

11th International Workshop On Meson Production, Properties And Interaction (MESON 2010)

Measurements of τ Decays into Kaons at BaBar and Determination of $|V_{us}|$

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Outline

- τ Physics at BaBar
- Theoretical overview
- Experimental determination of $|V_{us}|$
 - from inclusive $\tau \rightarrow s$ decays
 - from the ratio $\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$
- Conclusion

τ Physics at BaBar

BaBar is a τ factory:

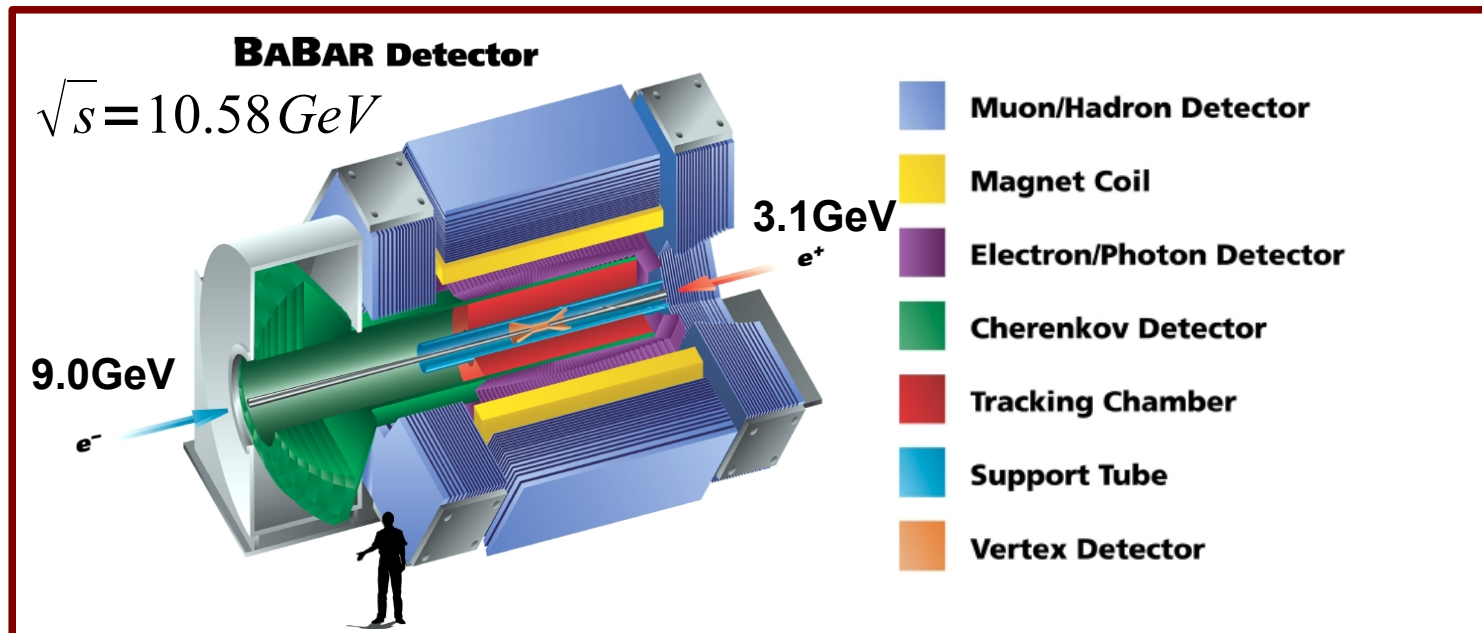
$$\sigma_{\tau\tau} = 0.9 \text{ nb}, (\sigma_{\text{BB}} = 1.1 \text{ nb})$$

$$\mathcal{L} = 531 \text{ fb}^{-1}$$

→ 488 million $\tau\tau$ pairs

Areas of τ Physics with recent results:

- precise τ branching fractions
- τ mass
- constraints on Lepton Flavor Violation
- $|V_{us}|$ from strange τ decays



CKM Matrix element $|V_{us}|$

- Cabibbo-Kobayashi-Maskawa Matrix

$$\begin{pmatrix} V_{ud} & \boxed{V_{us}} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- Unitarity condition:

$$|V_{ud}|^2 + |V_{ub}|^2 + |V_{us}|^2 = 1$$

negligibly small

$$\begin{aligned} |V_{ud}| &= 0.97425 \pm 0.00022 \\ &\text{(Towner, Hardy 2009)} \\ |V_{ub}| &= (3.93 \pm 0.36) \times 10^{-3} \end{aligned}$$

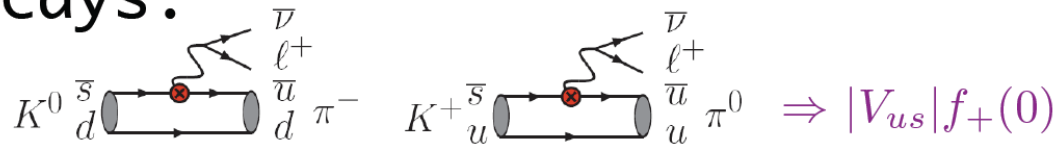

$$\boxed{|V_{us}| = 0.2255 \pm 0.0010}$$

Methods of $|V_{us}|$ determination

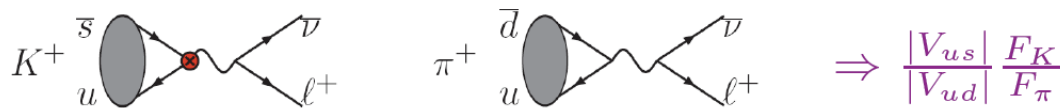
Hyperon decays:



Kl3 decays:

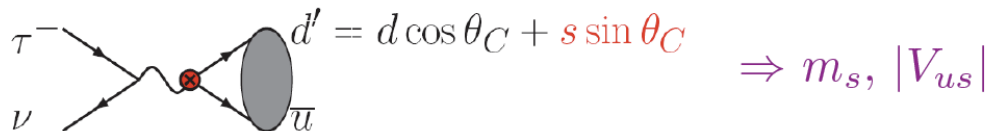


Kl2 decays:



τ decays, kl2-like method: $\frac{BR(\tau \rightarrow K \nu)}{BR(\tau \rightarrow \pi \nu)} \propto \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{F_K^2}{F_\pi^2}$

τ decays:



limited by
theory uncertainty:

$\sigma[f_+(0)] = 0.51\%$
(PRL 100:141601,2008)

$\sigma[F_K/F_\pi] = 0.59\%$
(PRL 100:062002,2008)

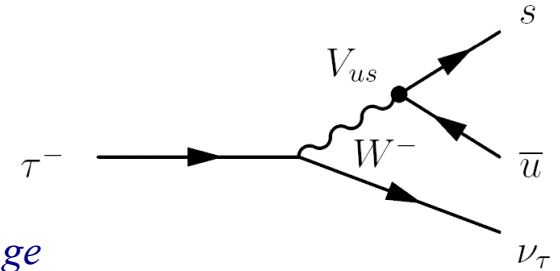
limited by statistical
uncertainty

$|V_{us}|$ theory uncertainty
estimate: 0.23%
(PoSKAON:008, 2008)

$|V_{us}|$ from inclusive $\tau \rightarrow s$ decays

τ decay rate into hadrons

$$R_\tau = \frac{\Gamma(\tau^- \rightarrow [\text{hadrons}]^- \nu_\tau)}{\Gamma(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)} = R_{\tau, \text{non-strange}} + R_{\tau, \text{strange}}$$



Branching fractions are experimental input for $|V_{us}|$ determination:

$$|V_{us}|^2 = \frac{R_{\tau, \text{strange}}}{\frac{R_{\tau, \text{non strange}}}{|V_{ud}|^2} + \delta R_{OPE}}$$

δR is a SU(3) symmetry breaking correction, obtained from OPE/FESR, small; $< 0.1 \cdot R_{\tau, \text{ns}} / |V_{ud}|^2$

OPE = Operator Product Expansion
FESR = Finite Energy Sum Rules

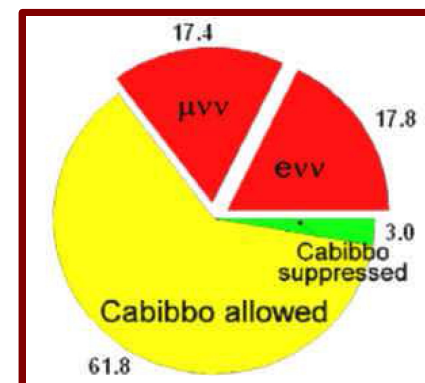
(Gamiz et al., 2007)

Strange τ Decays

Decay	$\mathcal{B}_{PDG2009}[\%]$			$\frac{\Delta\mathcal{B}}{\mathcal{B}}[\%]$
$\tau^- \rightarrow K^- \nu_\tau$	0.685	$\pm$	0.023	3.4
$(\tau^- \rightarrow K^- \nu_\tau \text{ [indirect]})$	0.715	$\pm$	0.004	0.6)
$\tau^- \rightarrow K^- \pi^0 \nu_\tau$	0.426	$\pm$	0.016	3.8
$\tau^- \rightarrow K^- \pi^0 \pi^0 \nu_\tau$	0.058	$\pm$	0.024	30
$\tau^- \rightarrow \bar{K}^0 \nu_\tau$	0.831	$\pm$	0.030	5.7
$\tau^- \rightarrow \bar{K}^0 \pi^0 \nu_\tau$	0.360	$\pm$	0.040	11
$\tau^- \rightarrow K^- \pi^- \pi^+ \nu_\tau$	0.280	$\pm$	0.002	0.7
$\tau^- \rightarrow (\bar{K} \pi \pi \pi)^- \nu_\tau \text{ (est'd)}$	0.074	$\pm$	0.030	40
$\tau^- \rightarrow (\bar{K} \pi \pi \pi \pi)^- \nu_\tau \text{ (est'd)}$	0.011	$\pm$	0.007	64
$\tau^- \rightarrow K_1(1270) \nu_\tau \rightarrow K^- \omega$	0.067	$\pm$	0.021	31
$\tau^- \rightarrow K^- \eta \nu_\tau$	0.016	$\pm$	0.001	6.2
$\tau^- \rightarrow K^{*-} \eta \nu_\tau$	0.013	$\pm$	0.002	15
$\tau^- \rightarrow K^- \phi \nu_\tau$	0.0037	$\pm$	0.0003	8.1
Total	2.8247	$\pm$	0.0725	2.6
	(2.8547	$\pm$	0.0689	2.4)

(*) indirect $\tau \rightarrow K \nu$

use precise measurement of $\text{BF}[K \rightarrow \mu \nu(\gamma)]$
to get indirect measurement of $\text{BF}[\tau \rightarrow K \nu(\gamma)]$
Rev.Mod.Phys. 78 1043 (2006)

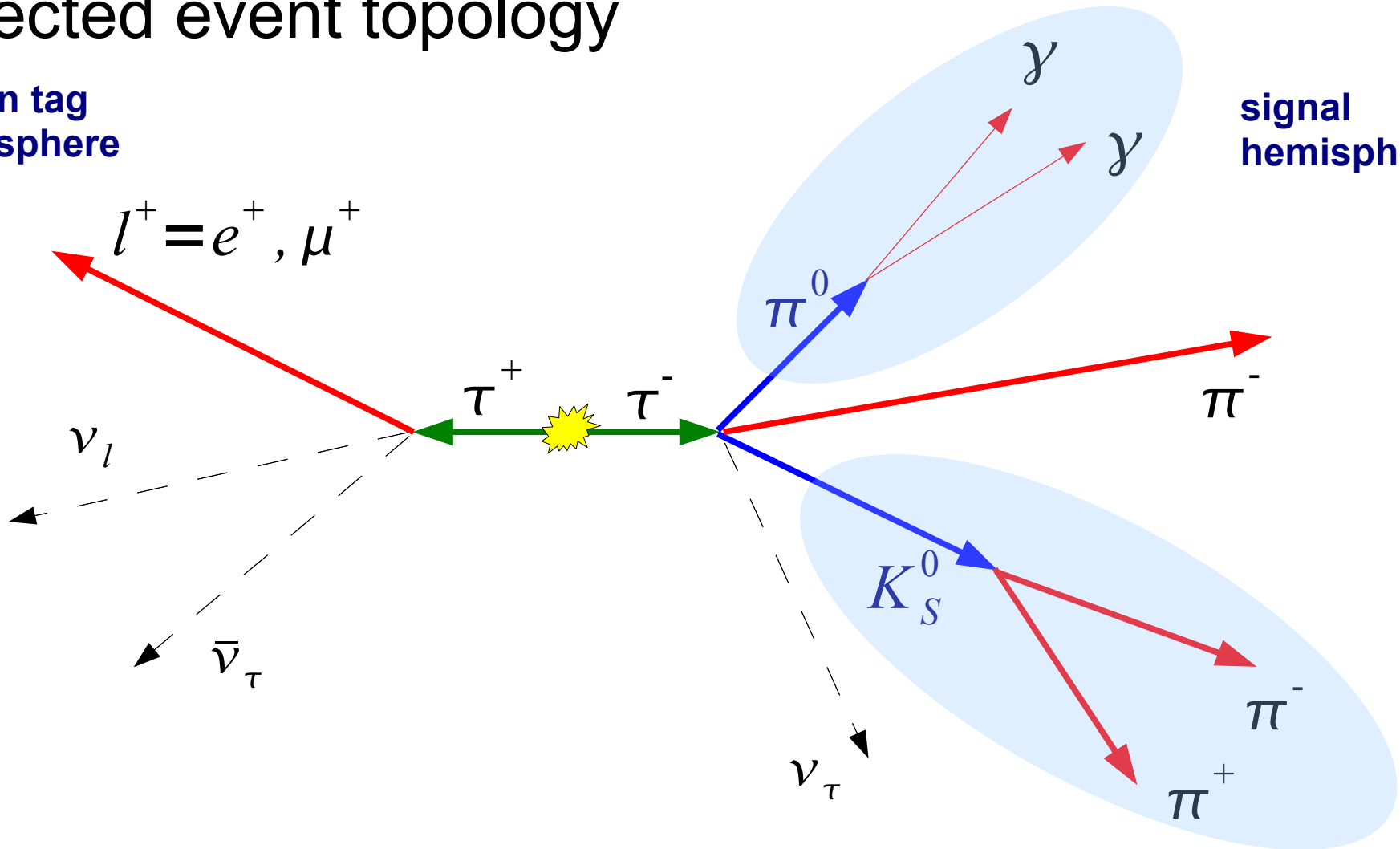


Measurement of $\tau \rightarrow K_s^0 \pi \pi^0 \nu_\tau$

Selected event topology

lepton tag
hemisphere

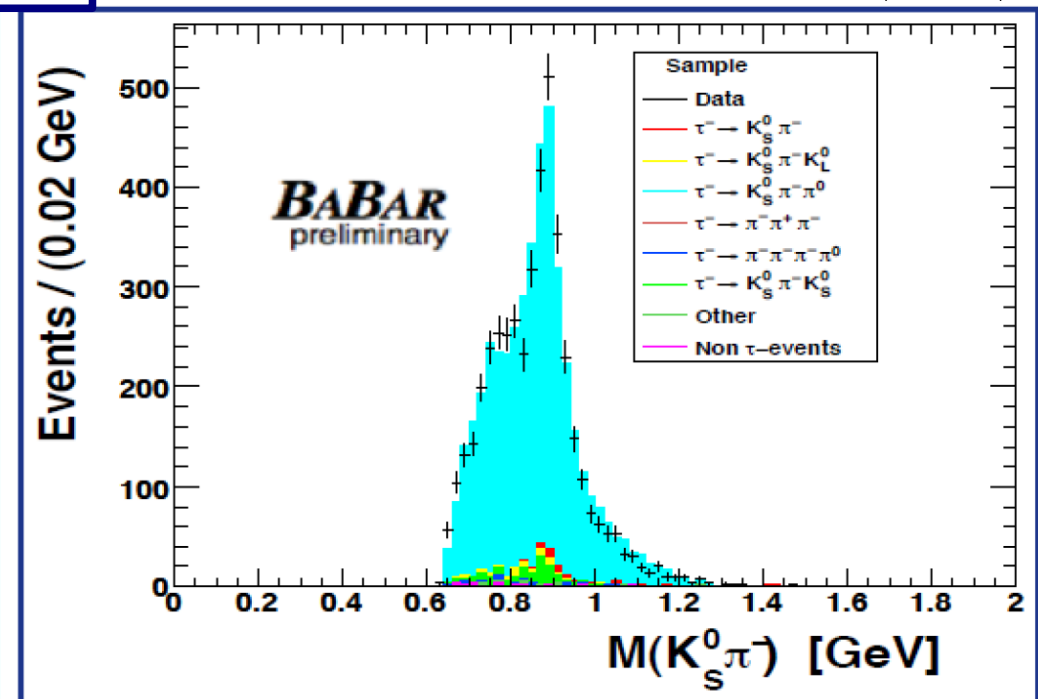
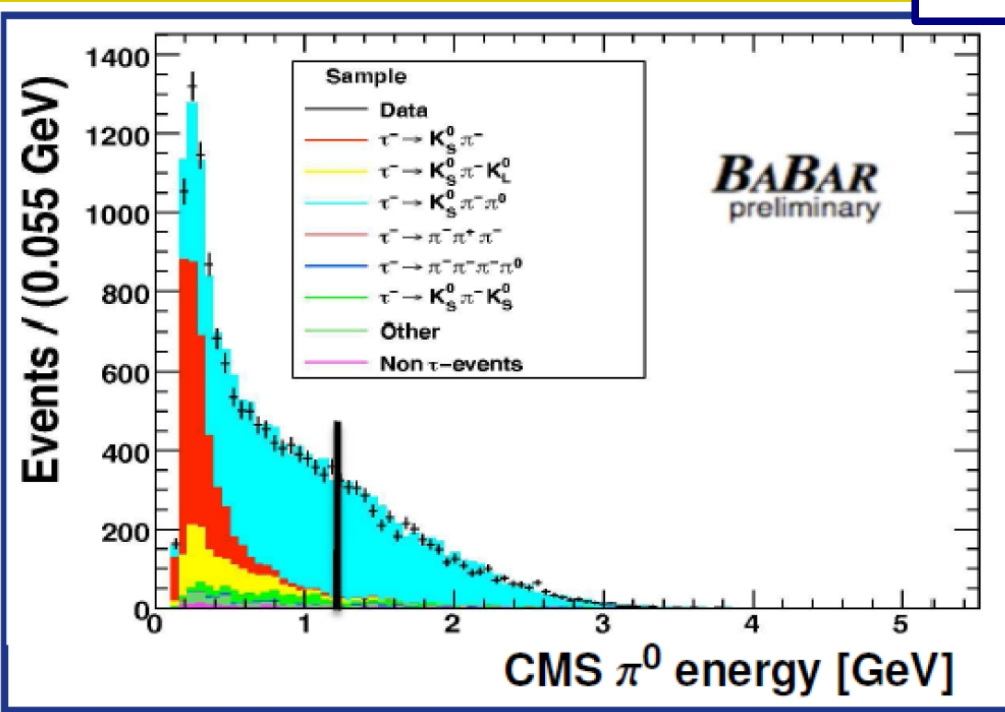
signal
hemisphere



red arrows: particles reconstructed with the BaBar detector



Measurement of $\tau \rightarrow K_s^0 \pi \pi^0 \nu_\tau$

384 fb⁻¹

- lepton tag on signal side
- high π^0 energy required in CMS
→ high purity (93%)
- π^0 trajectory within 90° of $K_s^0 \pi$ momentum

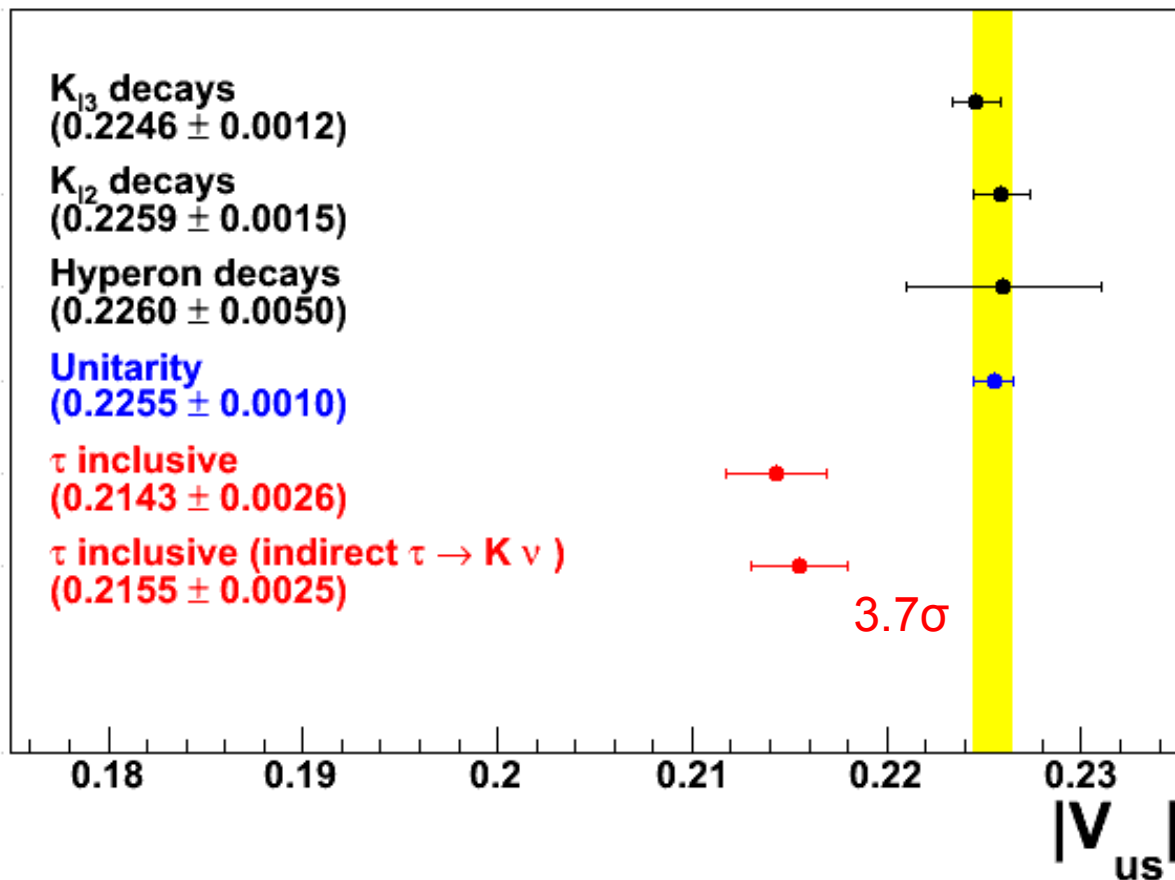
- τ Monte Carlo hadronic mass distribution tuned with data
- Dominant systematic uncertainty:
→ π^0 reconstruction efficiency (0.011%, rel. 3.2%)

BABAR
preliminary

$$BF(\tau \rightarrow K_s^0 \pi \pi^0 \nu_\tau) = [0.342 \pm 0.006(stat.) \pm 0.015(syst.)] \%$$

$\sigma_{rel.} 4.7\%$

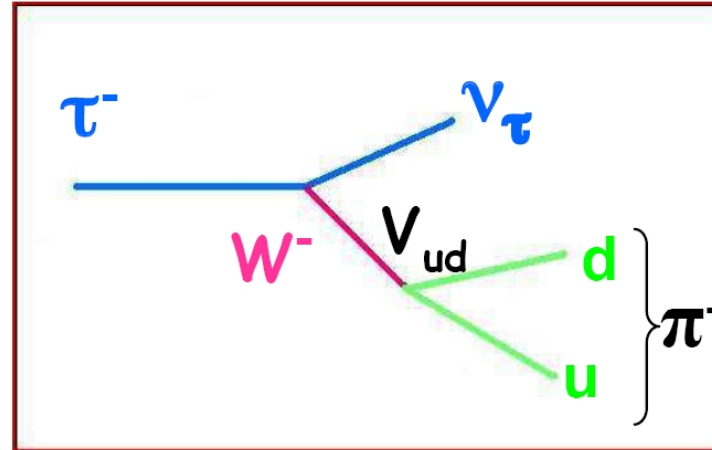
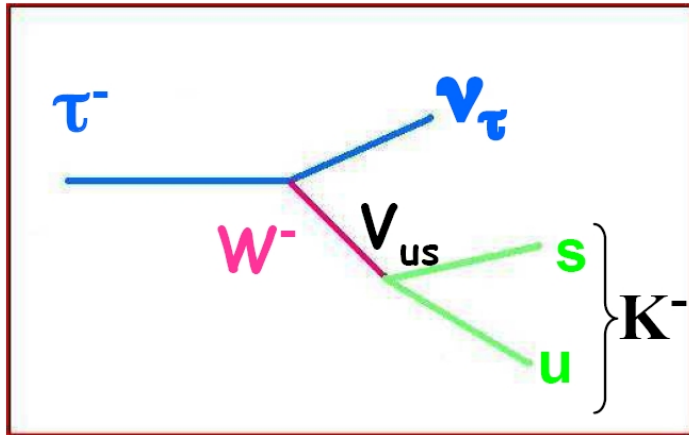
$|V_{us}|$ from inclusive $\tau \rightarrow s$



- $|V_{us}|$ from K,Hyp,Uni.
(A.Denig Chiral2009)
- $m_s(2\text{GeV}) = 94 \pm 6 \text{ MeV}$
(M.Jamin et al., 2006)
- $\delta R_{\text{OPE}} = 0.240 \pm 0.032$
(Gamiz et al., 2007)
- V_{ud} (Towner, Hardy 2009)
- $\text{BF}(\tau \rightarrow s)$ from PDG2009
→ update with new
 $\text{BF}(\tau \rightarrow K_s^0 \pi \pi^0 \nu_\tau)$

$|V_{us}|$ precision:
 → before update: 1.31%
 → Now: 1.15%

$|V_{us}|$ from ratio $\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$



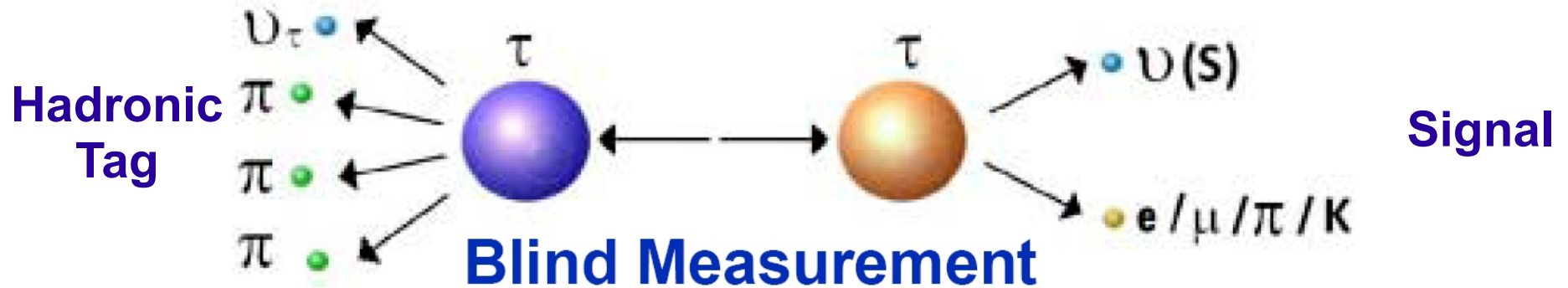
$$\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_K^2}{f_\pi^2} \left(\frac{1 - m_K^2/m_\tau^2}{1 - m_\pi^2/m_\tau^2} \right)^2 (1 + \delta_{LD}^\tau)$$

- δ_{LD} long distance electroweak correction
(short distance correction cancel) (arXiv:0402299)
- $|V_{ud}|$ from super allowed beta decays (Towner, Hardy 2009)
- ratio f_K^2/f_π^2 from lattice QCD (E. Follana et al. PRL 100)

Measurement of $\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$

Select $\tau\tau$ events with

- one τ decaying into 3 charged pions and neutrino (hadronic tag)
- the other τ into the signal decay

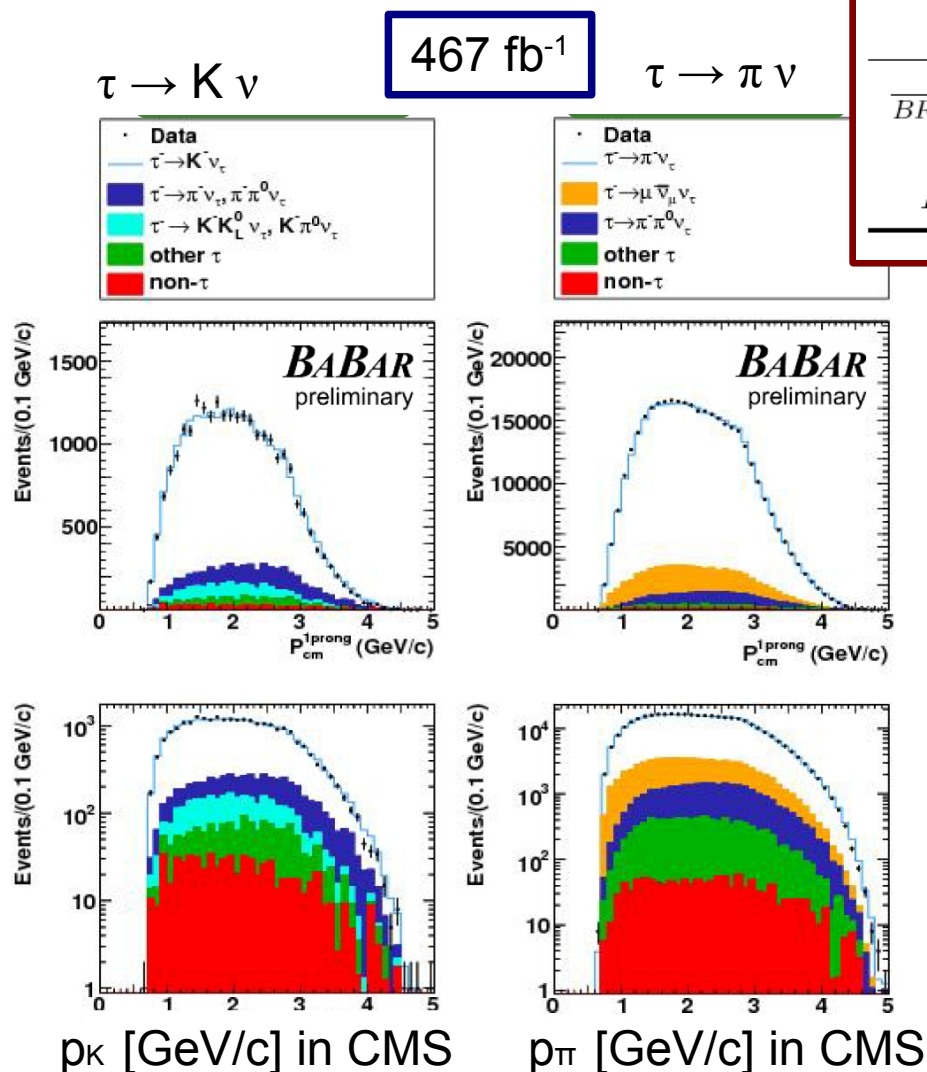


$$\text{Measure: } \frac{BF(\tau^- \rightarrow \pi^- \nu_\tau)}{BF(\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e)} \quad \frac{BF(\tau^- \rightarrow K^- \nu_\tau)}{BF(\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e)} \quad \boxed{\frac{BF(\tau^- \rightarrow K^- \nu_\tau)}{BF(\tau^- \rightarrow \pi^- \nu_\tau)}}$$

- Systematic effects cancel in the ratios
(e.g. uncertainties of efficiencies, luminosity)



$$\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$$ results



Decay	$\tau \rightarrow K \nu_\tau$	$\tau \rightarrow \pi \nu_\tau$
$\frac{BF}{BF(\tau \rightarrow e \nu_\tau \bar{\nu}_e)}$	$0.03883 \pm 0.00032 \pm 0.00057$	$0.5945 \pm 0.0014 \pm 0.0061$
BF	$(0.692 \pm 0.006 \pm 0.010)\%$	$(10.59 \pm 0.03 \pm 0.11)\%$
BF_{PDG}	$(0.685 \pm 0.023)\%$	$(10.828 \pm 0.105)\%$

$$\frac{B(\tau^- \rightarrow K^- \nu_\tau)}{B(\tau^- \rightarrow \pi^- \nu_\tau)} = (6.531 \pm 0.056 \pm 0.093) \times 10^{-2}$$

Systematic uncertainties:	$B(\pi)/B(e)$	$B(K)/B(e)$
Particle ID	0.51	0.94
Detector response	0.64	0.54
Backgrounds	0.44	0.85
Trigger	0.10	0.10
$\pi^- \pi^- \pi^+$ modelling	0.07	0.27
Radiation	0.10	0.04
$\mathcal{B}(\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau)$	0.15	0.40
$\mathcal{L} \sigma_{e^+ e^- \rightarrow \tau^+ \tau^-}$	0.39	0.20
Total [%]	1.0	1.5

next
slide

PID uncertainty in $\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$ analysis

One of the dominant systematic effects: charged particle identification

- PID algorithm performance is studied using control samples
- PID algorithm is applied to unbiased track of known type to determine the efficiency in data and simulation: differences are corrected

Kaon and pion identification

- Studied using two independent control samples

A control pion and a control kaon is kinematically selected in the decay chain:

$$D^{*+} \rightarrow \pi_{soft}^+ D^0$$
$$D^0 (\rightarrow \pi^+ K^-)$$

- control pion has same charge as soft π
- control kaon has opposite charge as soft π

Additional cross check:

τ decays in 3 charged tracks

- determine particle ID of two tracks
- 3rd track is control pion/kaon

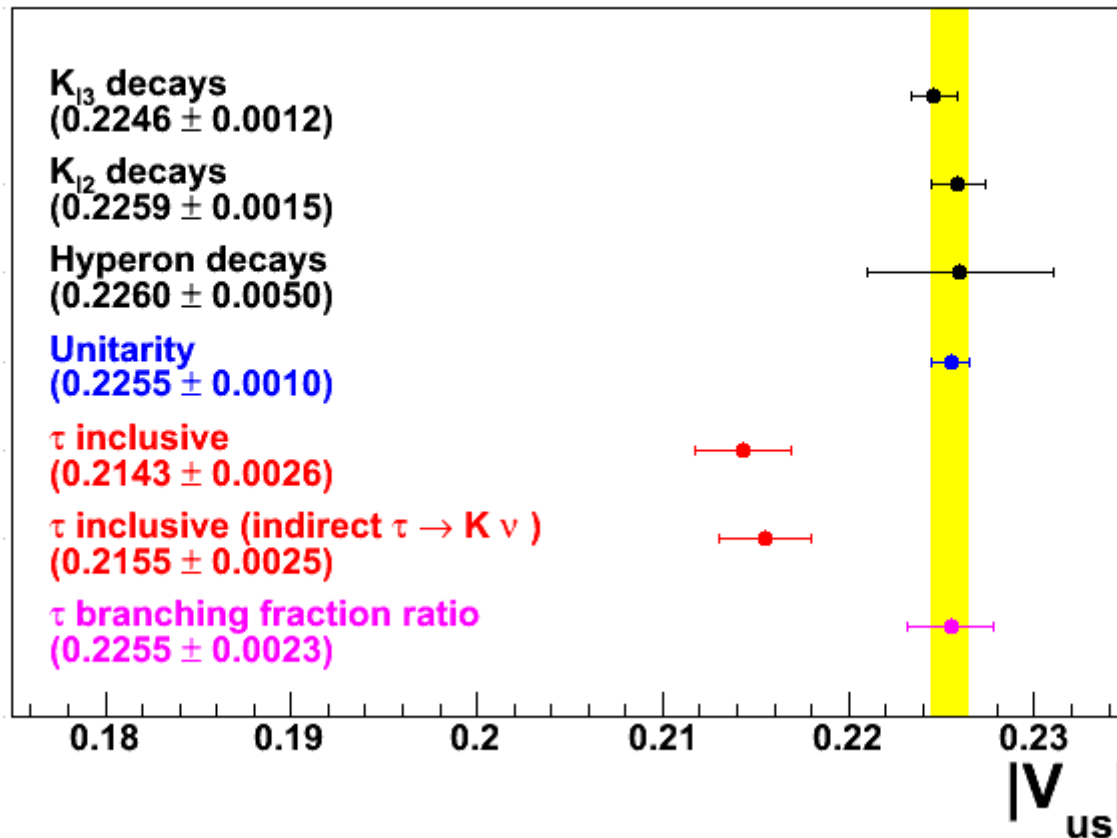
Pion control sample: $\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$

Kaon control sample: $\tau^- \rightarrow K^- \pi^- K^+ \nu_\tau$

Electron and Muon identification: Bhabha and radiative μ -pair control samples

→ e/ μ / π /K PID efficiency uncertainties are combined to a total PID uncertainty (previous slide)

$|V_{us}|$ from $\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$



- $\delta_{LD} = (0.03 \pm 0.44)\%$
(arXiv:0811.1429)
- $|V_{ud}| = 0.97425 \pm 0.00022$
(Towner, Hardy 2009)
- $f_K / f_\pi = 1.189 \pm 0.007$
(E. Follana et al. PRL 100)

$|V_{us}|$ consistent with unitarity

Conclusion

Unitarity	0.2255 ± 0.0010
inclusive $\tau \rightarrow s$	0.2155 ± 0.0025
$\frac{BF(\tau \rightarrow K \nu)}{BF(\tau \rightarrow \pi \nu)}$	0.2255 ± 0.0023

- $|V_{us}|$ from BF ratio consistent with unitarity.
- $|V_{us}|$ from inclusive $\tau \rightarrow s$ decays: $\sim 3\sigma$ discrepancy from unitarity.

However:

- Program of $\tau \rightarrow s$ measurements not yet completed.
(Only estimates for $\tau^- \rightarrow (\bar{K} \pi \pi \pi)^- \nu_\tau$, $\tau^- \rightarrow (\bar{K} \pi \pi \pi \pi)^- \nu_\tau$).
- Neglected correlations between BF measurements.
→ The recently formed HFAG-tau group is addressing that.
- Theorists are re-examining the FESR calculation of δR .