

Formation of η Mesic Nucleus

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Outline of this talk

- 1 Introduction
- 2 Eta-Nucleus Interaction.... Based on Chiral Models
- 3 Formation of eta mesic nucleus by (π , N) reaction
- 4 Preliminary results for d+d reaction
- 5 Summary

Introduction and Motivation



■ Interests of Mesic Nucleus

1. Exotic Many Body Physics

... Physics of ‘Impurities’ and ‘Asymmetry’

2. Hadron Physics at finite density

... Possible connections to
symmetries of strong interaction

Introduction and Motivation

■ Mesons in nuclei and main interest

- » Pionic Atom ... fpi at finite density (Toki, Yamazaki, Hayano, Itahashi, Suzuki,,,))
- » K-atom & nuclei ... deeply bound nuclear state ? (Yamagata-Sekihara)
- » η -mesic nuclei ... $N^*(1535)$ in medium (Nagahiro, Jido,,,))
- » η' -mesic nuclei ... $U_A(1)$ anomaly in medium (Nagahiro, Takizawa)
- » Φ -mesic nuclei ... mass shift, OZI rule (Yamagata-Sekihara, Cabrera, Vicente-Vacas)
- » ω -mesic nuclei ... bound state ? mass shift ? (Kaskulov, Nagahiro, Oset)
- » σ -mesic nuclei ... $m_\sigma \sim 2m_\pi$ enhancement ? (Nagahiro, Hatsuda, Kunihiro)
- » -----
- » Θ^+ in medium ... $S=+1$ hypernuclei $[(K^+, \pi^+)]$ (Nagahiro, Oset, Vicente-Vacas)

Introduction of η -mesic nuclei

Motivation and our aim

- » η -N system ... strongly couples to the **$N^*(1535)$ resonance**
→ η -mesic nuclei ... doorway to **in-medium $N^*(1535)$**
- » **$N^*(1535)$** ... a candidate of the chiral partner of nucleon
→ **chiral symmetry for baryons**

Many works for η mesic nuclei from 1980's

- Theor. Liu, Haider, PRC34(1986)1845
 Kohno, Tanabe, PLB231(1989)219; NPA519(1990)755
 Garcia-Recio, Nieves, Inoue, Oset PLB550(02)47
 C. Wilkin, T. Ueda, S. Wycech,
- Exp. Chrien *et al.*, PRL60(1988)2595
 TAPS@MAMI ($\gamma + {}^3\text{He} \rightarrow \pi^0 + p + X$)
 COSY-GEM ($p + \text{Al} \rightarrow {}^3\text{He} + \text{Mg-}\eta$)
 WASA-at-COSY ($d + d \rightarrow {}^3\text{He} + p + \pi$)
 JPARC,

η -Nucleus system : Introduction

Our works for eta-mesic nuclei

- R.S. Hayano, S. Hirenzaki, A. Gillitzer, Eur. Phys. J. (99)
- D.Jido, H.Nagahiro and S.Hirenzaki, Phys.Rev.**C66**, 045202, 2002.
- H.Nagahiro, D.Jido, S.Hirenzaki, Phys.Rev.**C68**, 035205, 2003.
- H.Nagahiro, D.Jido and S.Hirenzaki, Nucl.Phys.**A761**,92, 2005.
- D.Jido, E.E.Kolomeitsev, H.Nagahiro, S.Hirenzaki, Nucl.Phys.**A811**:158, 2008.
- H.Nagahiro, D.Jido, S.Hirenzaki, Phys.Rev.**C80**,025205, 2009.

properties of eta meson

η meson

- » $m_\eta = 547.3$ [MeV] » $I = 0, J^P = 0^-$
- » $\Gamma = 1.18$ [keV] ($2\gamma, 3\pi^0, \pi^+\pi^-\pi^0, \dots$)

η -N system

- Strong Coupling to $N^*(1535)$, $J^P = \frac{1}{2}^-$

- » $\Gamma_{\pi N} \sim \Gamma_{\eta N} \sim 75$ [MeV]

ηNN^* system

- No $I=3/2$ baryon contamination
- Large coupling constant
- no suppression at threshold
(s-wave coupling)

$$\mathcal{L}_{\eta NN^*} = g_\eta \eta \bar{N} N + h.c.$$

eta-Nucleus system



Doorway to $N^*(1535)$

η -Nucleus Interaction $\sim N^*$ dominance model $\sim$

optical potential

$$V_{\text{opt}} = \frac{g_\eta^2}{2\mu} \frac{\rho}{\omega + m_N(\rho) - m_{N^*}(\rho) + i\Gamma_N^*(s; \rho)/2}$$

energy dependence

density-dependence

potential nature

In free space ($V \sim t\rho$)

$$\omega + m_N - m_{N^*} < 0 \quad \longrightarrow \quad \text{attractive}$$

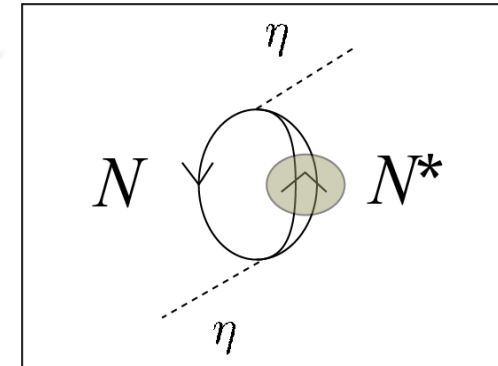
$$(m_\eta + m_N - m_{N^*} \sim -50\text{MeV})$$

medium effect

m_N & m_{N^*} change ??

$$\omega + m_N(\rho) - m_{N^*}(\rho) > 0 \quad \longrightarrow \quad \text{Repulsive ??}$$

N & N^* properties in medium evaluated
by two kinds of Chiral Models



(Chiang, Oset, Liu PRC44(1991)738)

(D.Jido, H.Nagahiro, S.H. PRC66(2002)045202)

$$g_\eta \simeq 2.0$$

to reproduce the partial width

$$\Gamma_{N^* \rightarrow \eta N} \simeq 75 \text{ MeV}$$

at tree level.

General feature

Chiral model for N and N*

Chiral doublet model

DeTar, Kunihiro, PRD39 (89)2805
Jido, Oka, Hosaka, Nemoto, PTP106(01)873
Jido, Hatsuda, Kunihiro, NPA671(00)471

Extended SU(2) Linear Sigma Model
for N and N*

Lagrangian

$$\mathcal{L} = \sum_{j=1,2} [\bar{N}_j i \not{\partial} N_j - g_j \bar{N}_j (\sigma + (-)^{j-1} i \gamma_5 \vec{\tau} \cdot \vec{\pi}) N_j] - m_0 (\bar{N}_1 \gamma_5 N_2 - \bar{N}_2 \gamma_5 N_1)$$

Physical fields

$$\begin{pmatrix} N \\ N^* \end{pmatrix} = \begin{pmatrix} \cos \theta & \gamma_5 \sin \theta \\ -\gamma_5 \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix}$$

N* : chiral partner of nucleon

Mass difference

$$m_N^*(\rho) - m_N^*(\rho) = (1 - C \frac{\rho}{\rho_0})(m_N - m_{N^*})$$

* C~0.2 :the strength of the Chiral restoration at the nuclear saturation density

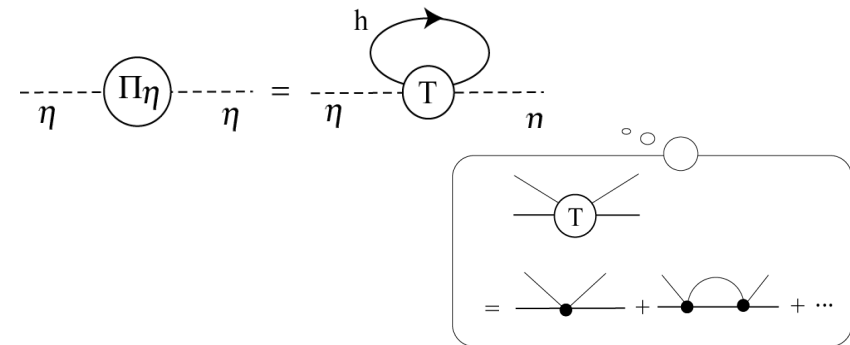
*** reduction of mass difference**

Chiral unitary model

Kaiser, Siegel, Weise, PLB362(95)23
Waas, Weise, NPA625(97)287
Garcia-Recio, Nieves, Inoue, Oset, PLB550(02)47
Inoue, Oset, NPA710(02) 354

* In this study, we directly take the eta-self-energy in the ref.NPA710(02)354
A coupled channel Bethe-Salpeter eq.

$$\{\pi^- p, \pi^0 n, \eta n, K^0 \Lambda, K^+ \Sigma^-, K^0 \Sigma^0, \pi^0 \pi^- p, \pi^+ \pi^- n\}$$



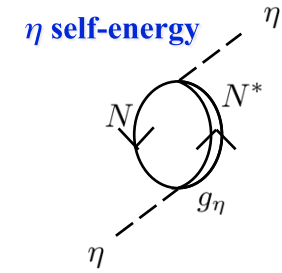
* the N* is introduced as **a resonance generated dynamically** from meson-baryon scattering.

*** No mass shift of N* is expected in the nuclear medium.**

η -nucleus interaction : potential descriptions

optical potential

$$V_{\text{opt}} \equiv \frac{\Pi_\eta}{2\mu} = \frac{g_\eta^2}{2\mu} \frac{\rho(r)}{\omega - (m_{N^*}(\rho) - m_N(\rho)) + i\Gamma_{N^*}(s; \rho)/2} + (\text{crossed term})$$



potential nature at η threshold

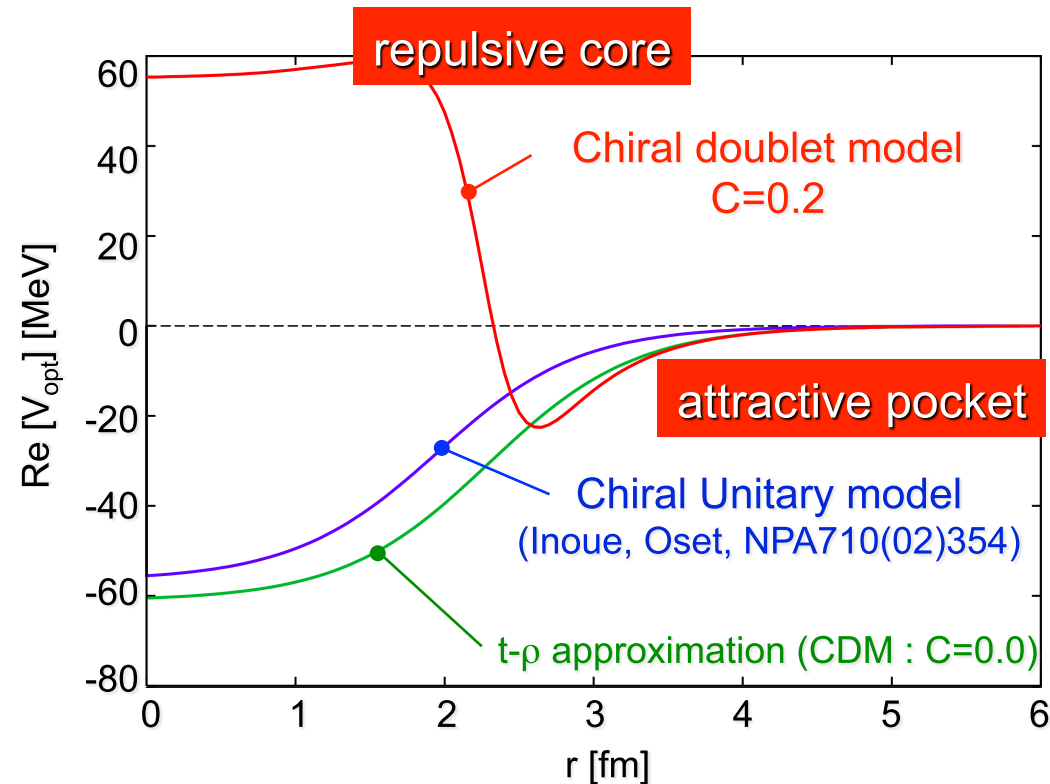
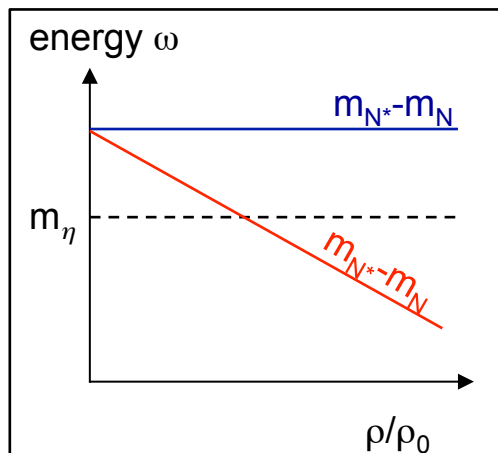
$$m_\eta - (m_{N^*} - m_N) < 0$$

attractive

medium effect

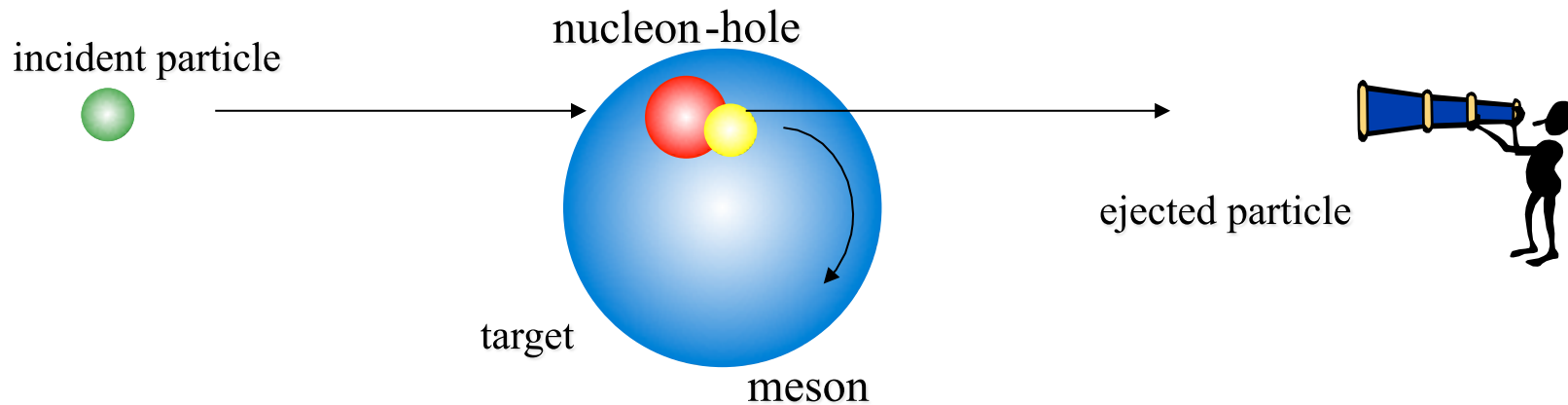
$$m_\eta - (m_{N^*}(\rho) - m_N(\rho)) > 0$$

repulsive



•D.Jido, H.Nagahiro and S.Hirenzaki, PRC66(02)045202

Formation by the Missing mass spectroscopy



Candidate reactions for the mesic nuclei formation

- » $(d, {}^3\text{He})$ reaction ... established method π atom formation (96, 98, 01)

S.Hirenzaki, H.Toki, T.Yamazaki, PRC44(91)2472, ...

K.Itahashi, *et al.*, PRC62(00)025202, ...

- » (γ, p) reaction ... smaller distortion effect

M.Kohno, H.Tanabe PLB231(89)219

E.Marco, W.Weise, PLB502(01)59

H.Nagahiro, D.Jido, S.Hirenzaki, Nucl. Phys. **A761** (2005) 92-119 etc..

- » (π, N) reaction

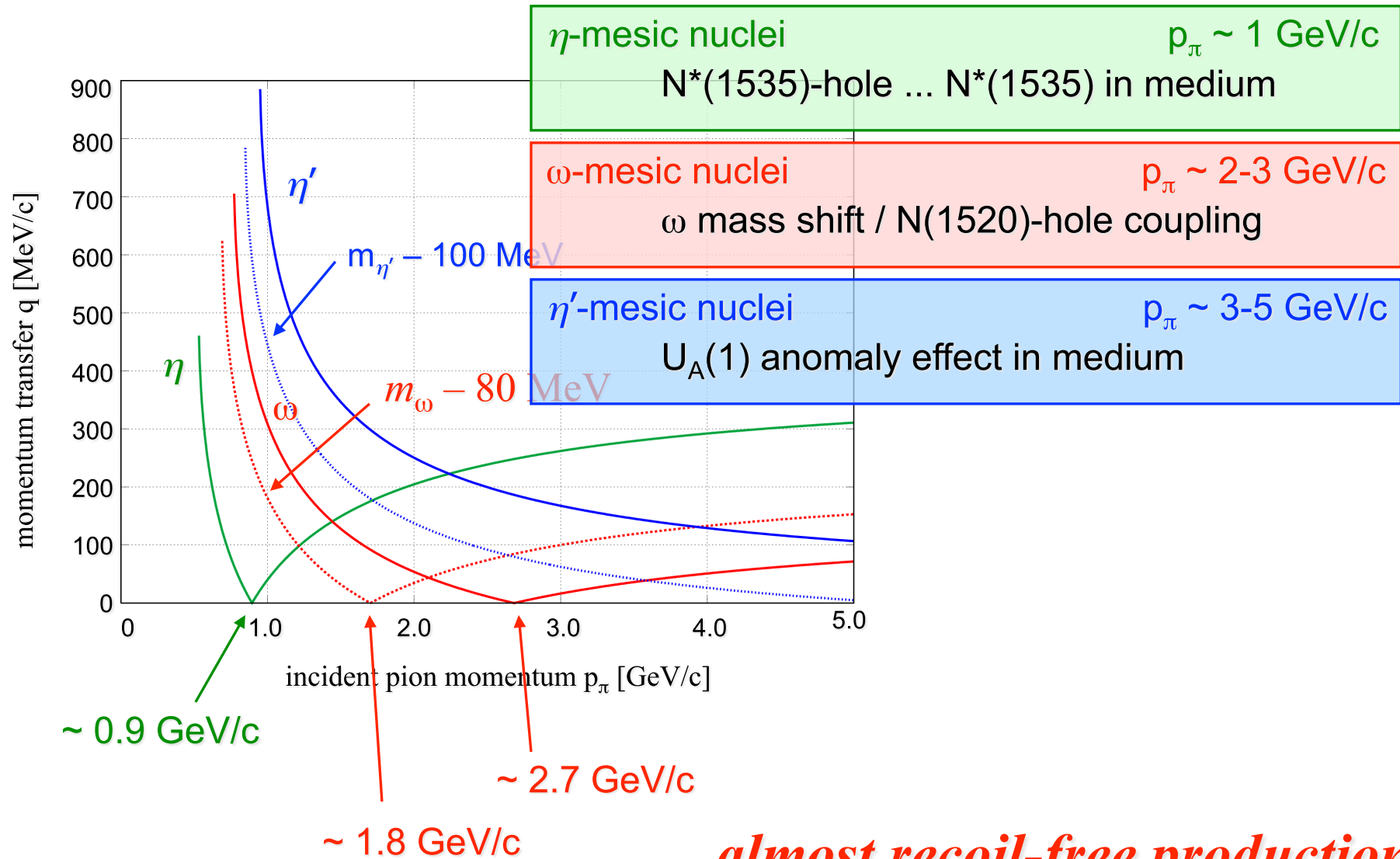
Chrien *et al.*, PRL60(1988)2595

Liu, Haider, PRC34(1986)1845

H.Nagahiro, D.Jido, S.Hirenzaki, PRC80(2009)025205, ...

meson production in recoil-free kinematics

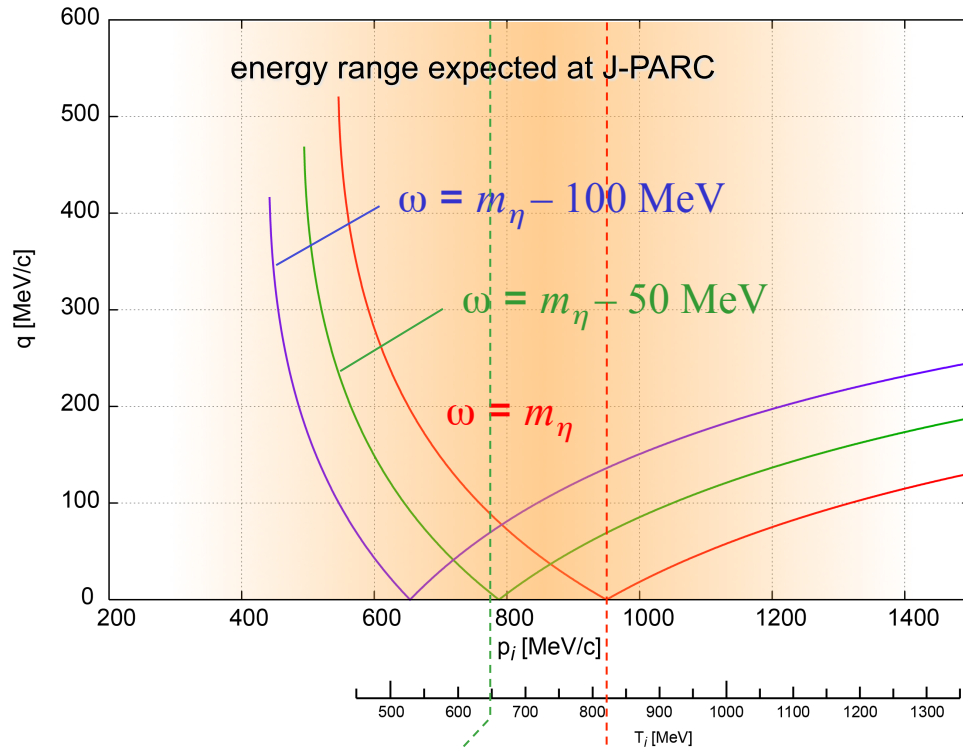
magic momentum in $^{12}\text{C}(\pi, \text{N})$ reaction



almost recoil-free production

$^{12}\text{C}(\pi^+, p)^{11}\text{C}_\eta$ reaction

Momentum transfer : forward proton angle



$T_\pi = 650 \text{ MeV } (p_\pi \sim 777 \text{ MeV/c}) \rightarrow \left(\frac{d\sigma}{d\Omega} \right)^{Lab.} = 2.4 \text{ mb/sr}$

$T_\pi = 820 \text{ MeV } (p_\pi \sim 950 \text{ MeV/c}) \rightarrow \left(\frac{d\sigma}{d\Omega} \right)^{Lab.} = 0.64 \text{ mb/sr}$

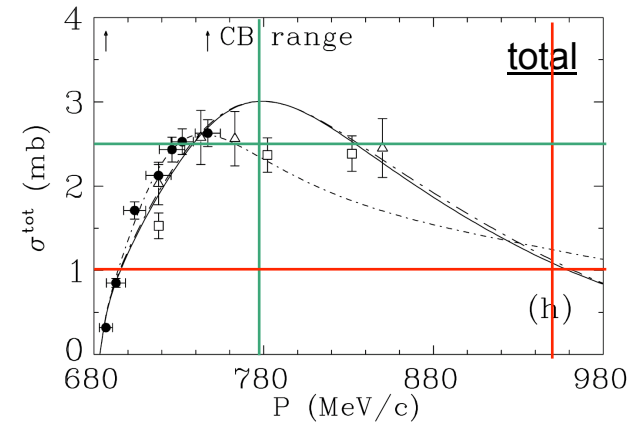
Elementary cross section

$$\pi^- p \rightarrow \eta n$$

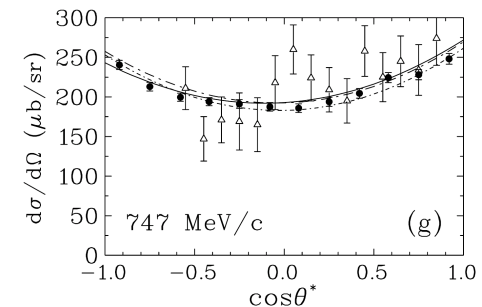
S.Prakhov *et al.*, [Crystal Ball Collaboration]
PRC72,015203 (2005).

$$\pi^+ n \rightarrow \eta p$$

Total cross section



Angular distribution ~ Nearly flat



Formulation : $\pi + A \rightarrow p + (A-1)_\eta$

Green's function method [Morimatsu, Yazaki NPA435(85)727, NPA483(88)493]

impulse approximation

$$\left(\frac{d^2\sigma}{d\Omega dE} \right) = \left(\frac{d\sigma}{d\Omega} \right)_{n(\pi,p)\eta}^{Lab.} \times S(E)$$

elementary cross section $\pi^+ + n \rightarrow p + \eta$

$$\left(\frac{d\sigma}{d\Omega} \right)^{Lab.} = 2.4 \text{mb/sr}$$

S.Prakhov *et al.*,
[Crystal Ball Collaboration]
PRC72,015203 (2005).

nuclear response function

$$S(E) = -\frac{1}{\pi} \text{Im} \sum_f \mathcal{T}_f^\dagger G(E) \mathcal{T}_f$$

Green's function

$$G(E, \mathbf{r}, \mathbf{r}') = \langle p^{-1} | \phi_\eta(\mathbf{r}) \frac{1}{E - H_\eta + i\epsilon} \phi_\eta^\dagger(\mathbf{r}') | p^{-1} \rangle$$

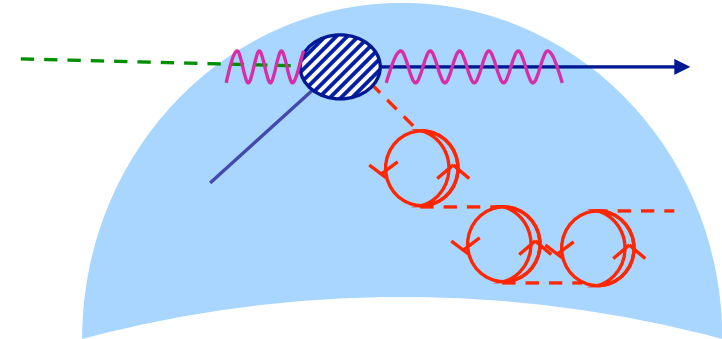
transition amplitude

$$\mathcal{T}_f(\mathbf{r}) = \chi_f^*(\mathbf{r}) \xi_{1/2, m_s}^* \left[Y_{\ell_\eta}^*(\hat{r}) \otimes \psi_{j_p}(\mathbf{r}) \right]_{JM} \chi_i(\mathbf{r})$$

Distortion factor : flux reduction due to absorption

$$\chi_f^*(\mathbf{r}) \chi_i(\mathbf{r}) = \exp[i\mathbf{q} \cdot \mathbf{r}] F(\mathbf{b}) \quad \text{eikonal approximation}$$

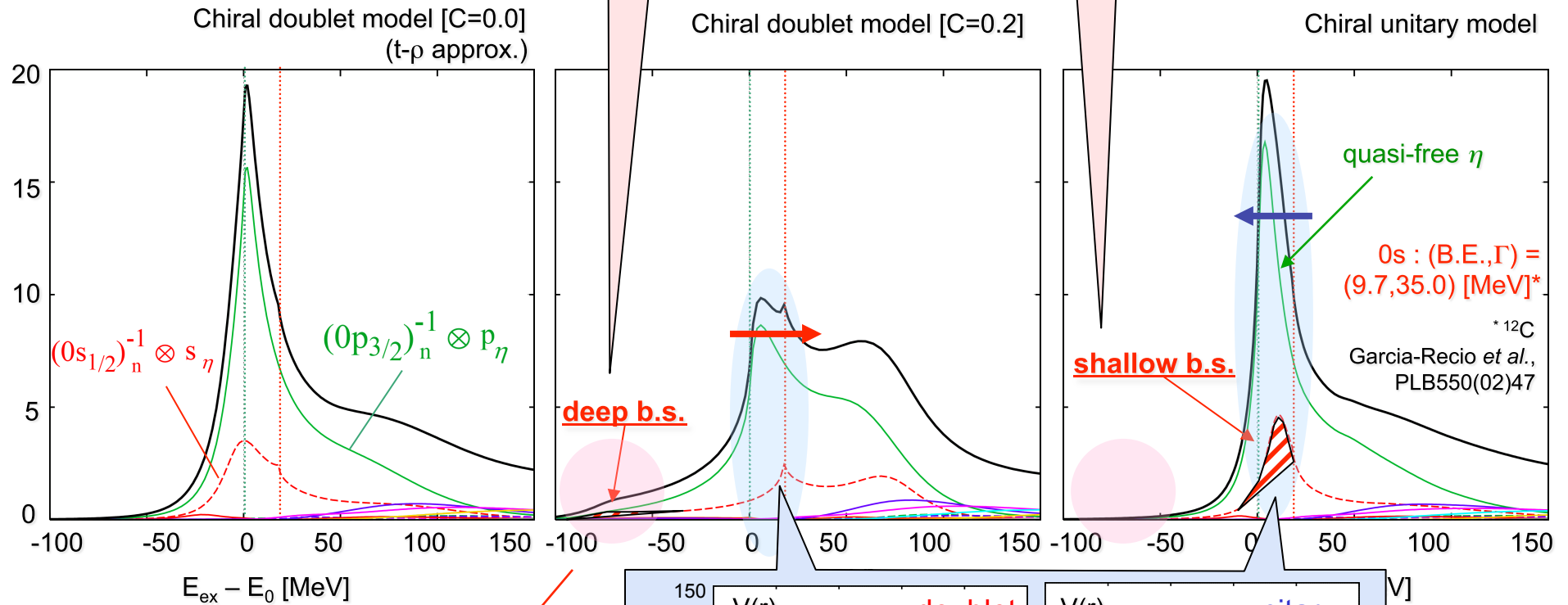
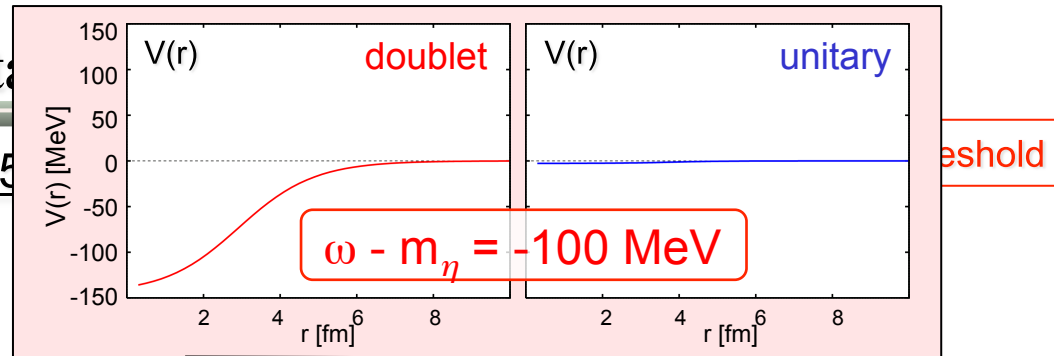
$$F(b) = \exp \left[-\frac{1}{2} \sigma_{iN} \int_{-\infty}^z dz' \rho_A(z', b) - \frac{1}{2} \sigma_{fN} \int_z^{\infty} dz' \rho_{A-1}(z', b) \right]$$



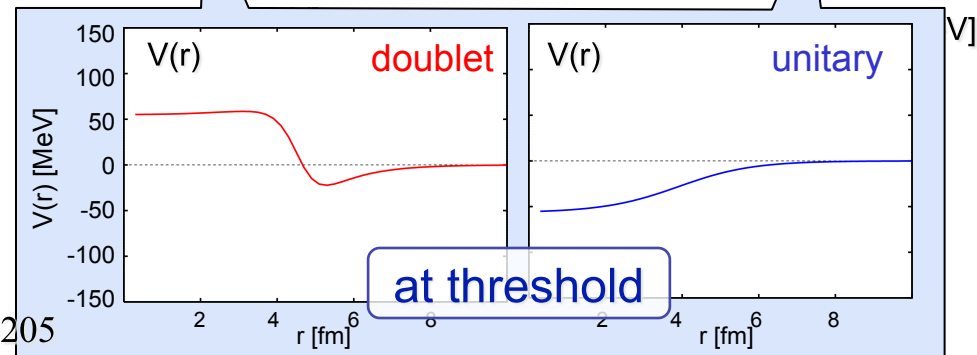
(π^+, p) spectra : ^{12}C

$$T_{\pi} = 820 \text{ MeV} \quad (p_{\pi} = 95 \text{ MeV/c})$$

$$\frac{d^2\sigma}{dEd\Omega} [\mu\text{b/srMeV}]$$



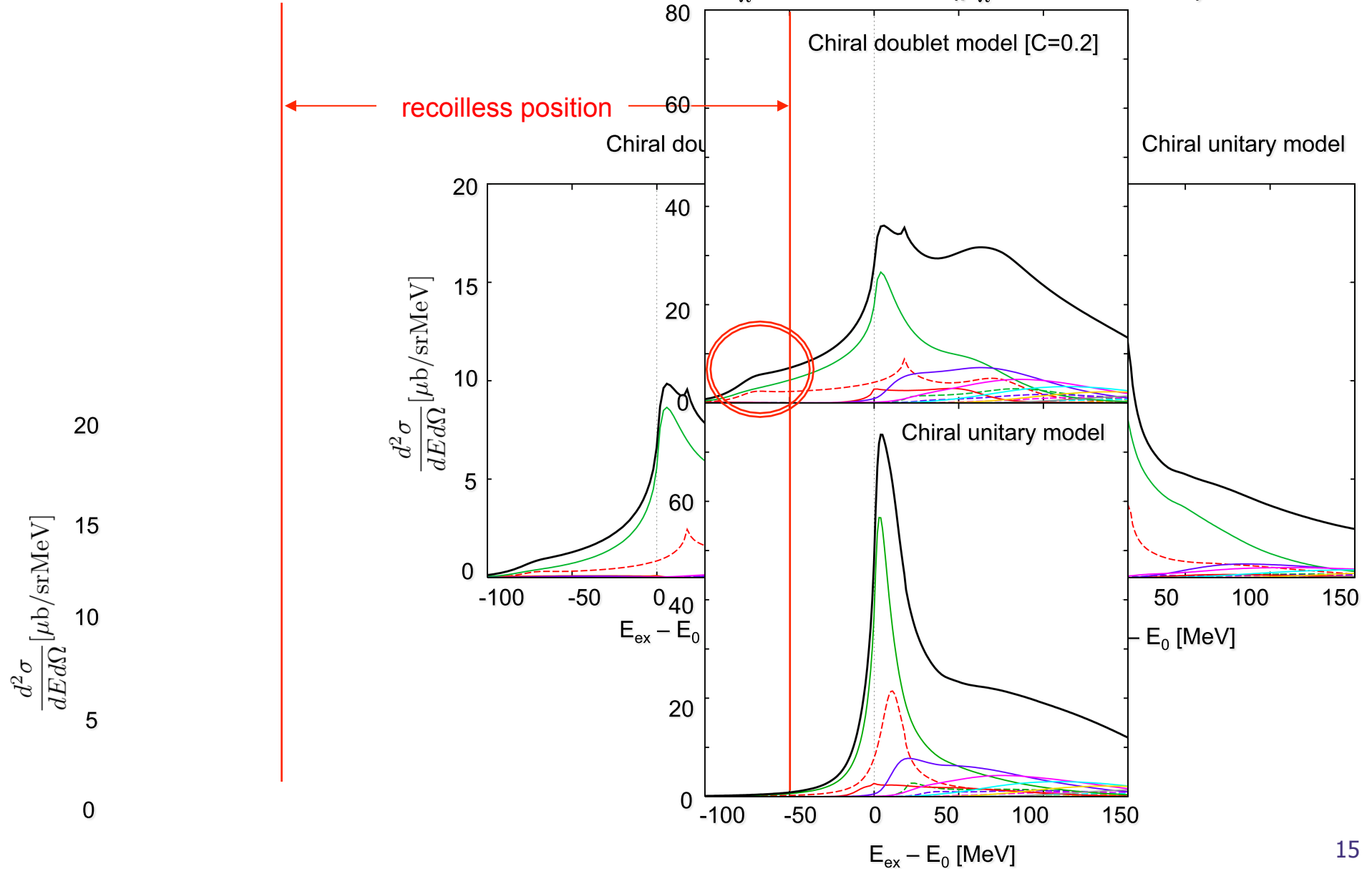
$$0s : (B.E., \Gamma) = (91.3, 26.3) [\text{MeV}]$$



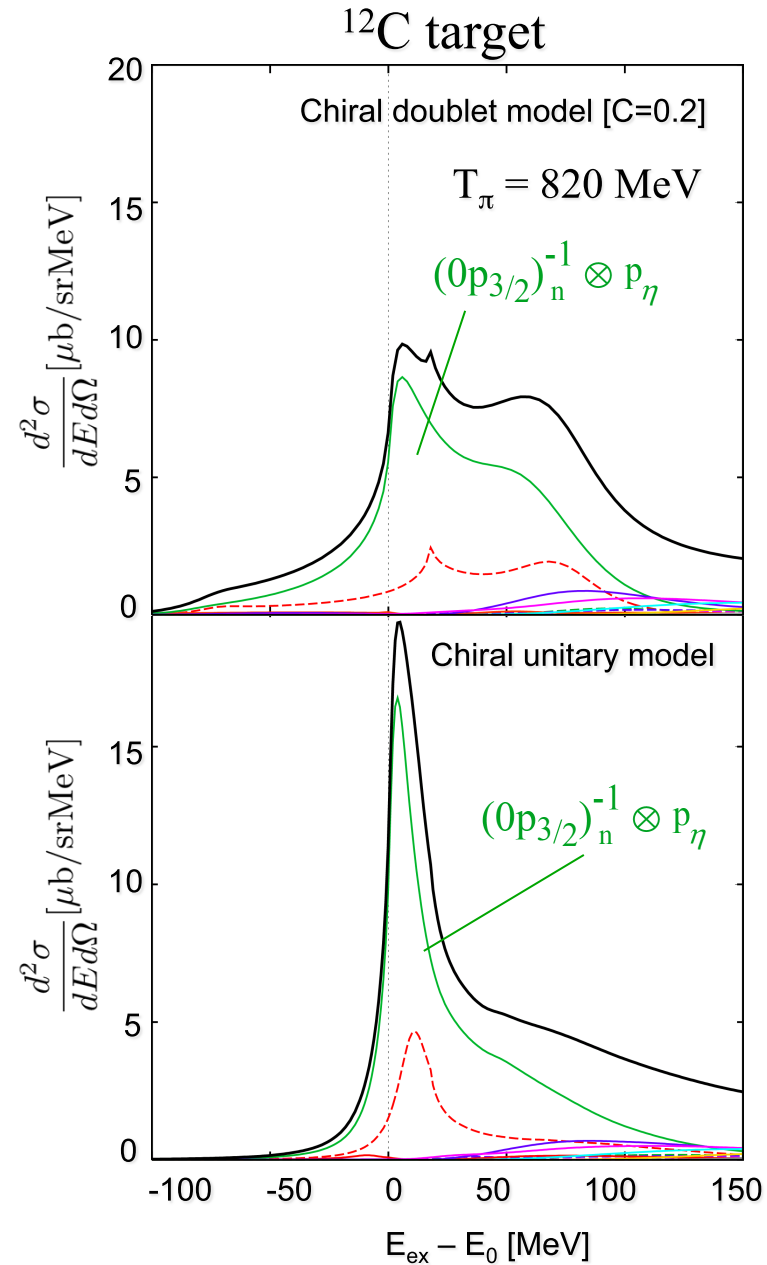
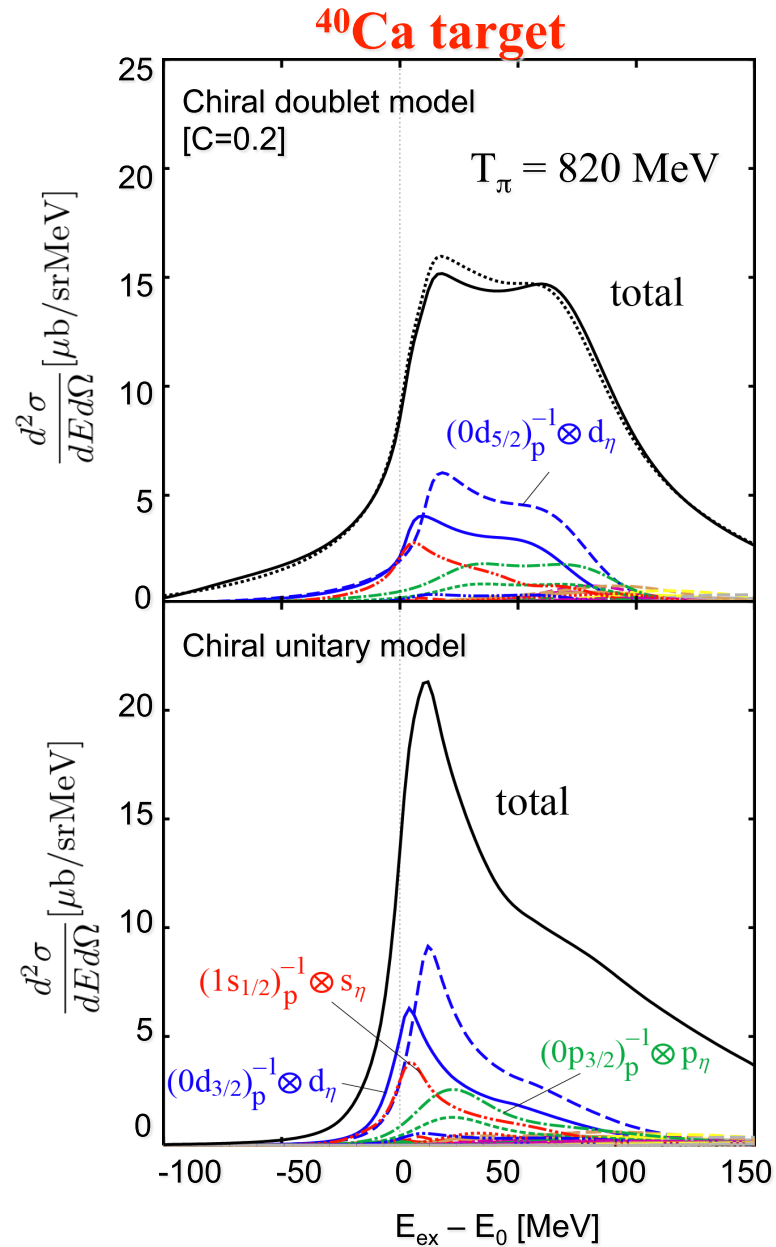
(π^+, p) spectra : ^{12}C target : incident energy dependence

$T_\pi = 820 \text{ MeV}$ ($p_\pi = 950 \text{ MeV/c}$)

$T_\pi = 650 \text{ MeV}$ ($p_\pi = 777 \text{ MeV/c}$)



Target dependence : (π^-, n) spectrum (proton picked up)



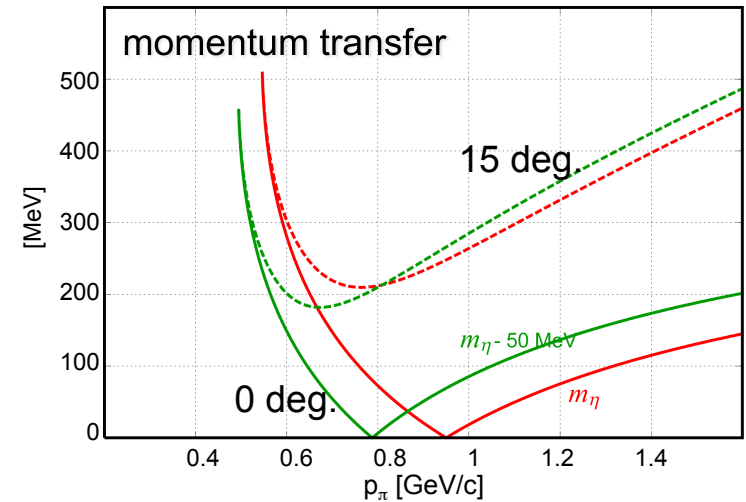
(π^+, p) spectra : experiment at Brookhaven

■ Chrien et al., PRL60(1988)2595

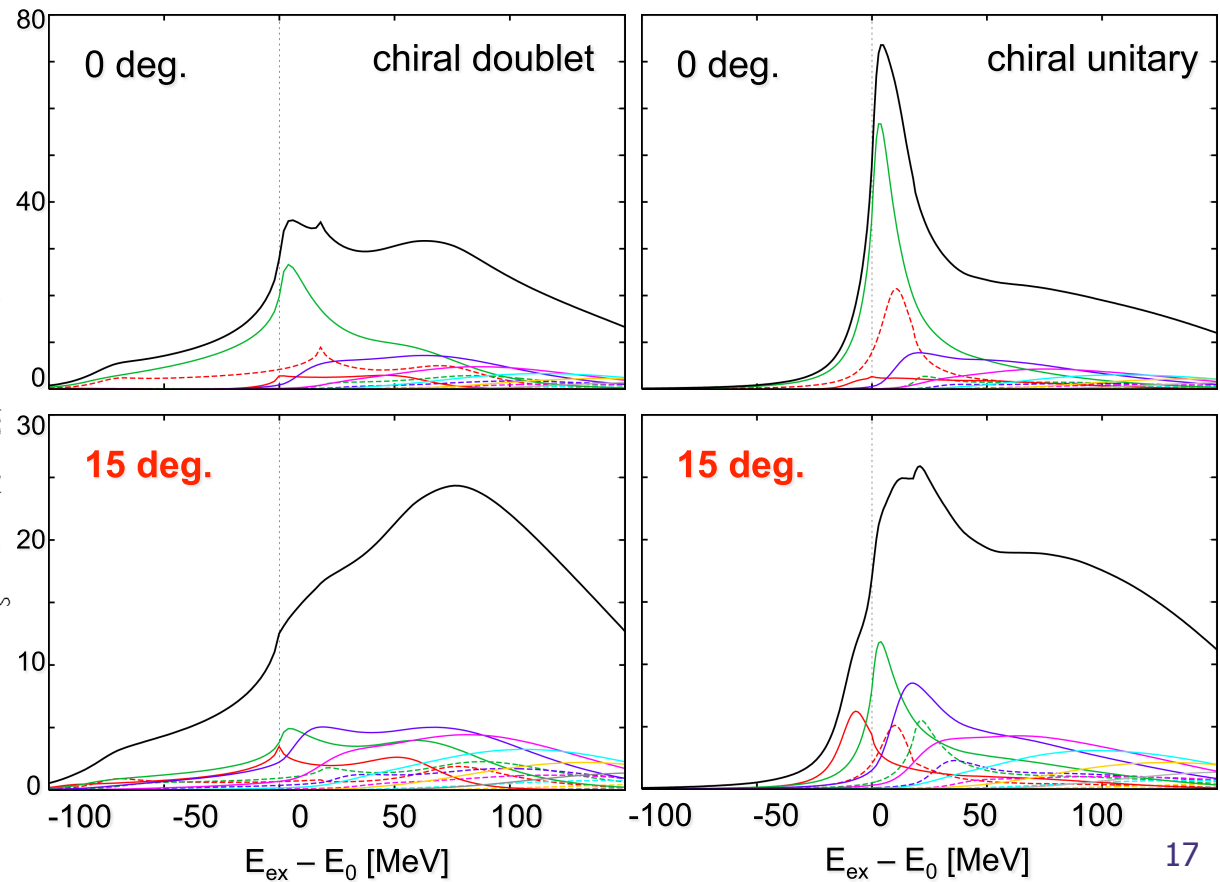
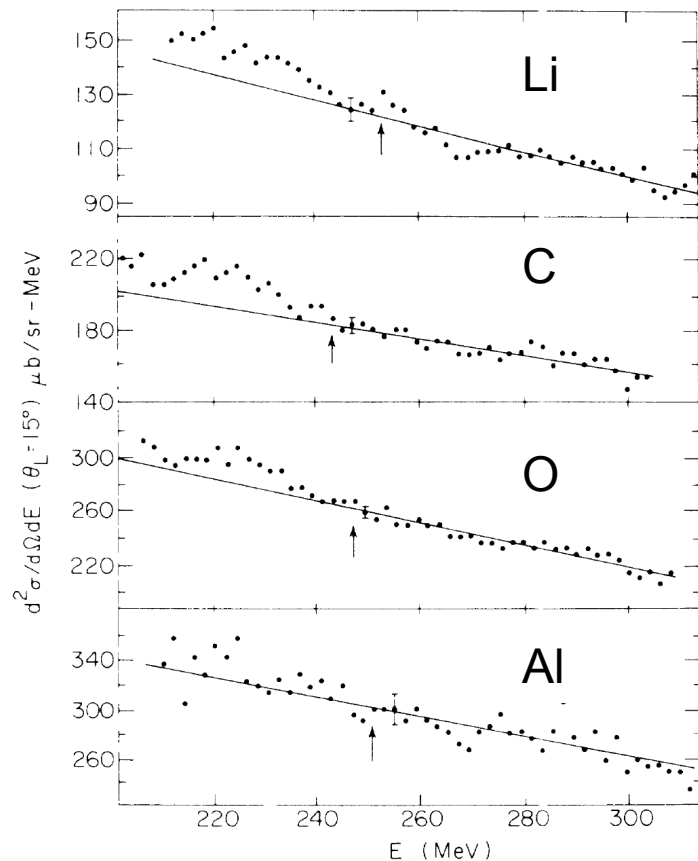
» $p_\pi = 800 \text{ MeV/c}$: proton angle : **15 deg. (Lab.)**

» search for predicted narrow bound state
by Liu, Haider, PRC34(86)1845

→ negative results (bound state peak was not observed)



Chrien et al., PRL60(1988)2595, Fig11



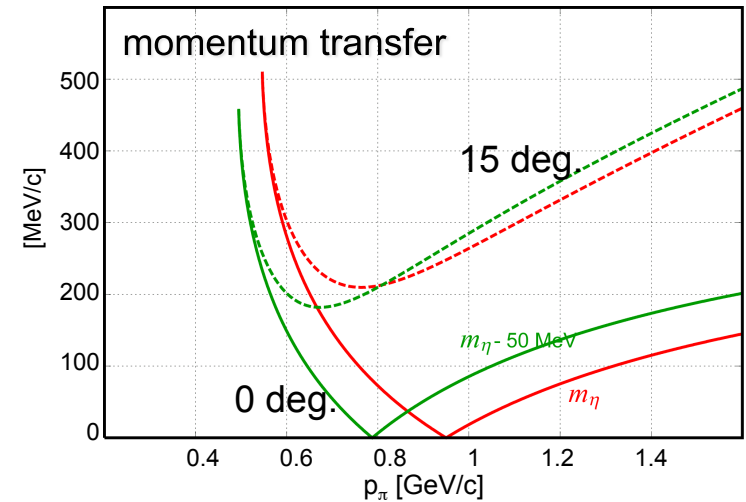
(π^+, p) spectra : experiment at Brookhaven

■ Chrien et al., PRL60(1988)2595

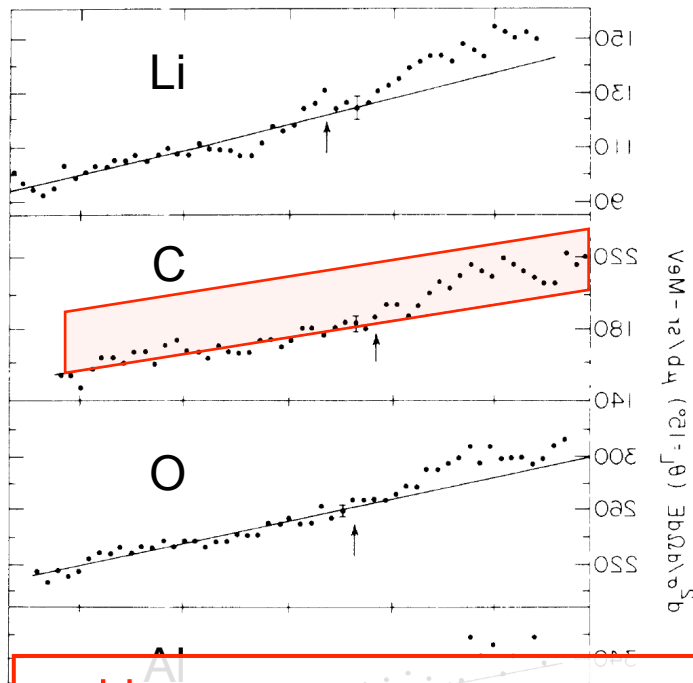
» $p_\pi = 800 \text{ MeV/c}$: proton angle : **15 deg. (Lab.)**

» search for predicted narrow bound state
by Liu, Haider, PRC34(86)1845

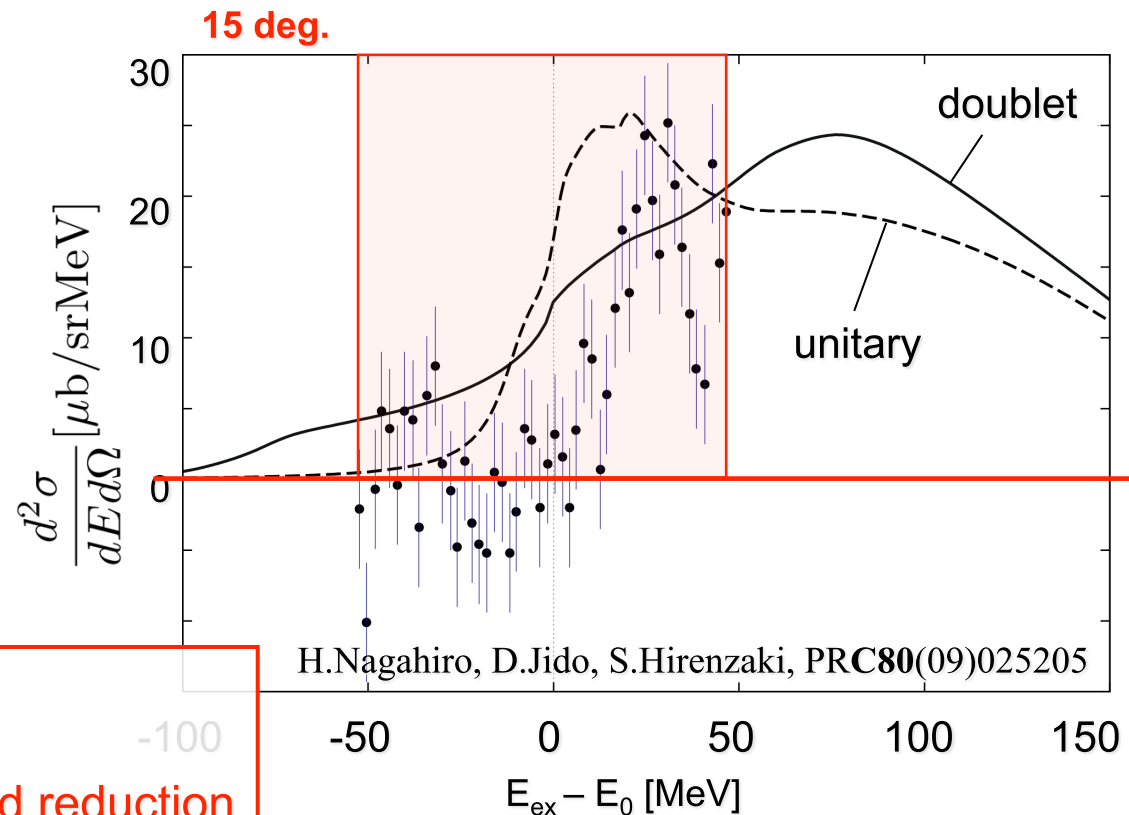
→ negative results (bound state peak was not observed)



Chrien et al., PRL60(88)2595, Fig.1

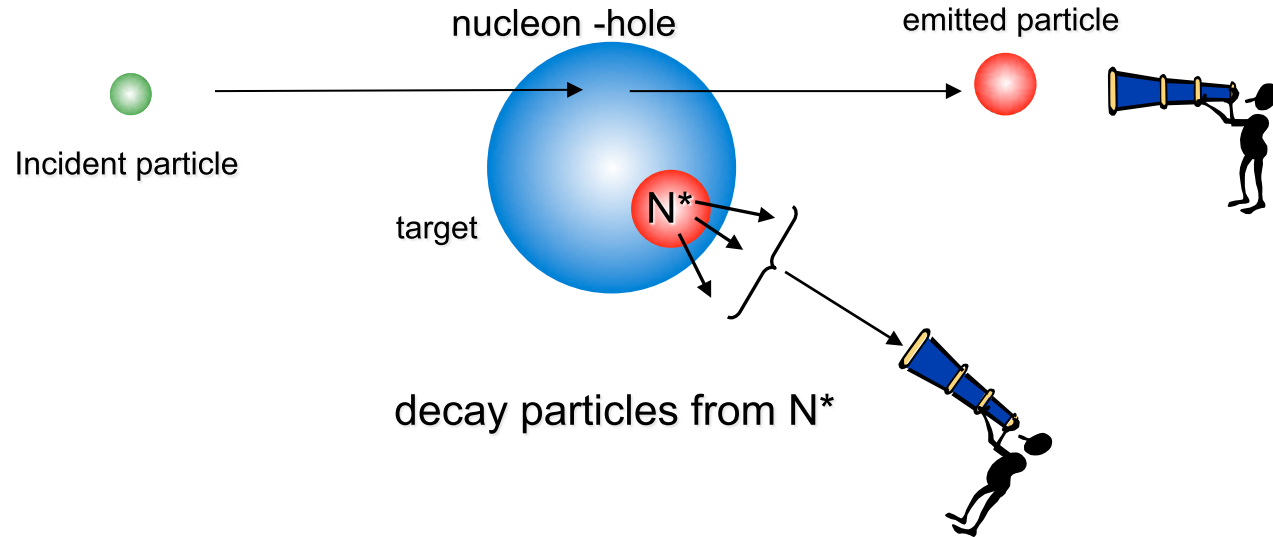
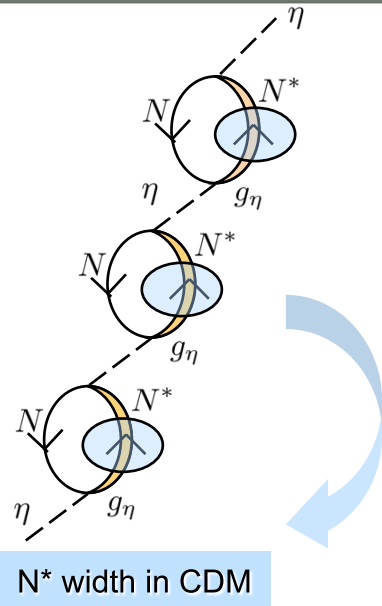


- wider energy range
- proton angle = 0 degree
- S/N $\sim 1/10 \rightarrow$ need background reduction

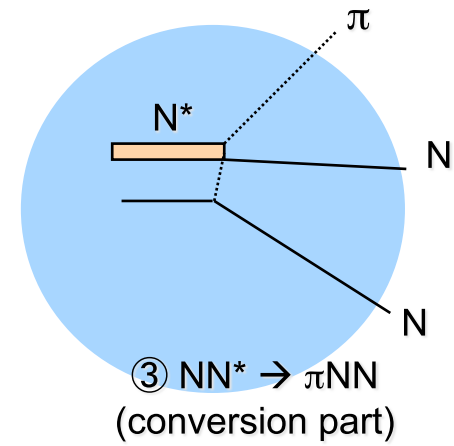
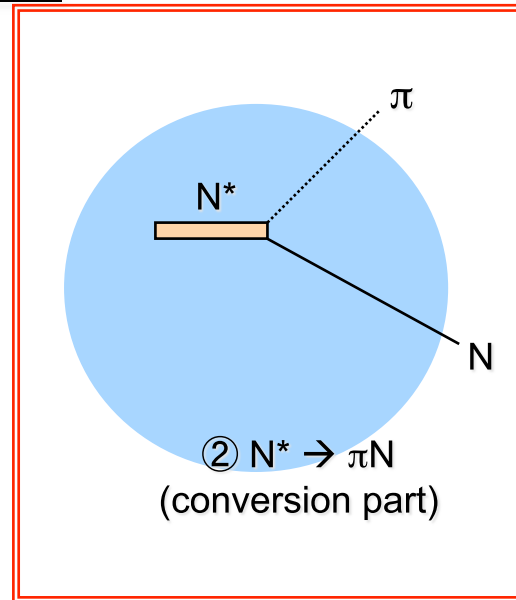
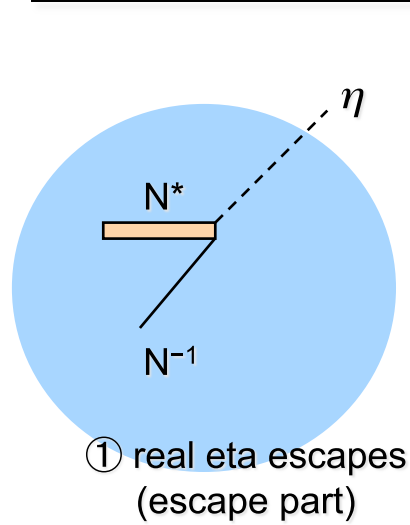
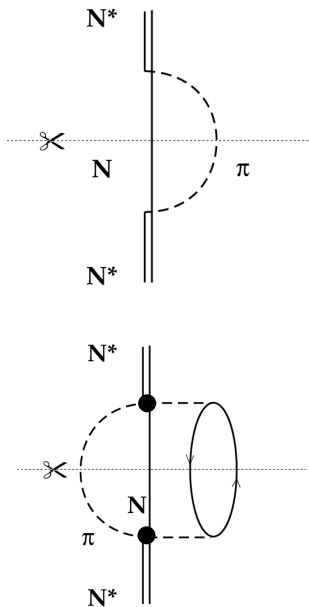


H.Nagahiro, D.Jido, S.Hirenzaki, PRC80(09)025205

background reduction : coincidence measurement



final states we considered



Green's function method

Ref. O.Morimatsu and K. Yazaki, NPA435(1985)727-737

where $\varepsilon_\alpha = E_\alpha - E_i$ is the nucleon separation energy for the state $|\alpha\rangle$, and G is the Green function for the optical potential U , satisfying the equation

$$G = G_0 + G_0 U G \quad (10)$$

with G_0 denoting the free Green function for Σ .

Taking the imaginary part of eq. (10), we obtain the following identity:

$$\text{Im } G = (1 + G^+ U^+) \text{Im } G_0 (1 + U G) + G^+ \text{Im } U G. \quad (11)$$

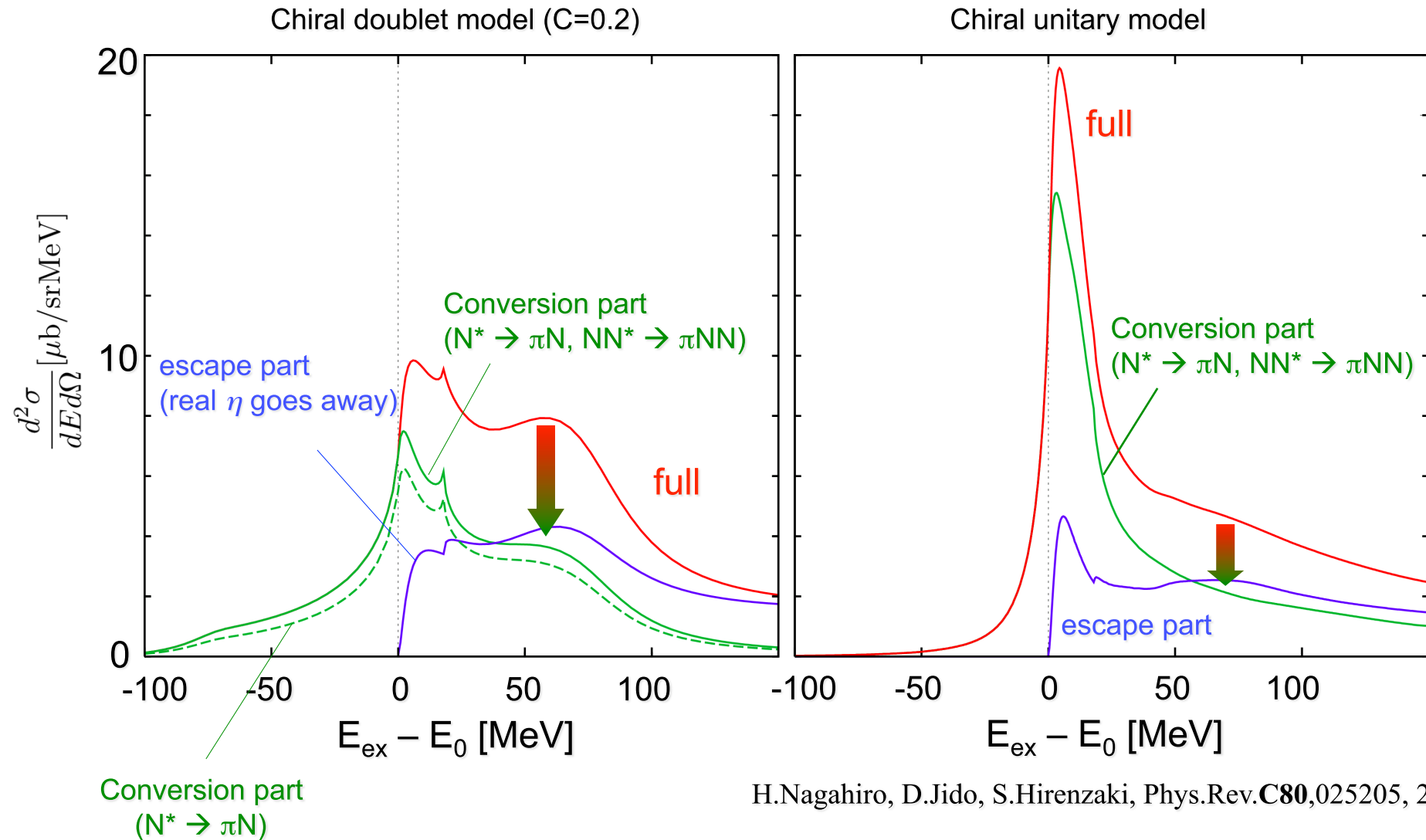
The first term on the r.h.s. of eq. (11) represents the contribution from the escape of the Σ from the nucleus, while the second term is due to the conversion of the Σ into Λ because the imaginary part of U is due to this conversion effect. Let us define the following quantities:

$$\begin{aligned} S_{\text{tot}}(E) &= -\tilde{f} \text{Im } G f \\ &= -\sum_{\alpha} \text{Im} \int d\mathbf{r} d\mathbf{r}' f_{\alpha}^*(\mathbf{r}') G(E - \varepsilon_{\alpha}; \mathbf{r}', \mathbf{r}) f_{\alpha}(\mathbf{r}), \end{aligned} \quad (12)$$

$$\Rightarrow S_{\text{esc}}(E) = -\tilde{f} (1 + G^+ U^+) \text{Im } G_0 (1 + U G) f, \quad (13)$$

$$\Rightarrow S_{\text{con}}(E) = -\tilde{f} G^+ \text{Im } U G f. \quad (14)$$

effect on “the signal” by coincidence measurement

H.Nagahiro, D.Jido, S.Hirenzaki, Phys.Rev.**C80**,025205, 2009

future work : estimation of absolute value of background

A Simple Theoretical Model for $d + d \rightarrow (^4\text{He}-\eta) \rightarrow p + \pi^- + ^3\text{He}$

(COSY Proposal 186.2)

(P.Moskal, arXiv:nucl-ex/09093979)

Some remarks

- Momentum transfer

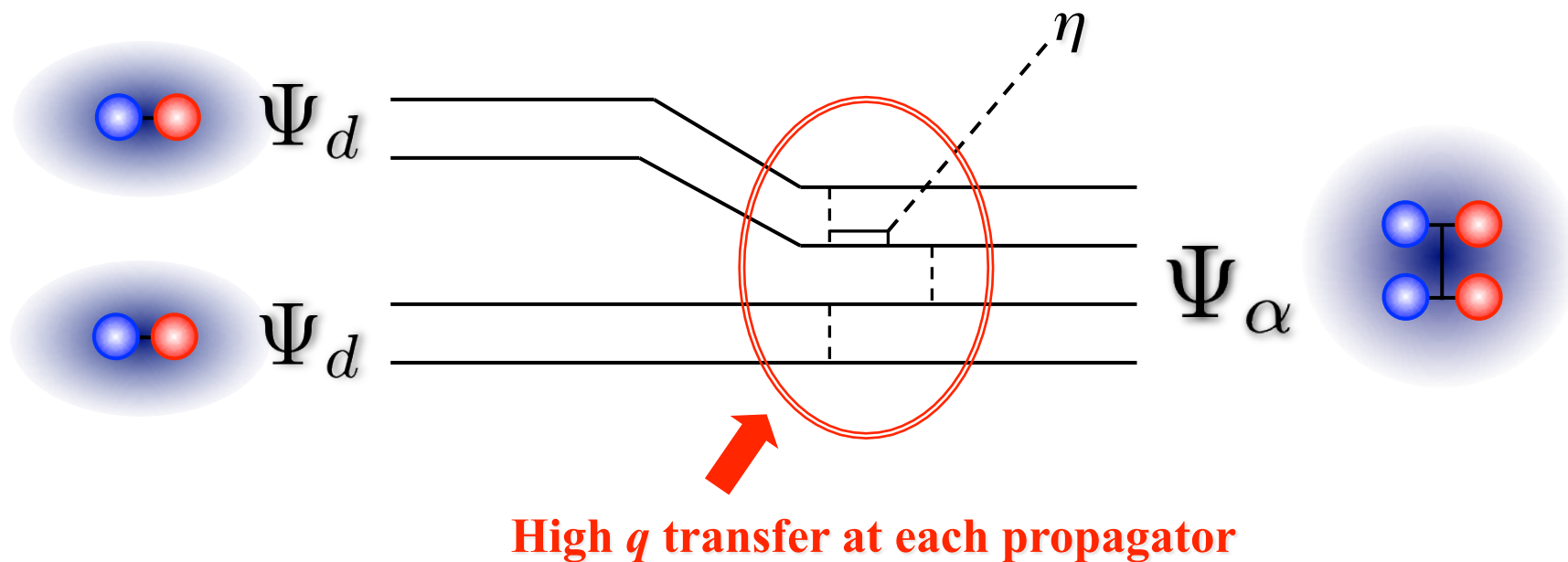
$$p_d = 1.025 \text{ GeV}/c, \quad p_\alpha = p_\eta = 0 \quad \text{at threshold in C.M.}$$

- Data of $d d \rightarrow ^4\text{He} \eta$
- Simple spectral structure for light systems
- System consists of
 $2 \text{ Nucleon} + 2 \text{ Nucleon} \rightarrow 4 \text{ Nucleon} + 1 \text{ meson}$

A Simple Theoretical Model for $d + d \rightarrow (^4\text{He}-\eta) \rightarrow p + \pi^- + ^3\text{He}$

Some remarks

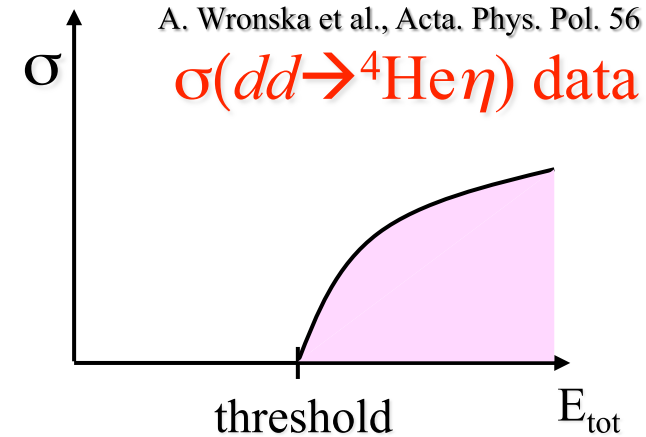
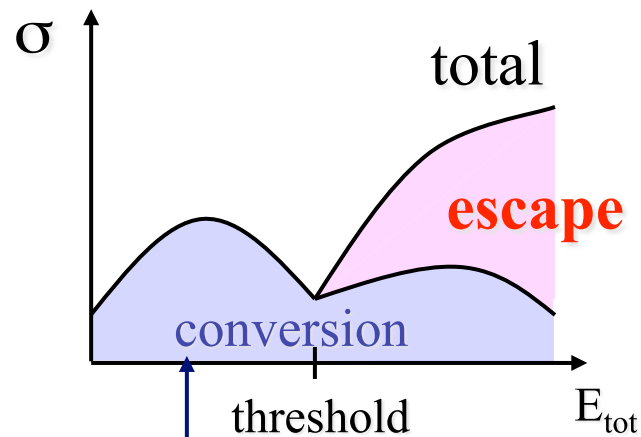
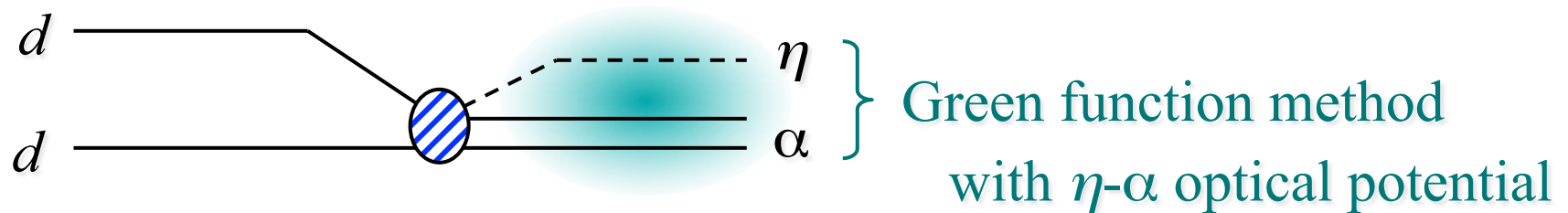
- Transition (η -production) part



→ Parameterize this part. Fix by η production data

A Simple Theoretical Model for $d + d \rightarrow (^4\text{He}-\eta) \rightarrow p + \pi^- + ^3\text{He}$

Schematic picture

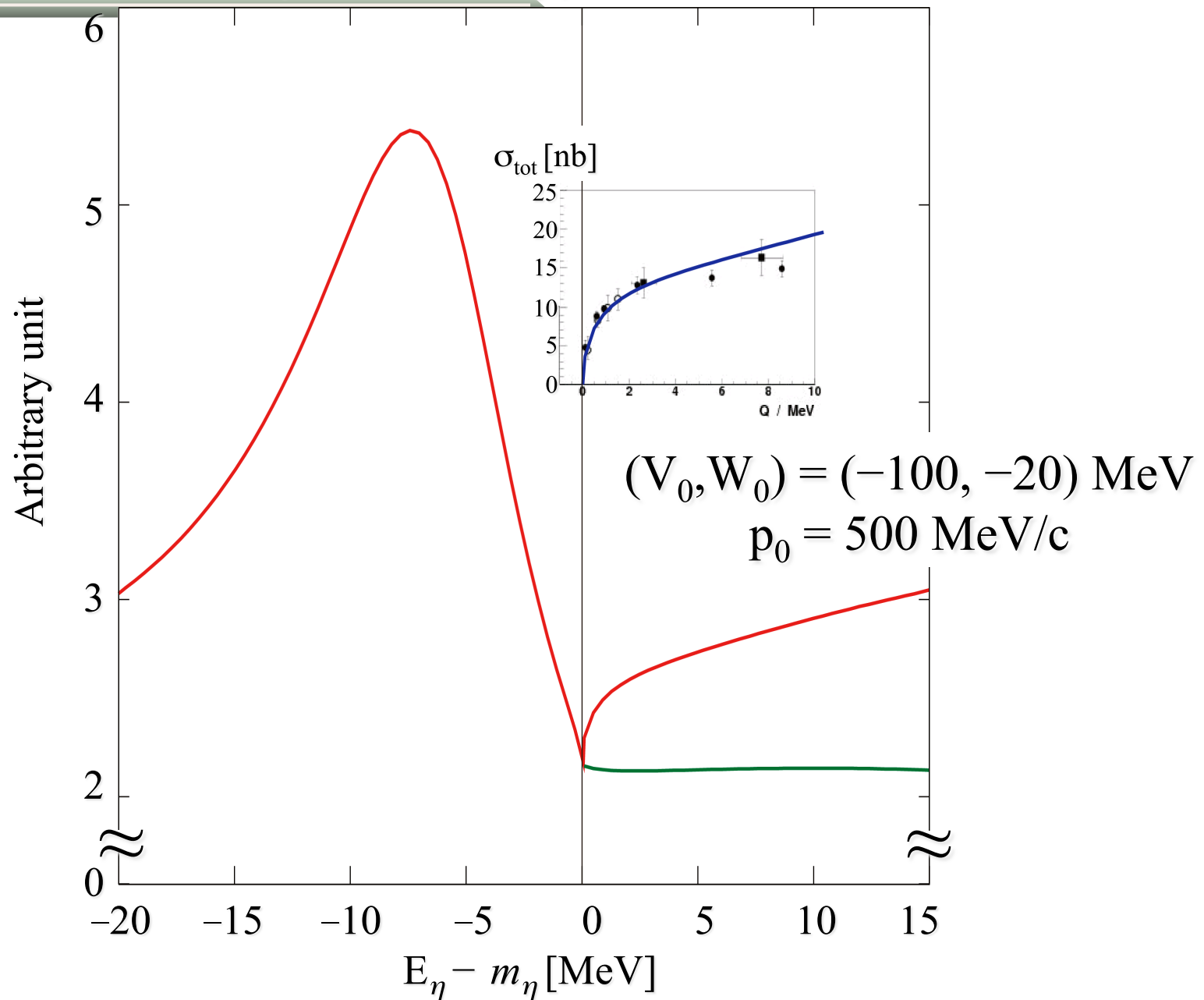


R.Frascaria et al., Rhys.Rev.C50 (1994) 573,
N. Wills et al., Phys. Lett. B 406 (1997) 14,
A. Wronska et al., Acta. Phys. Pol. 56 (2006) 279.

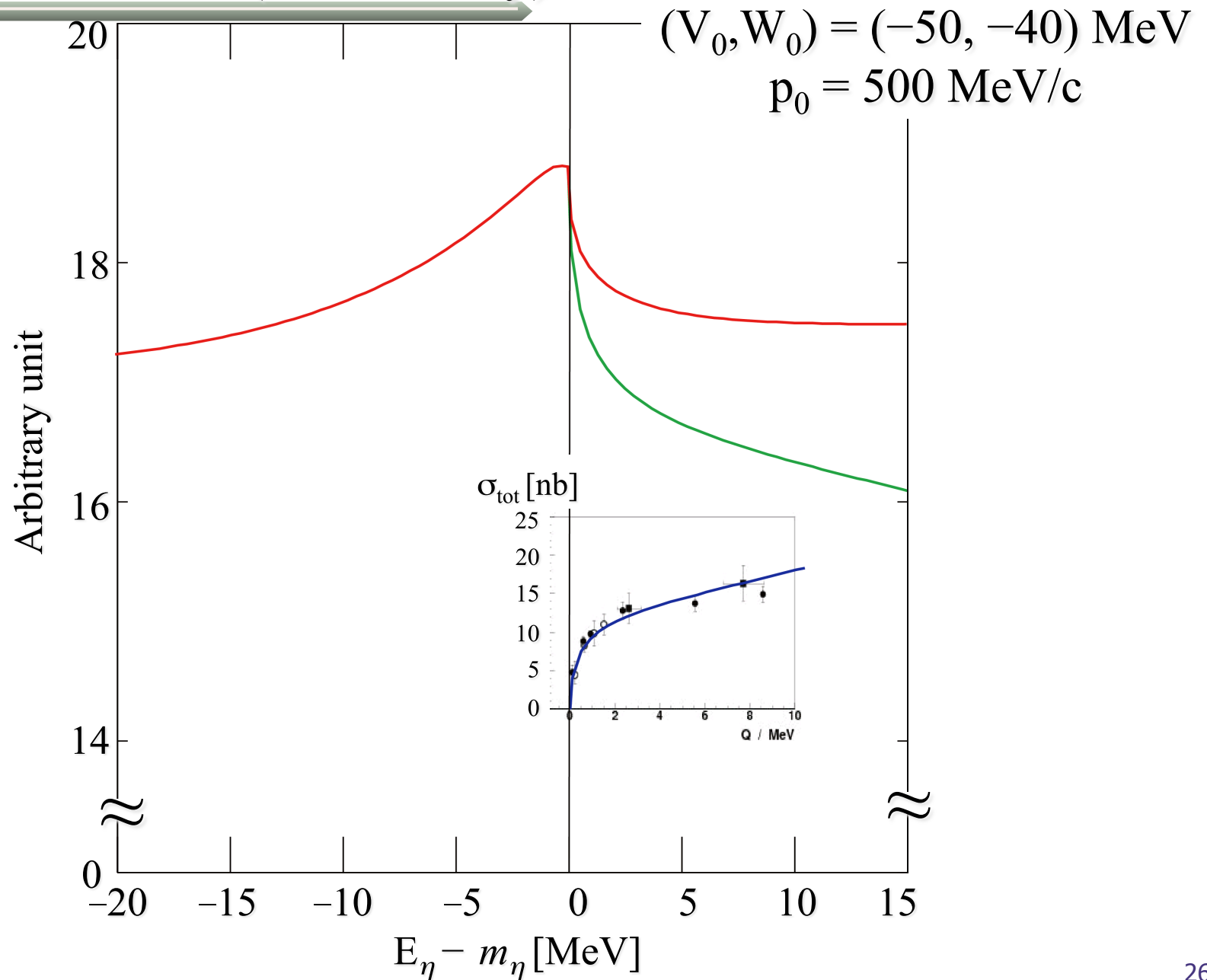
$\sigma(dd \rightarrow ^4\text{He}\eta)$ data



Numerical Results (Preliminary)



Numerical Results(Preliminary)



Summary

- Recent results on Formation of η mesic nucleus
 - » (π, p) reaction
 - » $d + d \rightarrow (^4\text{He}-\eta) \rightarrow p + \pi^- + 3\text{He}$ reaction

- Some indications by different Chiral models
for (π, p) reaction

- New Experiments
 - » Fujioka, Itahashi, ... @ J-PARC
 - » $d + d$; COSY Proposal 186.2

