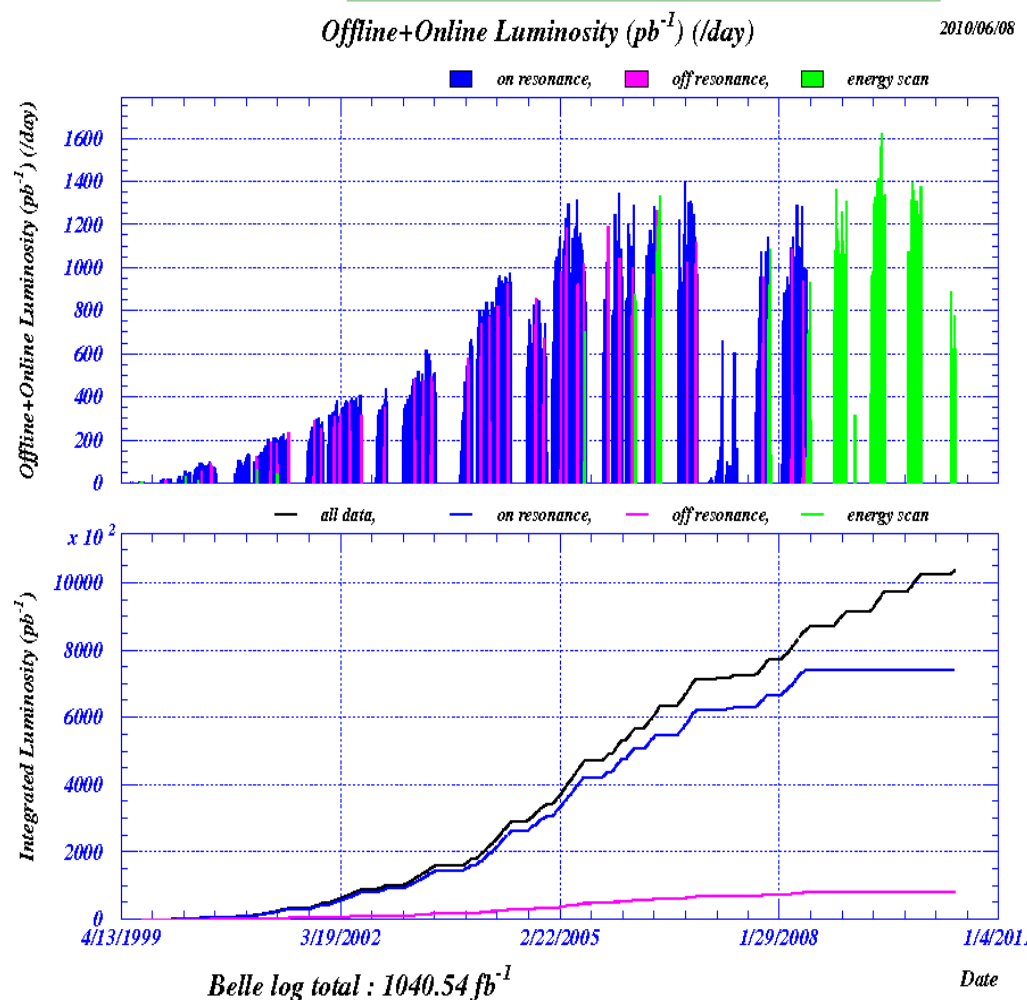
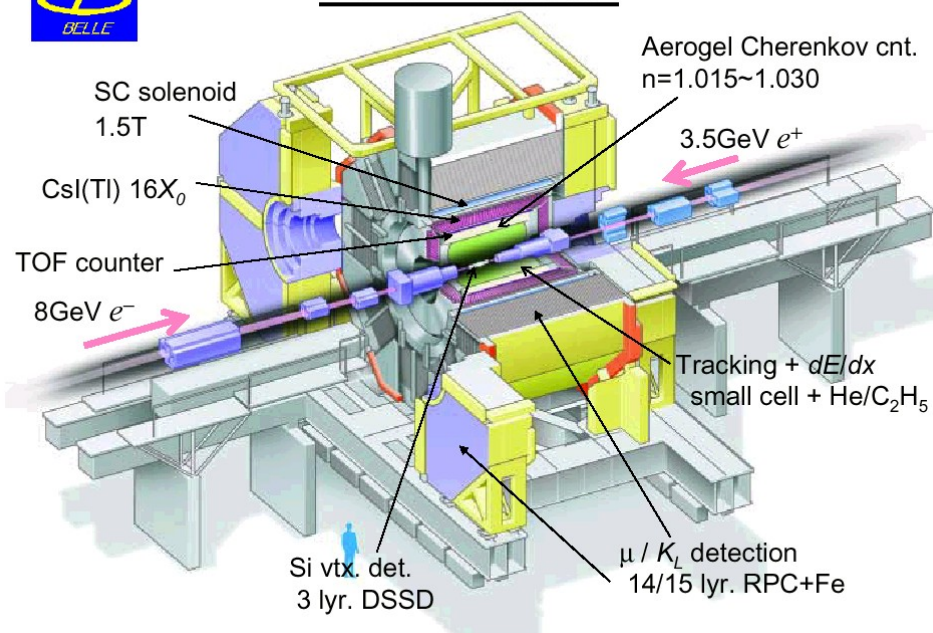


Recorded Data Samples:
 $\Upsilon(5S)$: 121 fb⁻¹
 $\Upsilon(4S)$: 711 fb⁻¹
 $\Upsilon(3S)$: 3 fb⁻¹
 $\Upsilon(2S)$: 24 fb⁻¹
 $\Upsilon(1S)$: 5.7 fb⁻¹

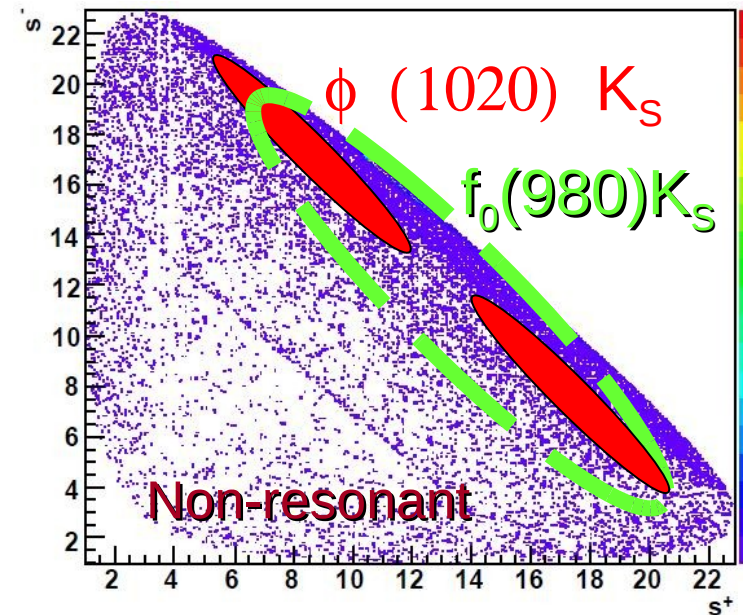
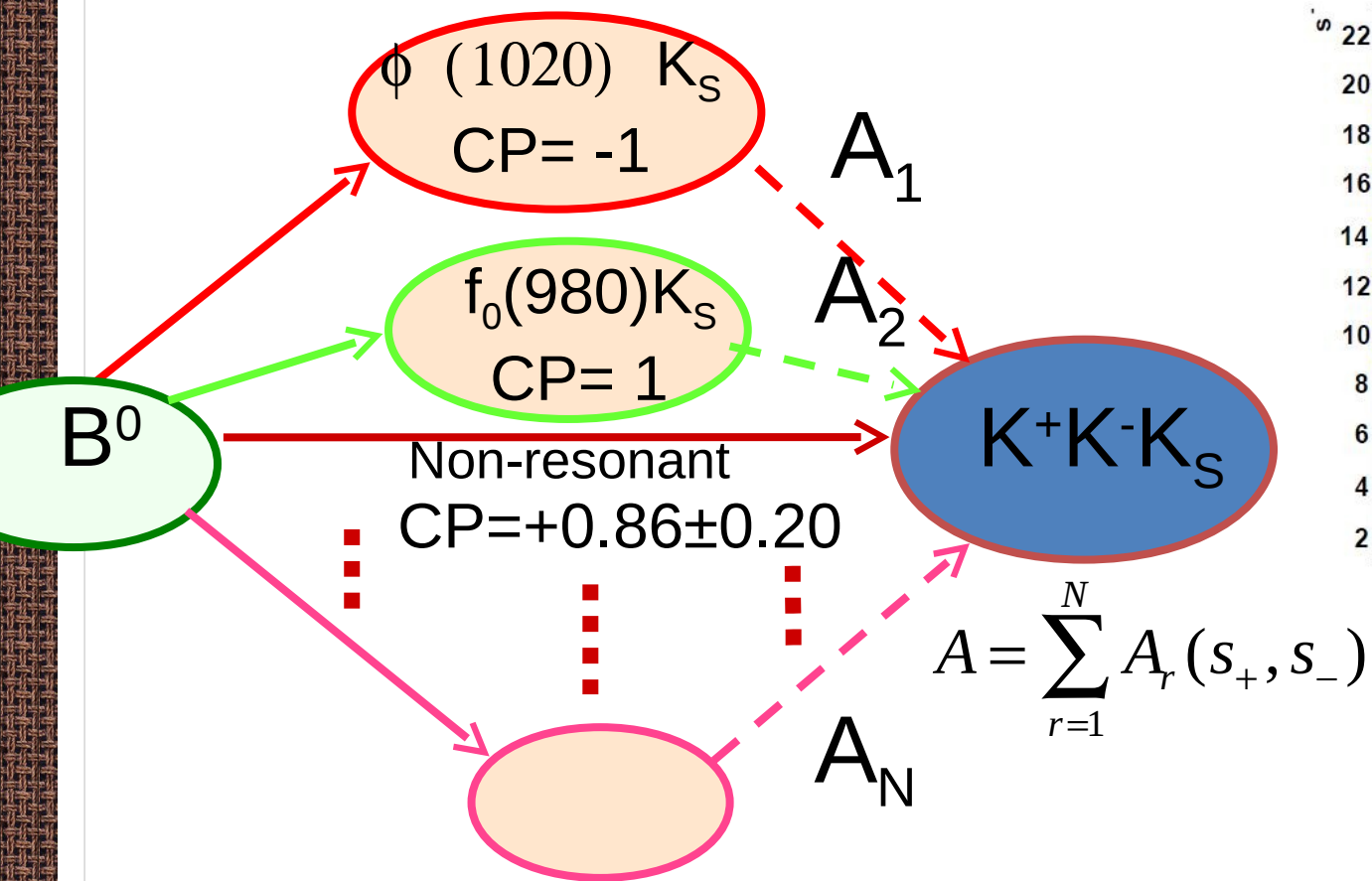
~770 million BB events



Belle Detector



CPV Measurements in the $B \rightarrow K^- K^+ K_S^0$ Dalitz Plot

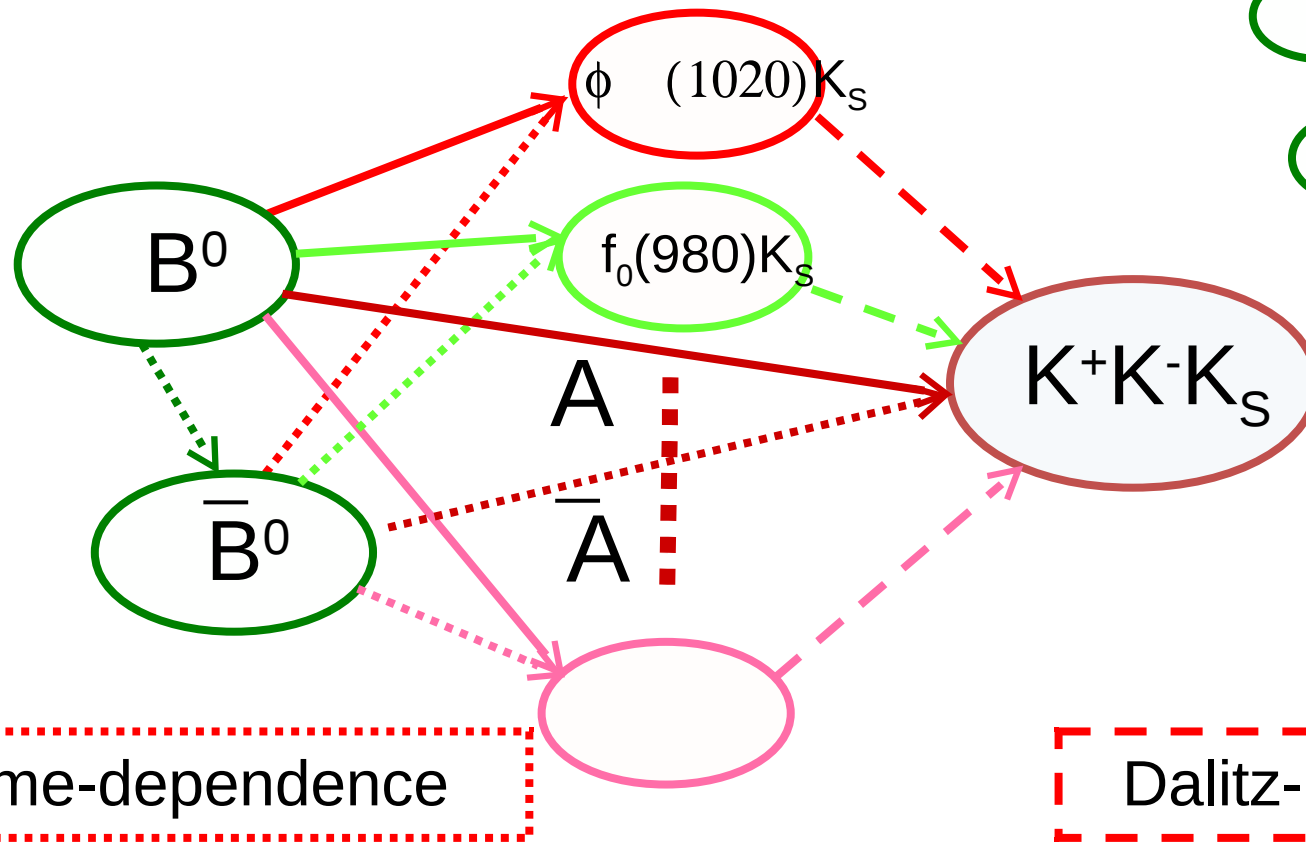
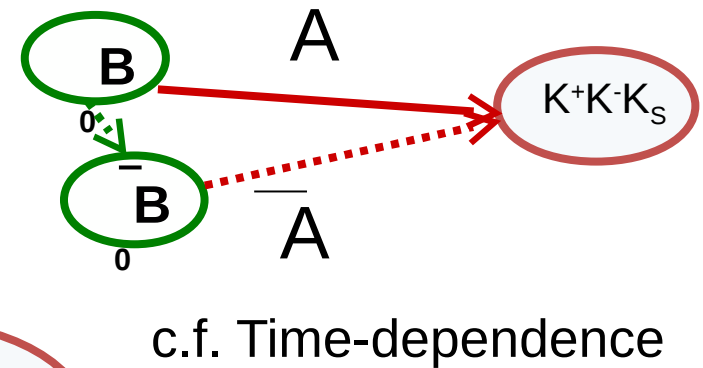


$$s_+ = M^2(K^+ K_S)$$

$$s_- = M^2(K^- K_S)$$

Diagrams thanks to K. Sumisawa (KEK)
(FPCP 2010 talk)

Time-dependence of Dalitz plot in $B^0 \rightarrow K^+ K^- K_S$



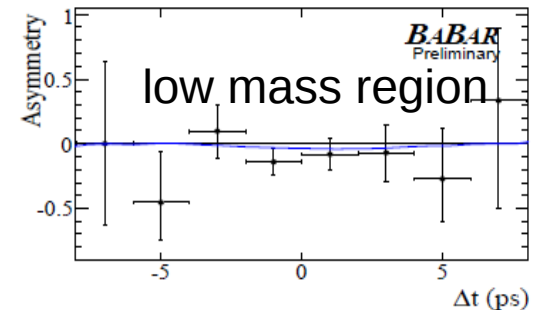
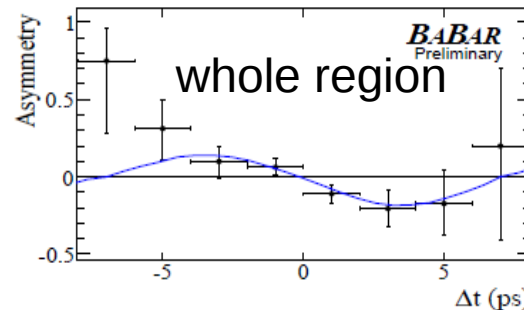
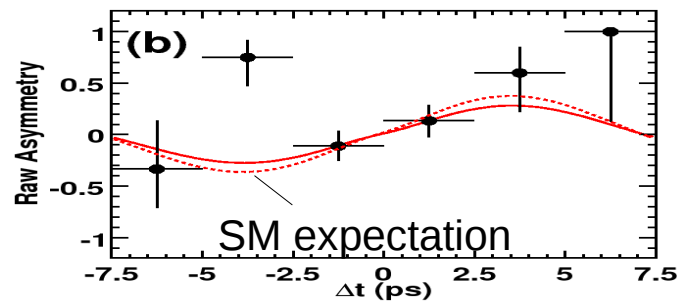
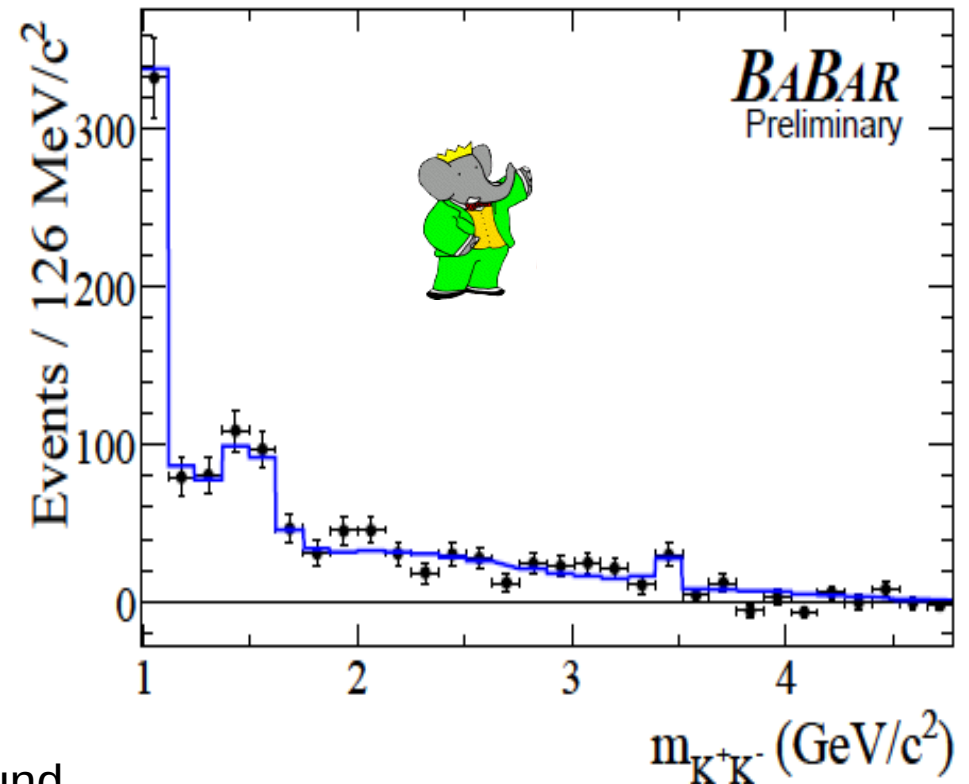
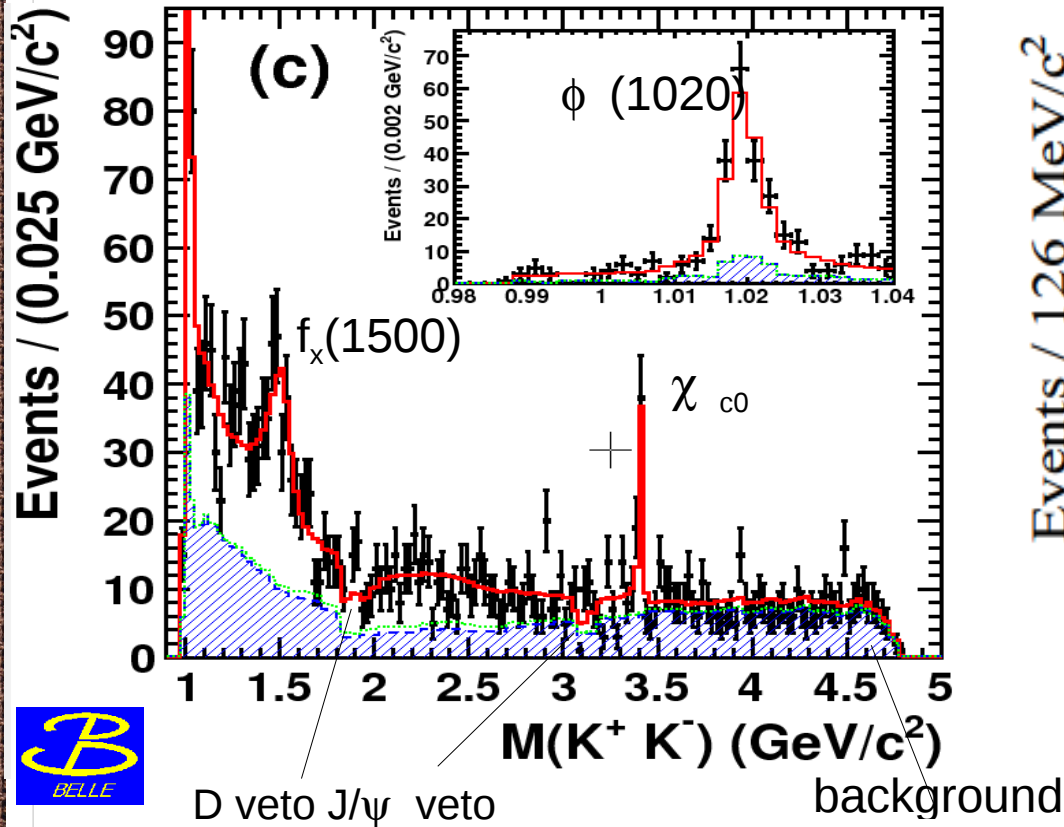
Interference in $B^0 \bar{B}^0 (\phi_{1,\text{eff}}) + \text{intermediate states (Dalitz phase)}$

CP asymmetry ($\phi_{1,\text{eff}}, A_{\text{CP}}$) of $B \rightarrow \phi(1020) K_S$
using Time-dependent Dalitz plot analysis in $B \rightarrow K^+ K^- K_S$

Dalitz plot fit results

Belle 657MBB to be submitted to PRD.

BABAR 465MBB arXiv:0808.0700



NOTE: Only the 1st of the four solutions is shown above.

Results from BaBar and Belle on Direct CPV using Dalitz plot analyses



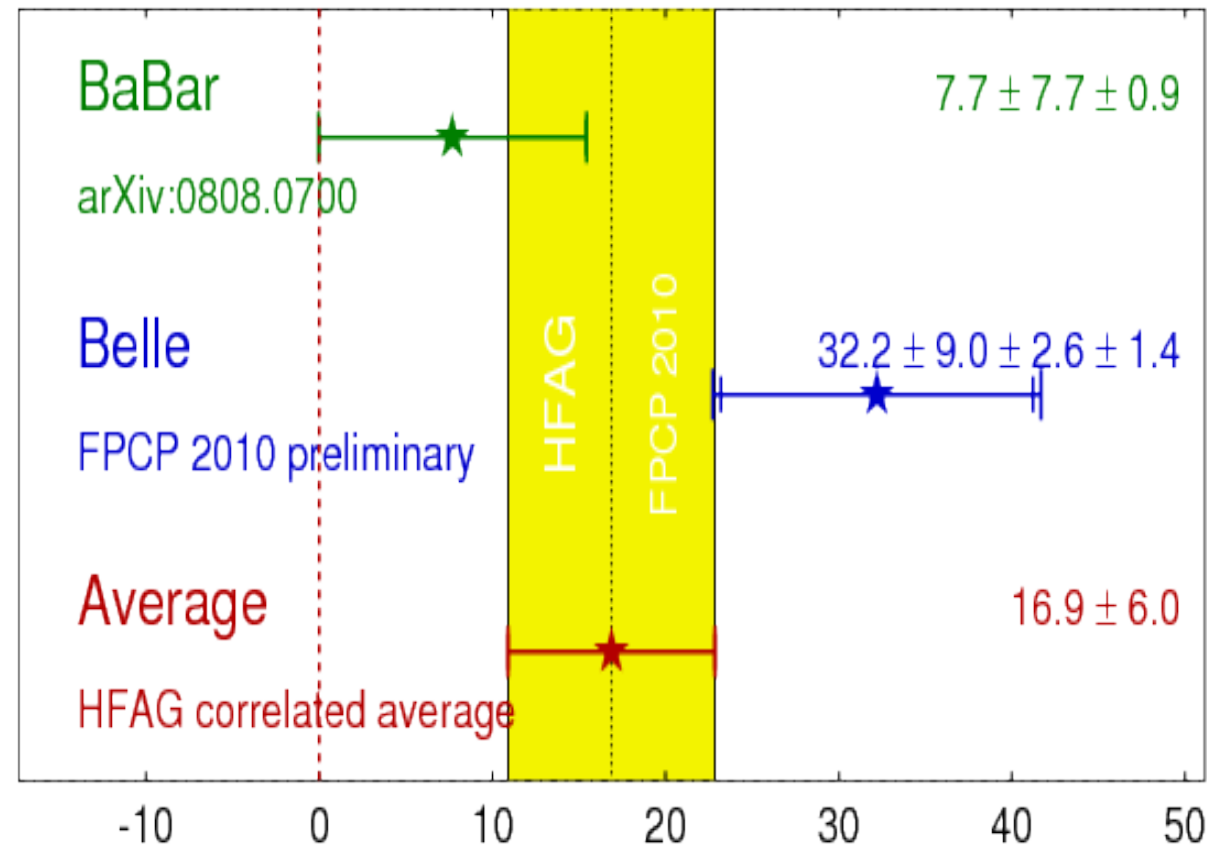
$K^+ K^- K_S \beta(\phi K_S)$

HFAG
FPCP 2010
PRELIMINARY

	Solution 1
$A_{CP}(f_0 K_S^0)$	$-0.30 \pm 0.29 \pm 0.11 \pm 0.09$
$\phi_1^{\text{eff}}(f_0 K_S^0)$	$(31.3 \pm 9.0 \pm 3.4 \pm 4.0)^\circ$
$A_{CP}(\phi K_S^0)$	$+0.04 \pm 0.20 \pm 0.10 \pm 0.02$
$\phi_1^{\text{eff}}(\phi K_S^0)$	$(32.2 \pm 9.0 \pm 2.6 \pm 1.4)^\circ$



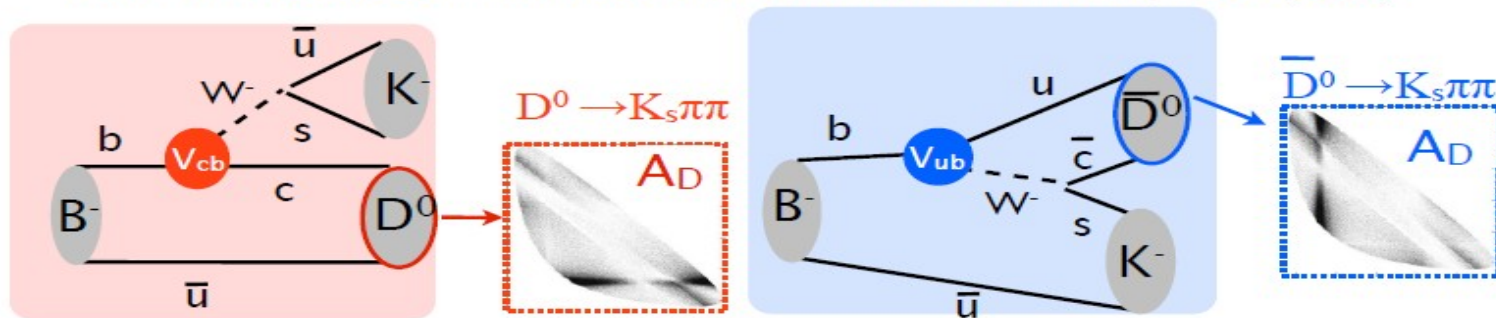
Name	Solution (1)
1 $A_{CP}(\phi K_S^0)$	$0.14 \pm 0.19 \pm 0.02$
2 $\beta_{\text{eff}}(\phi K_S^0)$	$(7.7 \pm 7.7 \pm 0.9)^\circ$
3 $A_{CP}(f_0 K_S^0)$	$0.01 \pm 0.26 \pm 0.07$
4 $\beta_{\text{eff}}(f_0 K_S^0)$	$(8.5 \pm 7.5 \pm 1.8)^\circ$



Measuring γ

- From interference of the decay amplitudes

γ in the interference term between transitions $b \rightarrow c\bar{u}s$ and $b \rightarrow u\bar{c}s$ when we reconstruct a final state accessible to both: $K_s\pi\pi$, K_sKK (GGSZ)



- Use final state accessible from both D^0 and $\bar{D}^0$
 - Methods:
 - * Gronau, London, Wyler Method,
 - * Atwood, Dunietz, Soni Method (incl. DCS decays of the D meson)
 - * Dalitz plot

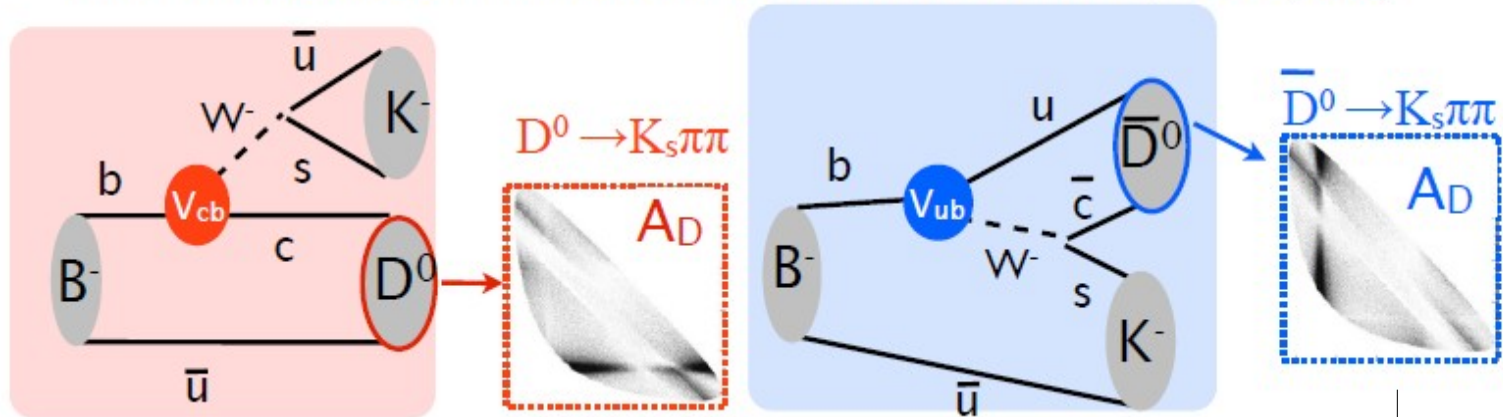
$$r_b = \left| \frac{A(b \rightarrow u)}{A(b \rightarrow c)} \right|$$

Strong (CP conserving)
phase difference δ
between $A(b \rightarrow u)$ and $A(b \rightarrow c)$

- Common hadronic parameters

CP violation in the measurement of the CKM angle γ with $B^\pm \rightarrow D^* K^{*\pm}$ decays

γ in the interference term between transitions $b \rightarrow c\bar{u}s$ and $b \rightarrow u\bar{c}s$
when we reconstruct a final state accessible to both: $K_s\pi\pi$, K_sKK (*GGSZ*)



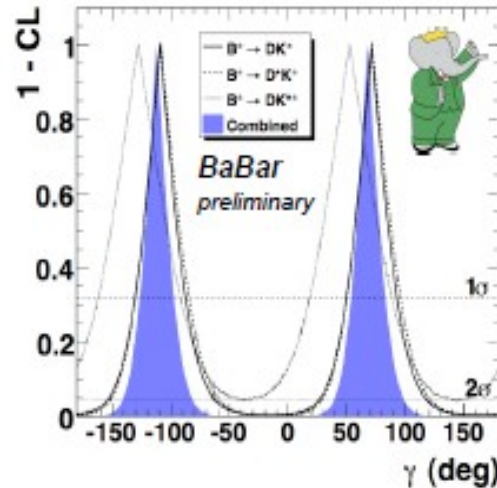
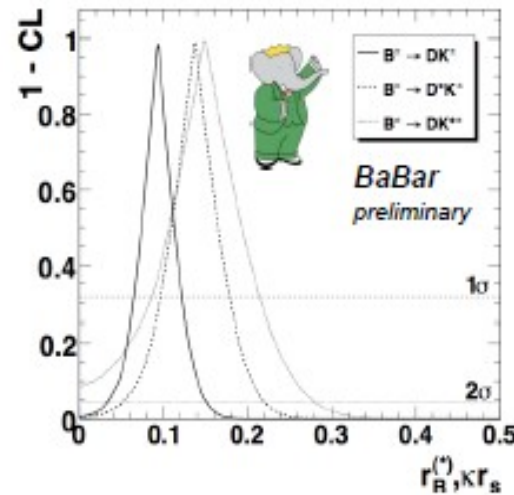
$$A(B^-) = \underline{\hspace{2cm}}$$

$$+ r_b e^{-i\gamma + i\delta_b}$$

Determined
from data

«... the full sub-resonance structure of the three-body decay is considered, involving also Cabibbo allowed decays. » - utfit.org

CP violation in the measurement of the CKM angle γ with $B^\pm \rightarrow D^* K^{*\pm}$ decays



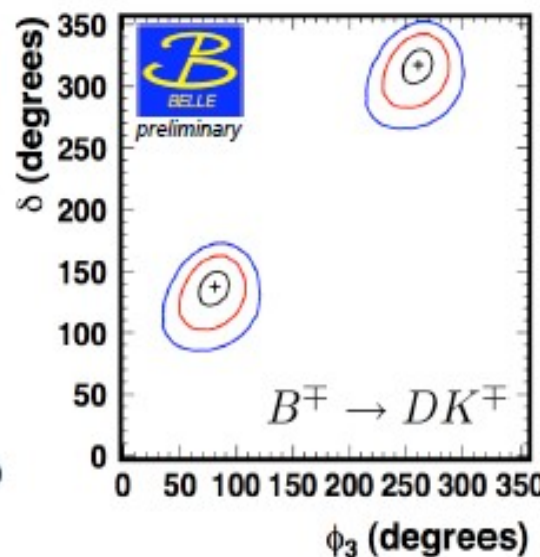
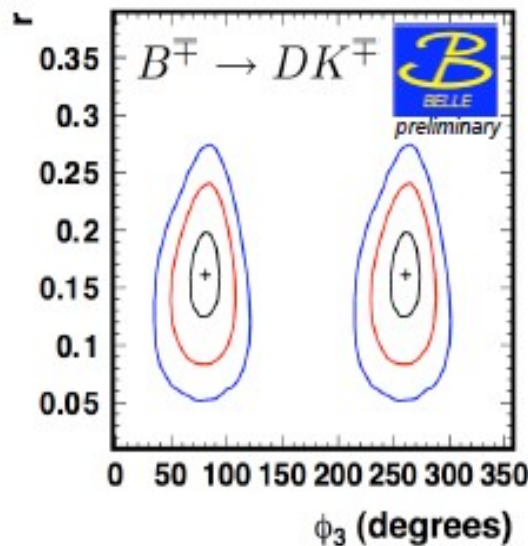
BaBar preliminary

$\gamma = (68 \pm 14 \pm 4 \pm 3)^\circ$
(value $\pm$ stat. $\pm$ sys. $\pm$ model) $^\circ$

Excludes $\gamma = 0$ at 3.5 std.dev.

$r_B(DK) = (9.4^{+2.8}_{-2.9})\%$
(value $\pm$ total error)%

Error breakdown (± 0.5 expt., ± 0.4 model)%



BELLE preliminary

$\gamma = (78.4^{+10.8}_{-11.6} \pm 3.6 \pm 8.9)^\circ$
(value $\pm$ stat. $\pm$ sys. $\pm$ model) $^\circ$

$B \rightarrow DK$ and $B \rightarrow D^*K$ only, 657 MB $\bar{B}$

Excludes $\gamma = 0$ at 3.5 std.dev.

$r_B(DK) = (16.0^{+4.0}_{-3.8} \pm 0.011^{+5.0}_{-1.0})\%$
(value $\pm$ stat. $\pm$ sys. $\pm$ model)%

Measurement of the CKM angle γ using a GLW analysis of $B^\pm \rightarrow D(\text{CP}) K^\pm$ decays at BaBar

- The Gronau, London, Wyler (GLW) method:

Gronau & London, PLB 253, 483 (1991)

Gronau & Wyler, PLB 265, 172 (1991)

$$R_{CP\pm} = 1 + r^2 \pm 2r \cos \delta \cos \gamma$$

$$A_{CP\pm} = \pm 2r \sin \delta \sin \gamma / R_{CP\pm}$$

—

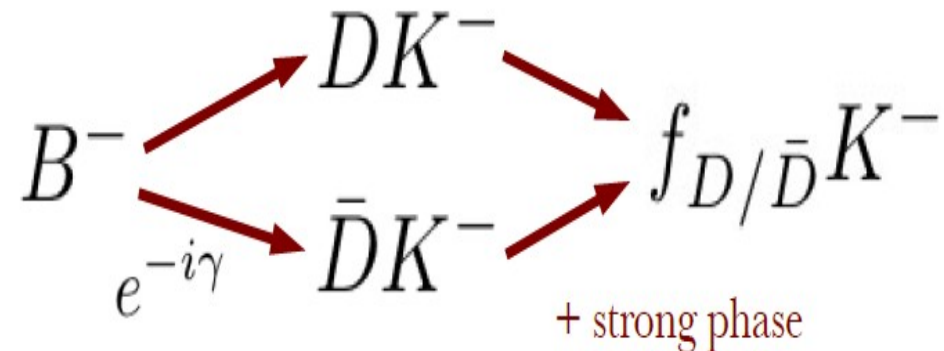
Make use of a larger control sample:

$$R_{CP\pm} \approx \frac{R_{K/\pi}^\pm}{R_{K/\pi}^{\text{flv}}}$$

Many systematics cancel in the double ratio.

$$R_{K/\pi}^\pm \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm}^0 K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm}^0 \pi^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm}^0 \pi^+)}$$

$$\begin{array}{l} B^+ \rightarrow \overline{D}^0 K^+ \\ B^+ \rightarrow \overline{D}^0 \pi^+ \end{array}$$



Measurement of the CKM angle γ using a GLW analysis of $B^\pm \rightarrow D(\text{CP}) K^\pm$ decays at BaBar

- Reconstruct $B^\pm \rightarrow D K^\pm$
 - D meson is reconstructed in CP-eigenstates and
 - Non-CP final states

$\overline{D}^0 \rightarrow$	CP+	CP-	non-CP
	$\pi^+ \pi^-$	$K_S \pi^0$	$K^+ \pi^-$
	$K^+ K^-$	$K_S \omega$	
		$K_S \Phi$	

Preliminary Results:

(submitted to PRD)

$$A_{CP+} = 0.25 \pm 0.06(\text{stat}) \pm 0.03(\text{syst})$$

$$A_{CP-} = -0.09 \pm 0.07(\text{stat}) \pm 0.02(\text{syst})$$

$$R_{CP+} = 1.18 \pm 0.09(\text{stat}) \pm 0.06(\text{syst})$$

$$R_{CP-} = 1.07 \pm 0.08(\text{stat}) \pm 0.05(\text{syst})$$

Improves over old result with:

- 20% more data; 467 million $B\overline{B}$ decays
- Improved fit strategy
- Now constrains γ

Measurement of the CKM angle γ using a GLW analysis of $B^\pm \rightarrow D(\text{CP}) K^\pm$ decays at BaBar

Preliminary Results:

(submitted to PRD)

At the 68% CL :

γ belongs to one of the three intervals

$[11.3^\circ, 22.7^\circ],$

$[80.9^\circ, 99.1^\circ]$

or

$[157.3^\circ, 168.7^\circ]$

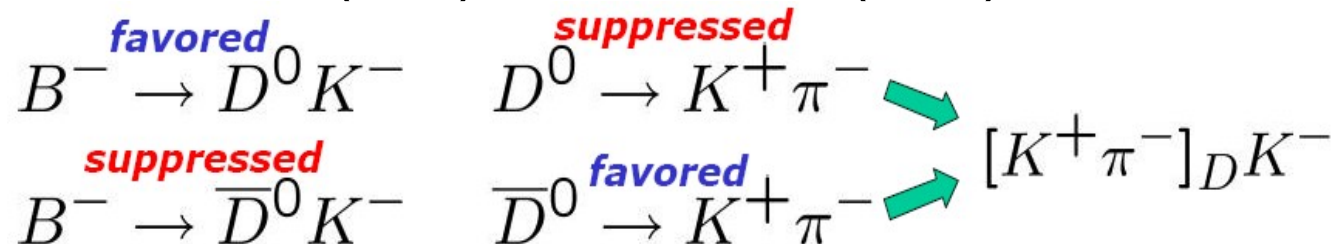
and

$$0.24 < r_B < 0.45$$

BaBar ADS analysis: $b \rightarrow u$ transitions in $B^- \rightarrow D^0 K^-$ and $B^- \rightarrow D^{*0} K^-$ decays

In the ADS technique the amplitudes are equalized

- Atwood, Dunietz, Soni (ADS), PRL 78, 3257 (1997) & PRD 63, 036005 (2001)



Small BF($\sim 10^{-7}$), but $A_2 = O(A_1)$: expect large CPV

$$R_{ADS} = \frac{BF([K^+ \pi^-] K^-) + BF([K^- \pi^+] K^+)}{BF([K^- \pi^+] K^-) + BF([K^+ \pi^-] K^+)} = r_D^2 + r_B^2 + 2r_B r_D \cos(\delta_D + \delta_B) \cos \gamma$$

Very sensitive to r_b

- Amount of interference depends on CKM angle γ/ϕ_3

$$A_{ADS} = \frac{BF([K^+ \pi^-] K^-) - BF([K^- \pi^+] K^+)}{BF([K^+ \pi^-] K^-) + BF([K^- \pi^+] K^+)} = 2r_B r_D \sin(\delta_D + \delta_B) \sin \gamma / R_{ADS}$$

CP asymmetry can be very large

BaBar ADS analysis: $b \rightarrow u$ transitions in $B^- \rightarrow D^0 K^-$ and $B^- \rightarrow D^{*0} K^-$ decays

- Clear evidence for $B \rightarrow D^{(*)} \pi$ DCSD
- Indication of a $D^0 K$ ADS signal at the 2.1σ level and $D^{*0} K$ at the 2.2σ level ($D^0 \pi^0$)

BaBar Preliminary Results:

$$\mathcal{R}_{DK} = (1.1 \pm 0.5 \pm 0.2) \times 10^{-2}. \quad \mathcal{R}_{DK, D^0 \pi^0}^* = (1.8 \pm 0.9 \pm 0.4) \times 10^{-2}.$$
$$= r_B^2 + r_D^2 + 2 r_B r_D \cos \gamma \cos \delta$$

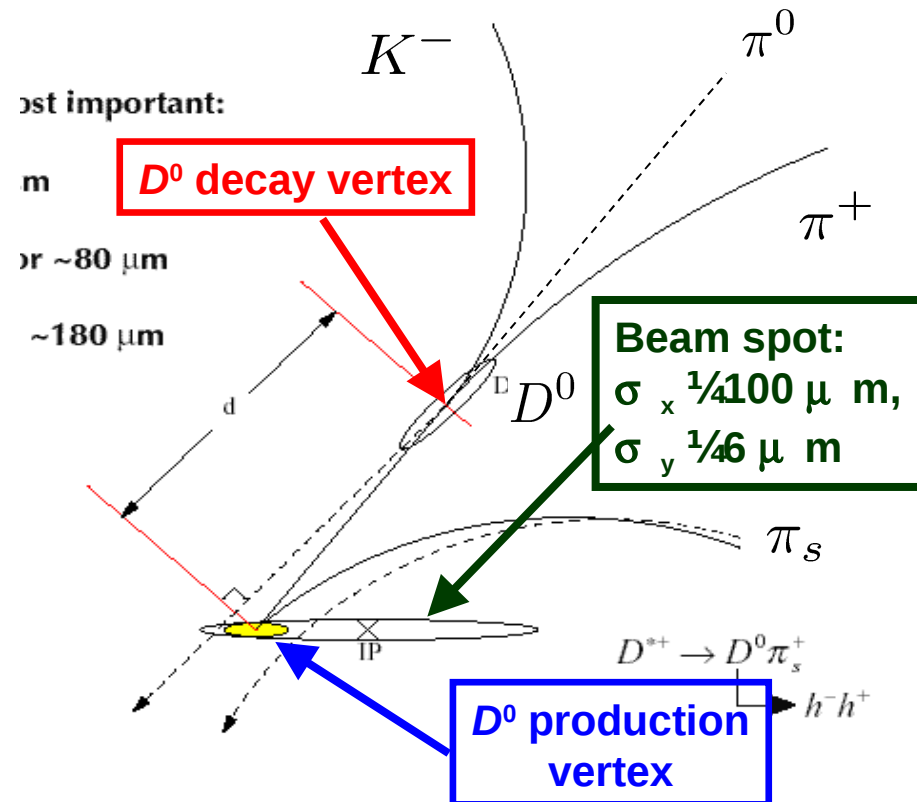
BaBar Preliminary Results:

$$\mathcal{A}_{DK} = -0.86 \pm 0.47 \begin{smallmatrix} +0.11 \\ -0.15 \end{smallmatrix}. \quad \mathcal{A}_{DK, D^0 \pi^0}^* = +0.77 \pm 0.35 \pm 0.12.$$
$$= 2 r_B r_D \sin \gamma \sin \delta / \mathcal{R}_{DK}$$

CP Violation in D decays at the B-factories

1.3 million charm events per /fb at Y(4S)

(Y(4S): cc cross section = 1/4 observed total)



Charm meson Tagging and Selection

- **Tagging at production:**

- Inclusive D^* production. Using $D^{*\pm} \rightarrow D^0 \pi_s^\pm$ decays.
- The flavor of the D^0 is determined by the charge of the π_s .

- **Tagging at decay:**

- The flavor can be determined by the wrong sign (WS) or right sign (RS) D^0 decay products.

$$D^0 \rightarrow K^- \pi^+ \pi^0 \quad \text{right-sign (RS)}$$

$$D^0 \rightarrow K^+ \pi^- \pi^0 \quad \text{wrong-sign (WS)}$$

- **Selection:**

- $e^+e^- \rightarrow c\bar{c}$ events have high D^0 momentum in the CM frame.
 - Use momentum to reject BB events ($p_{D^0}^{\text{CMF}} > 2.5 \text{ GeV}/c$)
- Beam spot constraint determines t and σ_t and improves m_D and $\Delta m = m(D^0 \pi_s) - m(D^0)$ resolutions.

D^0 mixing: $D^0 \rightarrow KK$ vs $K\pi$ and y_{CP}

- Since 2007 evidence, $D^0 \leftrightarrow \bar{D}^0$ mixing established by combination of many measurements.
- D^0 mixing and CP violation alter decay time distribution of CP eigenstates
- – No single measurement with $>5\sigma$ significance.

$$\begin{aligned} |D_1\rangle &= p|D^0\rangle + q|\bar{D}^0\rangle \\ |D_2\rangle &= p|D^0\rangle - q|\bar{D}^0\rangle \end{aligned}$$

In the limit of CP conservation:

$$\begin{aligned} D_1 &= CP+ \\ D_2 &= CP- \end{aligned}$$

- If CP is conserved (CPV < 0.1% in SM) $D^0 \rightarrow K+K^-$ directly measures Γ_1 .

D^0 mixing parameters

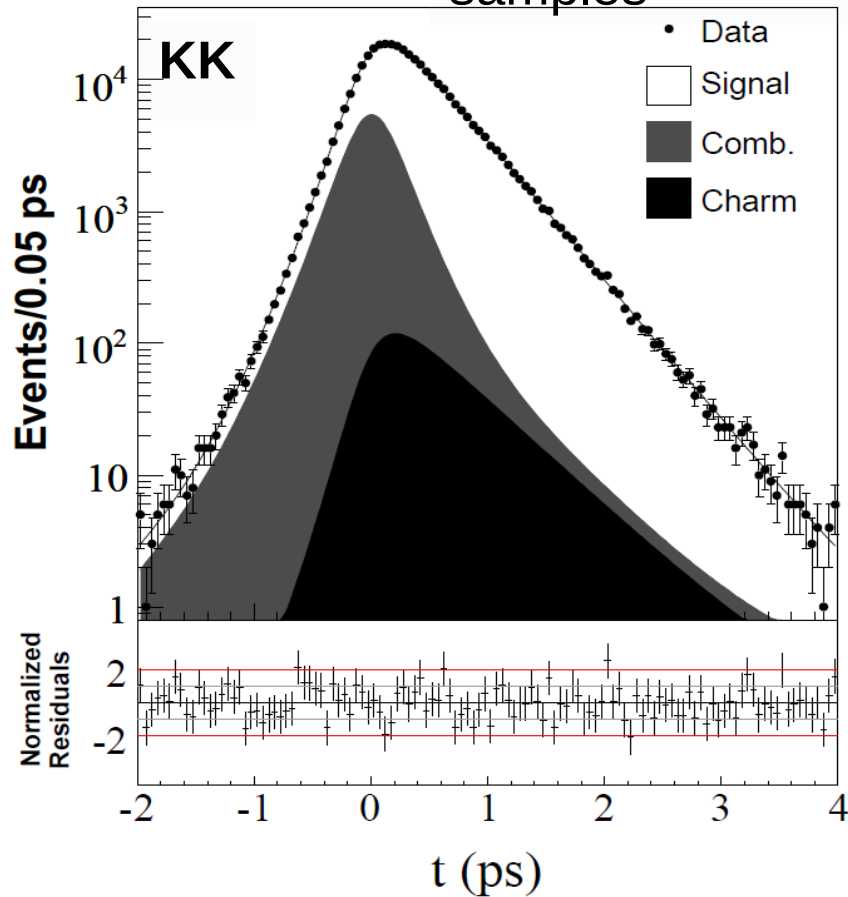
$$x \equiv 2 \frac{M_1 - M_2}{\Gamma_1 + \Gamma_2}, \quad y \equiv \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2} = \frac{\Gamma_1}{\Gamma} - 1$$

$$y_{CP} \equiv \frac{\tau_{K\pi}}{\tau_{KK}} - 1 = y$$

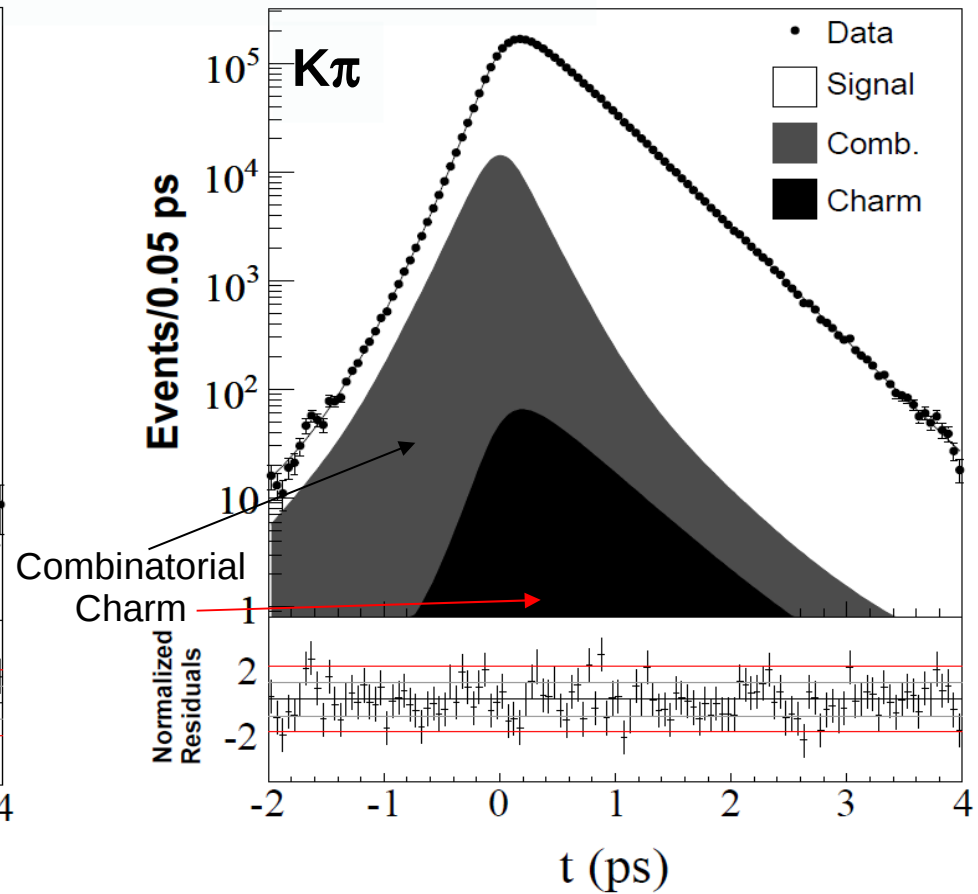
If CP conserved (SM)

D^0 mixing: $D^0 \rightarrow KK$ vs $K\pi$ and y_{CP}

Combined fit to KK and $K\pi$ data samples



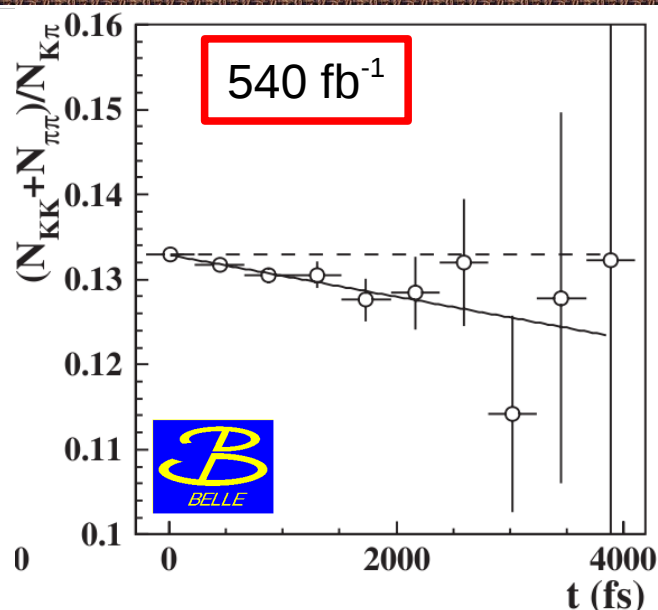
$$\tau_{KK} \text{ (fs)} \approx 405.85$$



$$\tau_{K\pi} \text{ (fs)} \approx 410.39$$

Resolution Offset
 $t_0 = -5.67 \pm 0.28 \text{ fs}$

Lifetime ratio $D^0 \rightarrow h^+ h^- / D^0 \rightarrow K^- \pi^+$



PRL 98, 211803 (2007) – Belle

$$y_{\text{CP}} = (1.31 \pm 0.32 \text{ (stat)} \pm 0.25 \text{ (syst)}) \cdot 10^{-2}$$

$$A_{\tau} = (0.01 \pm 0.30 \text{ (stat)} \pm 0.15 \text{ (syst)}) \cdot 10^{-2}$$

Mixing evidence at 3.2σ

PRD 78, 011105(R) (2008) – BaBar

Tagged:

$$y_{\text{CP}} = (1.03 \pm 0.33 \text{ (stat)} \pm 0.19 \text{ (syst)}) \cdot 10^{-2}$$

$$\Delta y = (-0.26 \pm 0.36 \text{ (stat)} \pm 0.08 \text{ (syst)}) \cdot 10^{-2}$$

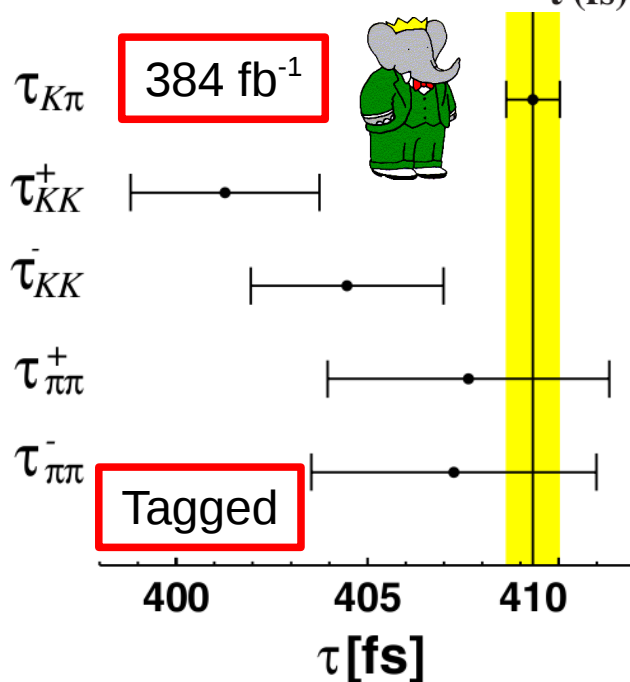
Mixing evidence at 3σ

PRD 80, 071103(R) (2009) – BaBar

Combined tagged + untagged:

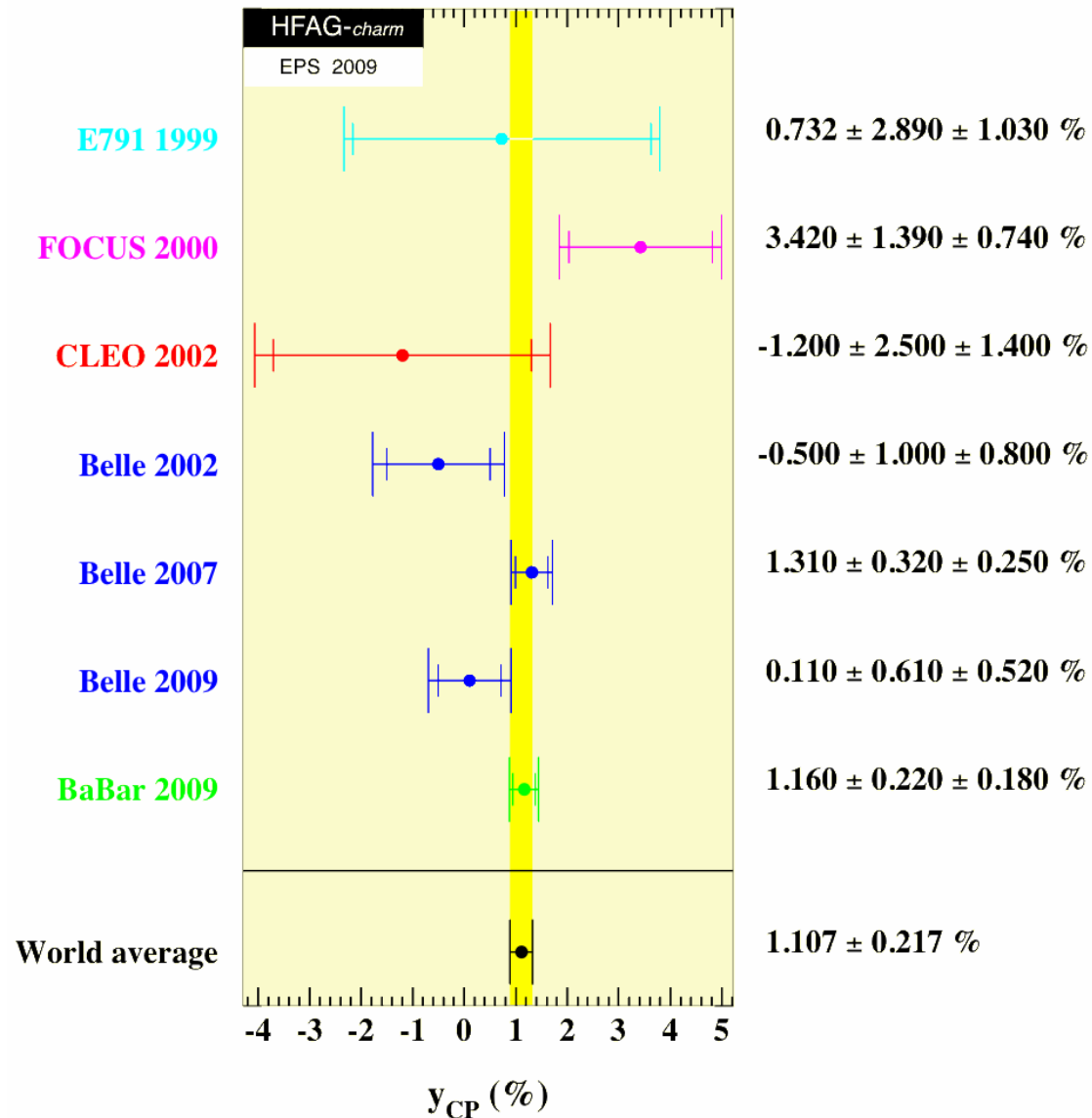
$$y_{\text{CP}} = (1.13 \pm 0.22 \text{ (stat)} \pm 0.18 \text{ (syst)}) \cdot 10^{-2}$$

Mixing evidence at 4.1σ



HFAG averages (measurements of y_{CP})

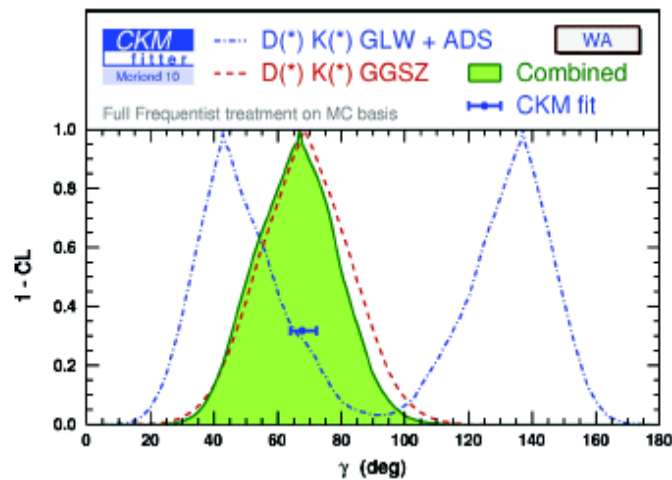
<http://www.slac.stanford.edu/xorg/hfag/charm/index.html>



Last Full Fit γ/ϕ_3 Results

Frequentist interpretation

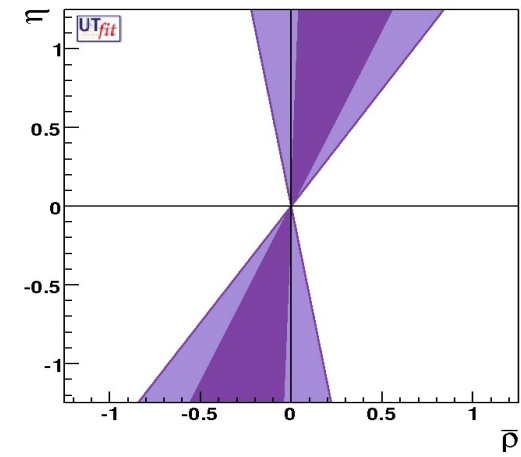
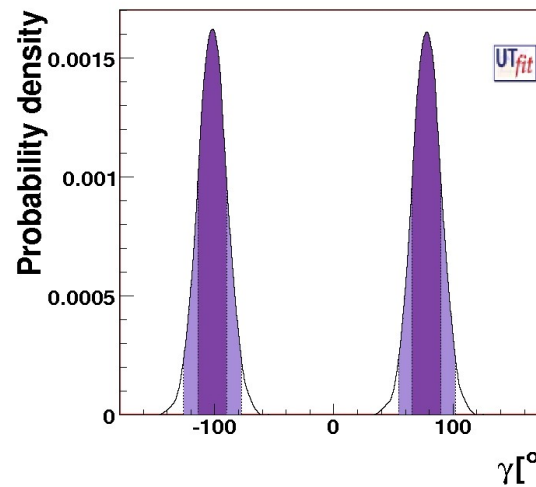
<http://ckmfitter.in2p3.fr>



$$\gamma = (69^{+19}_{-21})^\circ$$

μ supremum method used to combine HFAG averages of experimental inputs (conservative, but guarantees coverage).
See Karim Trabelsi's talk at CKM 2008 for details.

Bayesian interpretation



bound from
 $B \rightarrow DK, D^*K$ and DK^* decays with present measurements using all the methods.

$$\gamma = 78 \pm 12 \text{ ([54,102] @ 95\% Prob.)}$$

See:

<http://www.utfit.org/gamma/ckm-gamma.html>

Conclusions

- New results from Belle and BaBar in particular for the CKM angle γ/ϕ_3 :
 - Results from BaBar and Belle on Direct CPV using Dalitz plot analyses (new measurement on β and γ)
 - Measurement of the CKM angle γ using a GLW analysis of $B^\pm \rightarrow D(\text{CP}) K^\pm$ decays at BaBar
 - BaBar ADS analysis: $b \rightarrow u$ transitions in $B^- \rightarrow D^0 K^-$ and $B^- \rightarrow D^{*0} K^-$ decays (new result on γ)
 - D^0 mixing: $D^0 \rightarrow KK$ vs $K\pi$ and y_{CP}

Conclusions (continued)

- The data collection has ended but expect many more new and improved measurements and for the statistically limited measurements we look forward to the SuperB and BELLEII factories
- Many thanks to the Meson2010 organizers and the funding agencies

The end ...

Results from the Full Fit (utfit.org)

Parameter Value $\pm$ Error

$$\lambda \quad 0.2259 \pm 0.0016$$

$$\rho \quad 0.154 \pm 0.022$$

$$\eta \quad 0.342 \pm 0.014$$

$$\alpha(^{\circ}) \quad 92.0 \pm 3.4$$

$$\beta(^{\circ}) \quad 22.0 \pm 0.8$$

$$\gamma(^{\circ}) \quad 65.6 \pm 3.3$$

Dalitz plot fit results

BELLE

	Solution 1	Solution 2	Solution 3	Solution 4
$\mathcal{A}_{CP}(f_0 K_S^0)$	$-0.30 \pm 0.29 \pm 0.11 \pm 0.09$	$-0.20 \pm 0.15 \pm 0.08 \pm 0.05$	$+0.02 \pm 0.21 \pm 0.09 \pm 0.09$	$-0.18 \pm 0.14 \pm 0.08 \pm 0.06$
$\phi_1^{\text{eff}}(f_0 K_S^0)$	$(31.3 \pm 9.0 \pm 3.4 \pm 4.0)^\circ$	$(26.1 \pm 7.0 \pm 2.4 \pm 2.5)^\circ$	$(25.6 \pm 7.6 \pm 2.9 \pm 0.8)^\circ$	$(26.3 \pm 5.7 \pm 2.4 \pm 5.8)^\circ$
$\mathcal{A}_{CP}(\phi K_S^0)$	$+0.04 \pm 0.20 \pm 0.10 \pm 0.02$	$+0.08 \pm 0.18 \pm 0.10 \pm 0.03$	$-0.01 \pm 0.20 \pm 0.11 \pm 0.02$	$+0.21 \pm 0.18 \pm 0.11 \pm 0.05$
$\phi_1^{\text{eff}}(\phi K_S^0)$	$(32.2 \pm 9.0 \pm 2.6 \pm 1.4)^\circ$	$(26.2 \pm 8.8 \pm 2.7 \pm 1.2)^\circ$	$(27.3 \pm 8.6 \pm 2.8 \pm 1.3)^\circ$	$(24.3 \pm 8.0 \pm 2.9 \pm 5.2)^\circ$