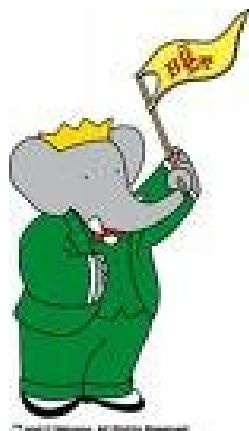


Workshop Meson 2008, Jun 7th 2008

Charmless B Decays

at

BABAR



Alejandro Pérez

LPNHE-IN2P3-CNRS

Universités de Paris VI, Paris VII





Motivation

- Charmless 3 body B decays $K\pi\pi$, $KK\pi$ and KKK
- Spectroscopy: $\pi\pi$, $K\pi$ and KK mass spectra.
- Mainly contributing diagrams: $b \rightarrow s$ loop, $b \rightarrow u$ tree and $b \rightarrow d$ loop. (good place to look for New Physics).
- CKM Physics:
 - ◆ Testing CKM constraints from charmless modes: γ and β measurements.
 - ◆ Compare with global CKM fits.

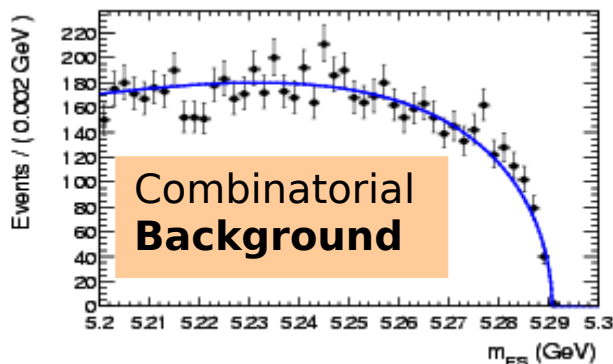
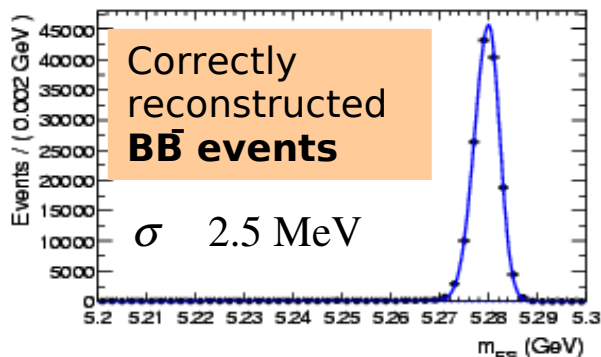


Experimental Issues

- Small S/B ratio, **mostly continuum** ($e^+e^- \rightarrow q\bar{q}$, $q \neq b$) background.
- Use **kinematical** and **event-shape** variables to **discriminate**:

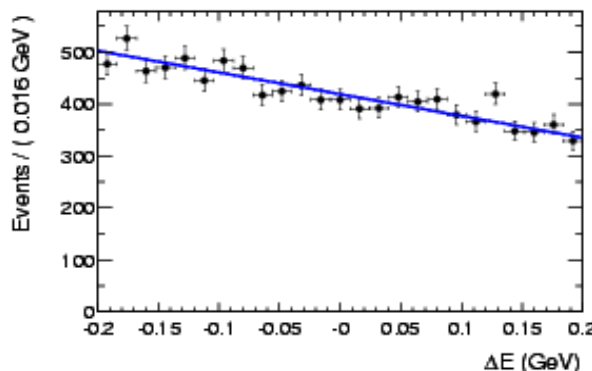
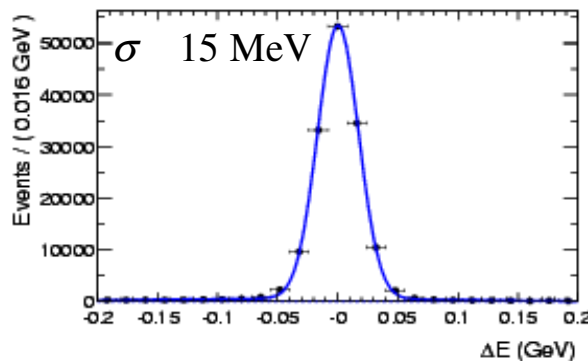
Beam-energy substituted mass

$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$



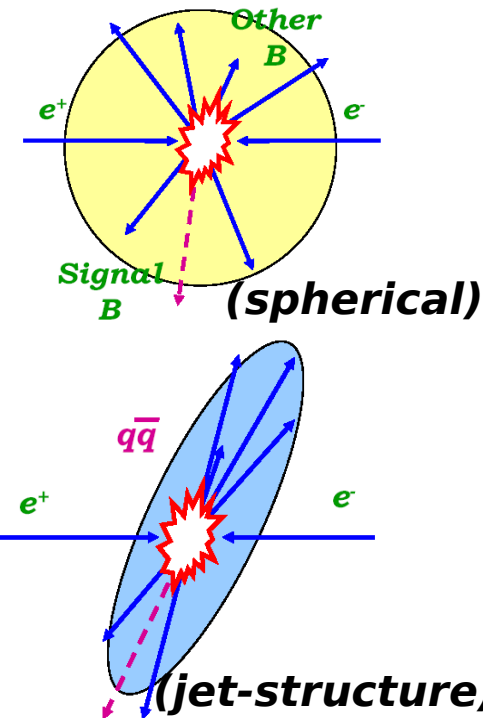
Energy difference

$$\Delta E = E_B^* - E_{beam}^*$$



Event topology

(multivariate methods)





Time-dependent Dalitz Plot Analyses

- Parameterizing signal PDF using Isobar Model

Dalitz Plot

Isobar Model

$$\begin{cases} A(DP) = \sum a_j F_j(DP) \\ \bar{A}(DP) = \sum \bar{a}_j \bar{F}_j(DP) \end{cases}$$

Shapes of intermediates

states over DP

Time-dependent DP PDF

$$f(\Delta t, DP, q_{tag}) \propto (|A|^2 + |\bar{A}|^2) \frac{e^{-|\Delta t|/\tau}}{4\tau} \left(1 + q_{tag} \frac{2 \operatorname{Im}[\bar{A}A^*]}{|A|^2 + |\bar{A}|^2} \sin(\Delta m_d \Delta t) - q_{tag} \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} \cos(\Delta m_d \Delta t) \right)$$

CP violation varies over DP

Complex amplitudes a_j and \bar{a}_j determine DP interference pattern. Module and phase can be directly fitted on data.

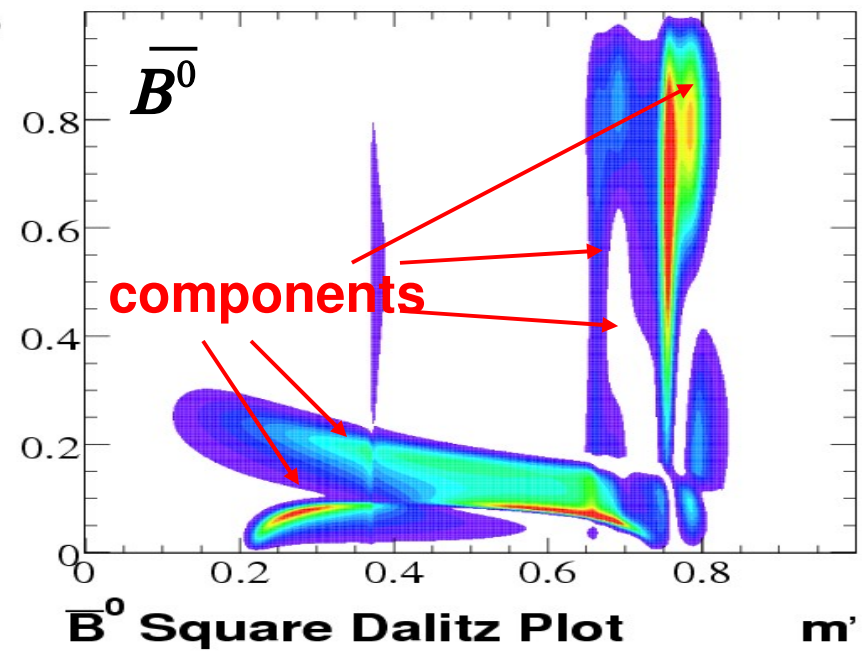
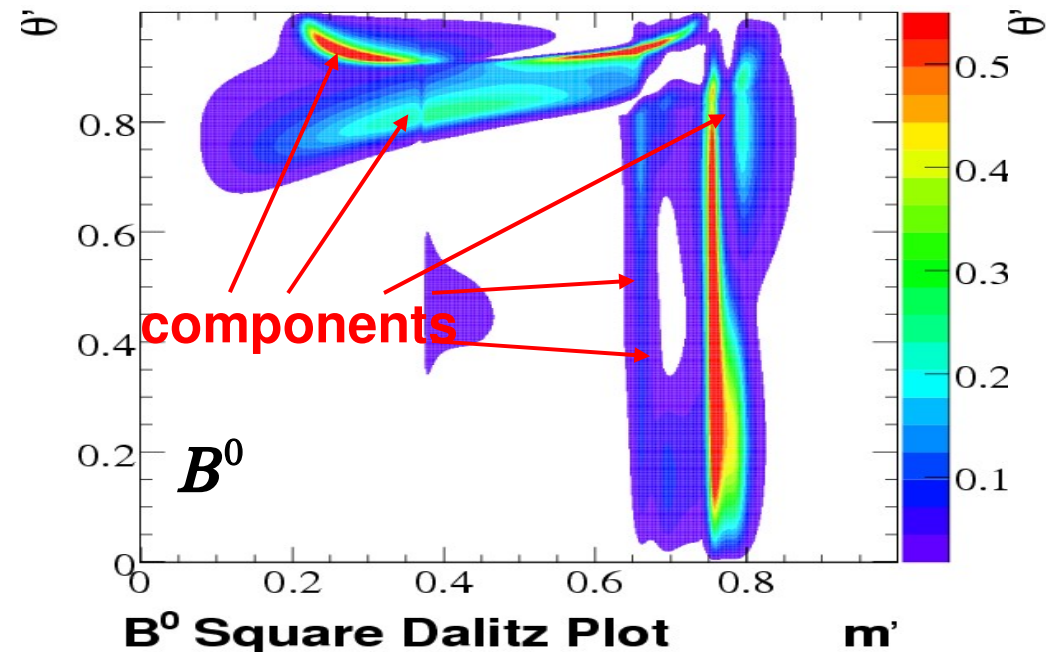
Time-dependent CPV parameters:

$$C_j = \frac{|a_j|^2 - |\bar{a}_j|^2}{|a_j|^2 + |\bar{a}_j|^2} \quad S_j = \frac{2 \operatorname{Im}[a_j \bar{a}_j^*]}{|a_j|^2 + |\bar{a}_j|^2}$$

Interference helps disentangling strong and weak phases and thus raises the degeneracy on the phases.



Time-dependent Dalitz Plot Analyses





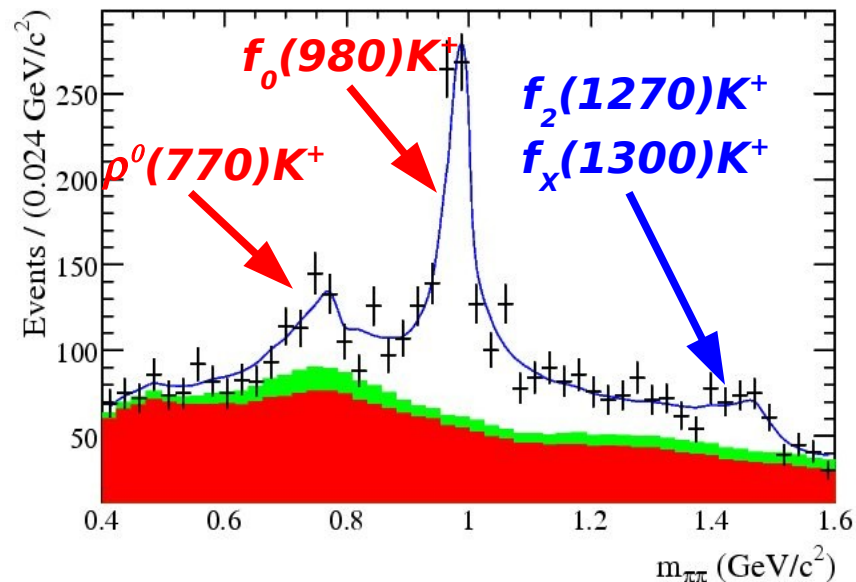
Spectroscopy: $\pi\pi$, $K\pi$ and KK mass spectra



Dalitz analysis of $B^+ \rightarrow K^+ \pi^- \pi^+$

- Some resonances are wide, they overlap and interfere (e.g. $\rho^0 K^+$ and $f_0 K^+$) $\Rightarrow B^+ \rightarrow K^+ \pi^- \pi^+$ Dalitz-plot (DP) analysis (time-integrated) is needed: magnitudes and relative phases of amplitudes are directly fitted.
- Sensitive to DCPV in decay rate asymmetry and in relative phase asymmetry.
- Largest S/B ratio among $B \rightarrow K \pi \pi$ decays \Rightarrow Used to study $\pi\pi$ and $K\pi$ mass spectra.

- $\pi\pi$ mass spectrum: use $f_0(980)K^+$, $\rho^0(770)K^+$, $f_2(1270)K^+$ and a scalar $f_x(1300)K^+$ with
$$\begin{cases} m = 1479 \pm 8 \text{ MeV}/c^2 \text{ and} \\ \Gamma = 80 \pm 19 \text{ MeV}/c^2 \end{cases}$$





Dalitz analysis of $B^+ \rightarrow K^+ \pi^- \pi^+$

- Some resonances are wide, they overlap and interfere
(e.g. $\rho^0 K^+$ and $f_0 K^+$) \Rightarrow $B^+ \rightarrow K^+ \pi^- \pi^+$ Dalitz-plot (DP) analysis (time-integrated) is needed: magnitudes and relative phases of amplitudes are directly fitted.
- Sensitive to DCPV in decay rate asymmetry and in relative phase asymmetry.
- Largest S/B ratio among $B \rightarrow K \pi \pi$ decays \Rightarrow Used to study $\pi\pi$ and $K\pi$ mass spectra.

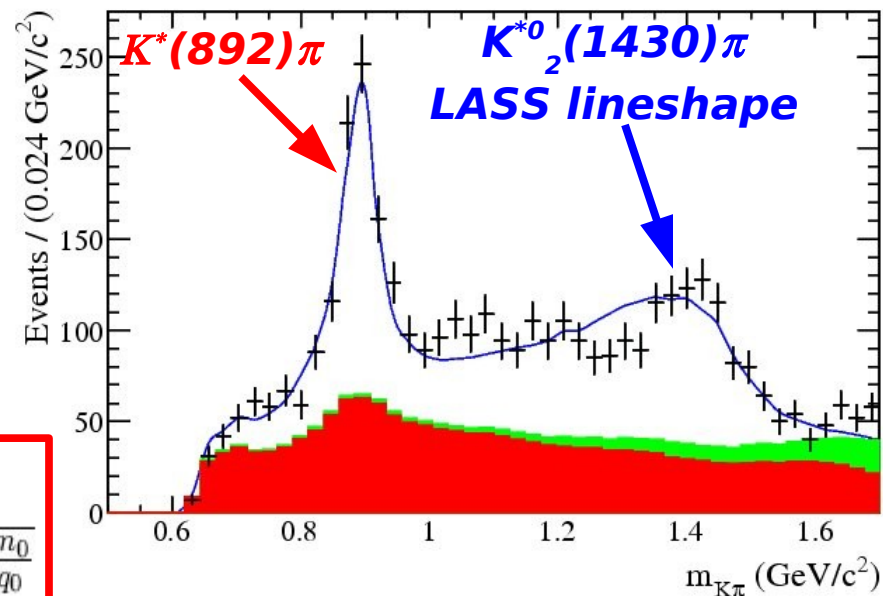
- $K\pi$ mass spectrum: use

$K^{*0}(892)$, $K^{*0}_2(1430)$

LASS lineshape used for describing $K\pi$ S-wave.

Nucl. Phys., B296:493, 1988

$$R_j(m_{K\pi}) = \frac{m_{K\pi}}{q \cot \delta_B - iq} + e^{2i\delta_B} \frac{m_0 \Gamma_0 \frac{m_0}{q_0}}{(m_0^2 - m_{K\pi}^2) - im_0 \Gamma_0 \frac{q}{m_{K\pi}} \frac{m_0}{q_0}}$$



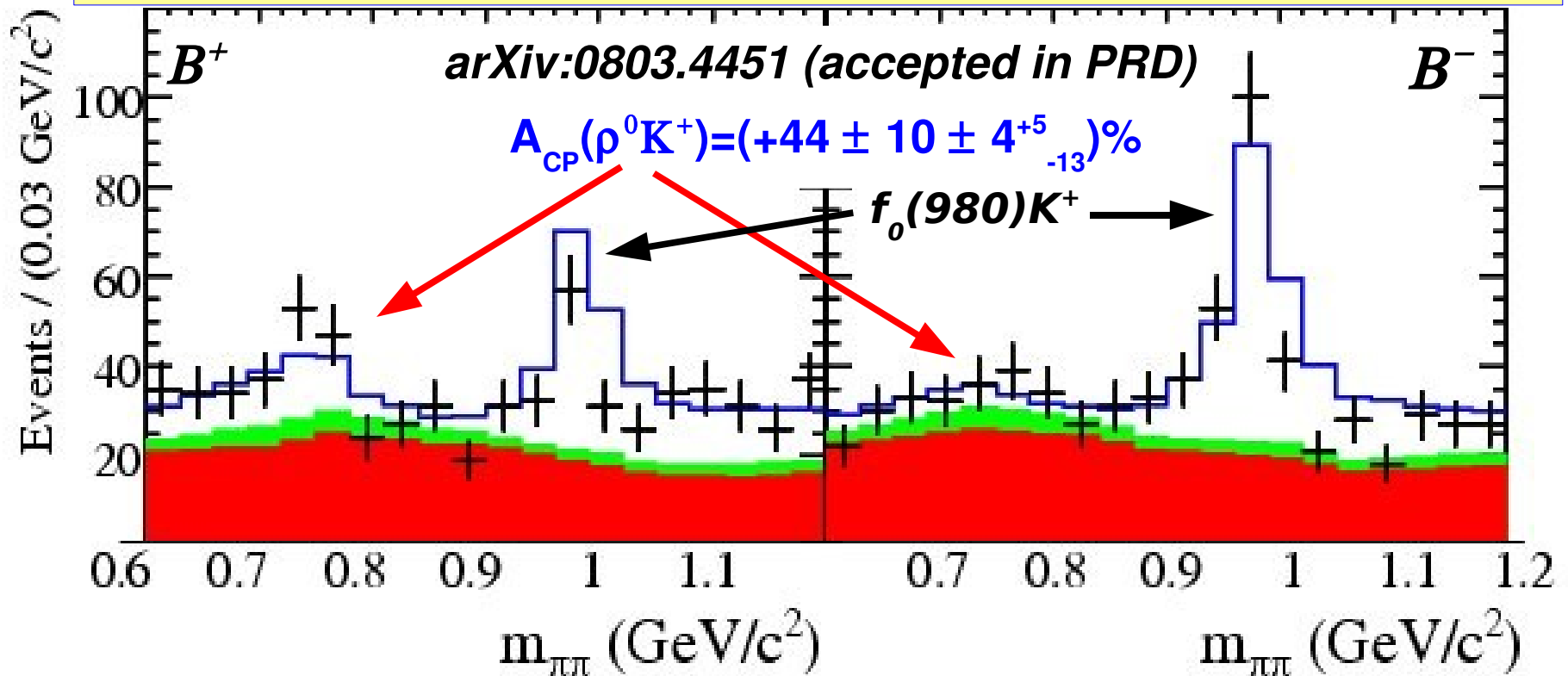


Dalitz analysis of $B^+ \rightarrow K^+ \pi^- \pi^+$

- Some resonances are wide, they overlap and interfere
(e.g. $\rho^0 K^+$ and $f_0 K^+$) $\Rightarrow B^+ \rightarrow K^+ \pi^- \pi^+$ Dalitz-plot (DP) analysis (time-integrated) is needed: magnitudes and relative phases of amplitudes are directly fitted.

- Sensitive to DCPV in decay rate asymmetry and in relative phase asymmetry

- $A_{CP}(K^0 \pi^+) \sim 0$ (as expected in SM).
- Evidence of DCPV in decay rate and relative phase for $B^+ \rightarrow \rho^0 K^+$ at 3.7σ

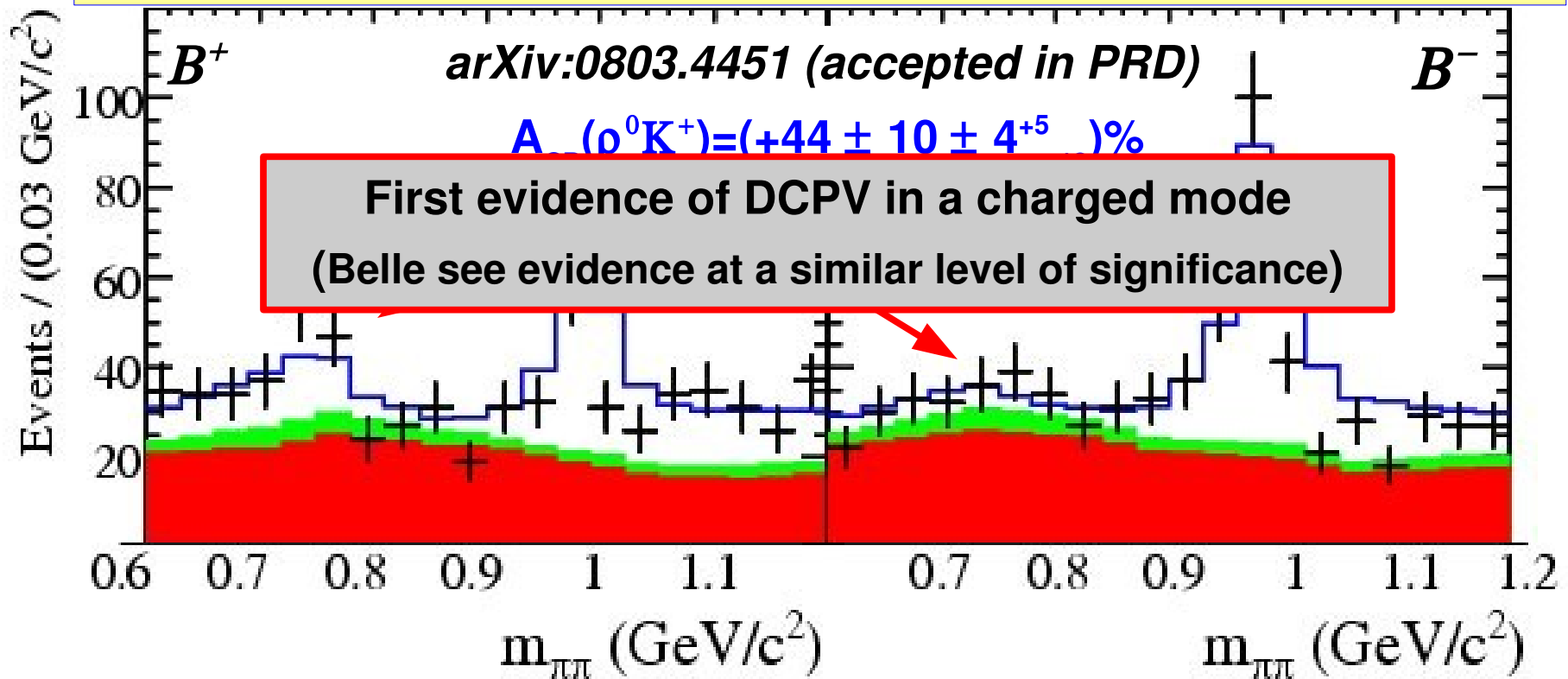




Dalitz analysis of $B^+ \rightarrow K^+ \pi^- \pi^+$

- Some resonances are wide, they overlap and interfere
(e.g. $\rho^0 K^+$ and $f_0 K^+$) $\Rightarrow B^+ \rightarrow K^+ \pi^- \pi^+$ Dalitz-plot (DP) analysis (time-integrated) is needed: magnitudes and relative phases of amplitudes are directly fitted.
- Sensitive to DCPV in decay rate asymmetry and in relative phase asymmetry

- $A_{CP}(K^0 \pi^+) \sim 0$ (as expected in SM).
- Evidence of DCPV in decay rate and relative phase for $B^+ \rightarrow \rho^0 K^+$ at 3.7σ



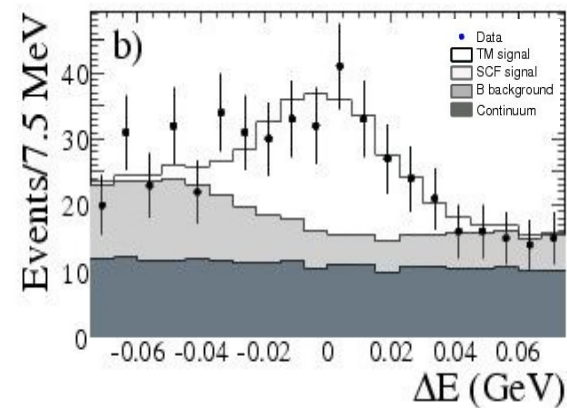
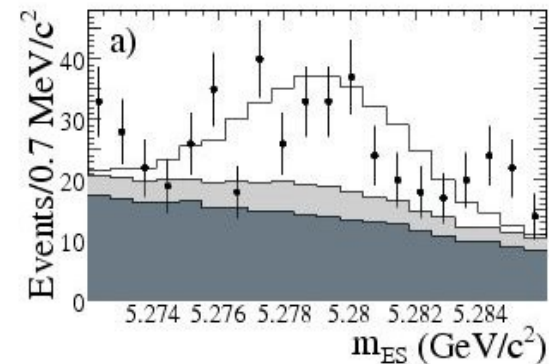


KK S-wave from $K^+K^-\pi^+$ & $K^+K^-K^0$

Observation of $B^+ \rightarrow K^+K^-\pi^+$ at 9.6σ :

$$BR = (5.0 \pm 0.5 \pm 0.5) \times 10^{-6}$$

(429 \pm 43 events)





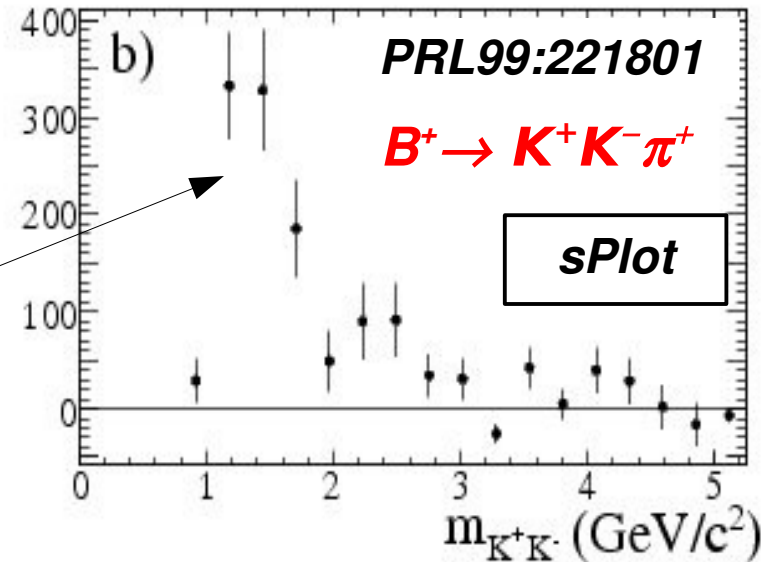
KK S-wave from $K^+K^-\pi^+$ & $K^+K^-K^0$

- Observation of $B^+ \rightarrow K^+K^-\pi^+$ at 9.6σ :

$$BR = (5.0 \pm 0.5 \pm 0.5) \times 10^{-6}$$

(429 ± 43 events)

- Broad peak at $\sim 1.5 \text{ GeV}/c^2$ in KK mass
- $\phi(\overline{ss}) \rightarrow$ peak not seen
(as expected in SM)





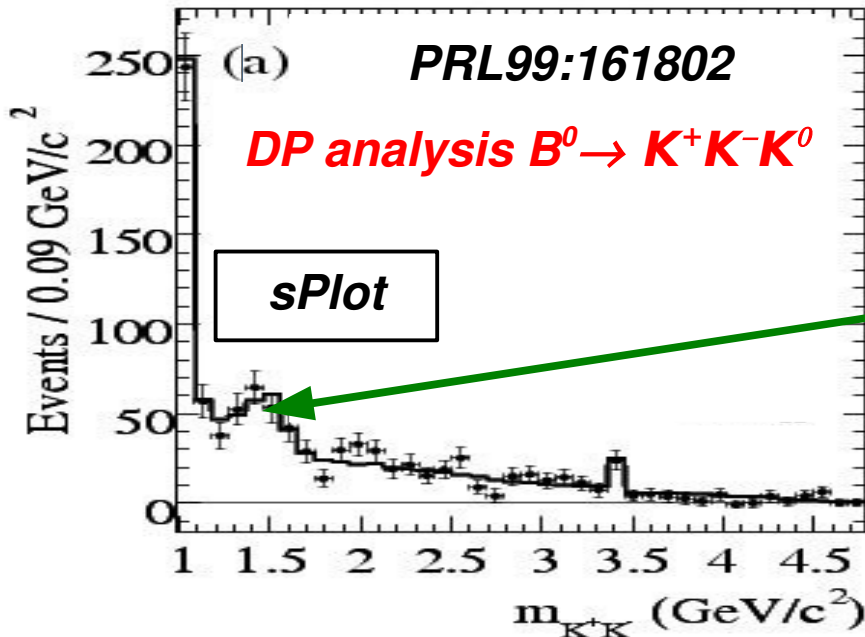
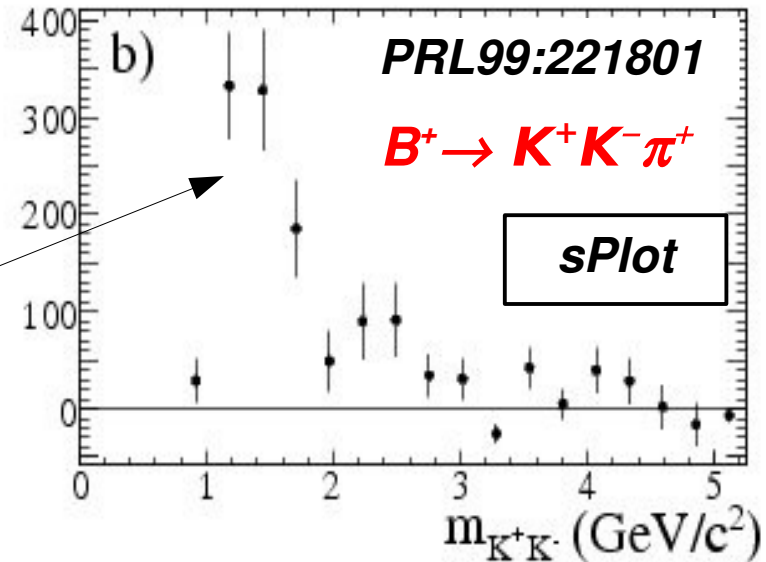
KK S-wave from $K^+K^-\pi^+$ & $K^+K^-K^0$

- Observation of $B^+ \rightarrow K^+K^-\pi^+$ at 9.6σ :

$$BR = (5.0 \pm 0.5 \pm 0.5) \times 10^{-6}$$

(429 ± 43 events)

- Broad peak at $\sim 1.5 \text{ GeV}/c^2$ in KK mass
- $\phi(\overline{ss}) \rightarrow$ peak not seen
(as expected in SM)



- Broad peak at $\sim 1.5 \text{ GeV}/c^2$ in KK (scalar) also seen in other modes:

$$B^0 \rightarrow K^+K^-K^0$$

$$m = 1539 \pm 20 \text{ MeV}/c^2, \Gamma = 257 \pm 33 \text{ MeV}/c^2$$

- $B^0 \rightarrow KKK$ modes dominated by non-resonant component

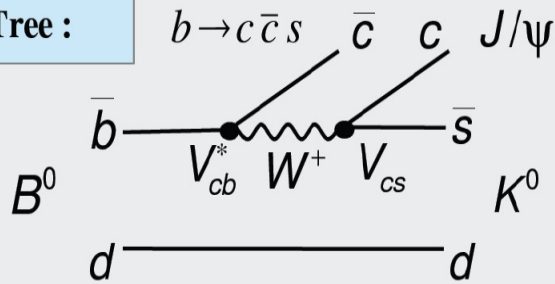


CKM physics: γ and β measurements



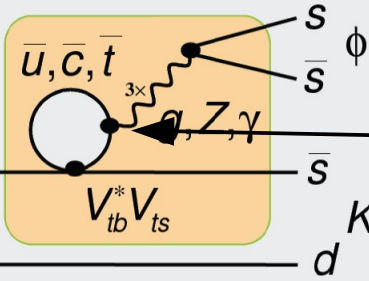
b → sqq̄ penguins: loop-dominance

Tree :



Penguin :

$b \rightarrow s \bar{s} s$



New Physics?

■ b → scc̄:

- “golden” modes for $\sin(2\beta)$, i.e. $J/\psi K_s^0$
- tree-dominated decays
- penguins carry same weak phase

■ b → sqq̄:

- pure “internal” or “flavor-singlet” penguins, i.e. ϕK_s^0
- dominant phase, same CKM factors as $b \rightarrow scc̄$
- BSM particles could contribute in loops
- **A window to New Physics**

Standard Model:

$$S_{scc} = S_{sss} + \Delta S_{SM} = \sin(2\beta)$$

$$C_{scc} \approx C_{sss} \approx 0$$

New Physics:

$$S_{scc} \neq S_{sss} + \Delta S_{SM}$$

$$C_{scc} \neq C_{sss}$$

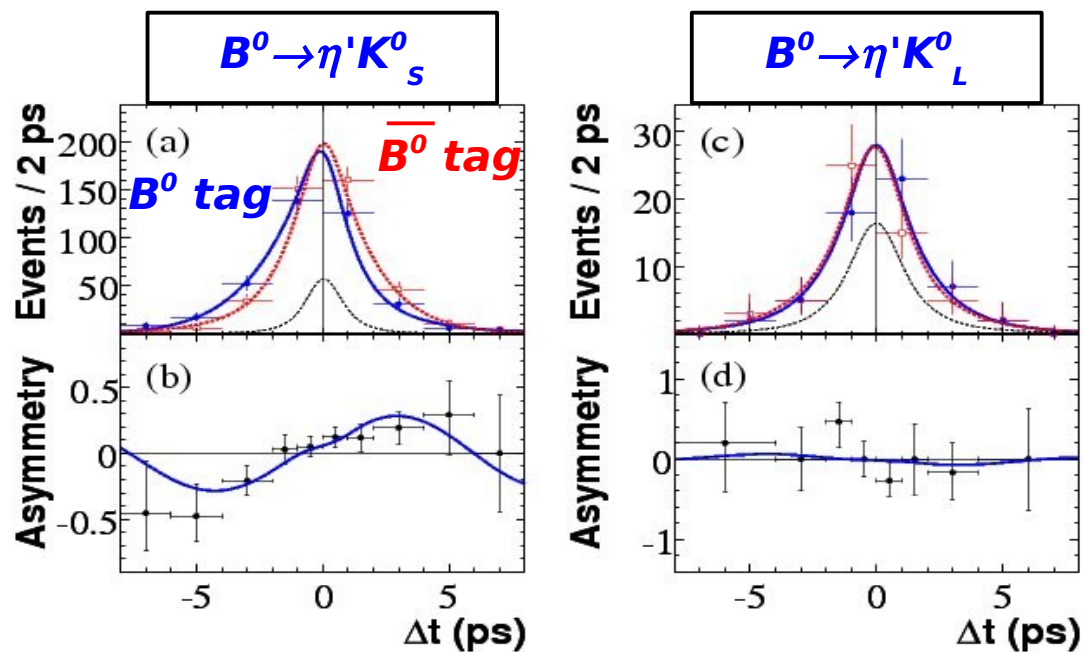
Theoretical issue: evaluate ΔS_{SM} for each mode

identify clean modes (with small ΔS_{SM})



$\sin(2\beta_{\text{eff}})$ from $B^0 \rightarrow \eta' K^0$

- Experimentally clean: largest BR among $b \rightarrow s$ penguin modes
kinematical identification of η'
 $\eta' K^0_L$ adds 50% more events
- Theoretically clean: negligible tree contributions
- First $b \rightarrow sq\bar{q}$ mode to establish CP violation;
results in agreement with $b \rightarrow sc\bar{c}$



PL98:031801 (2007)

Measurements:

$$C = -0.16 \pm 0.07 \pm 0.03$$

$$S = 0.58 \pm 0.10 \pm 0.03$$

Observed mixing-induced
CPV at 5.5σ level

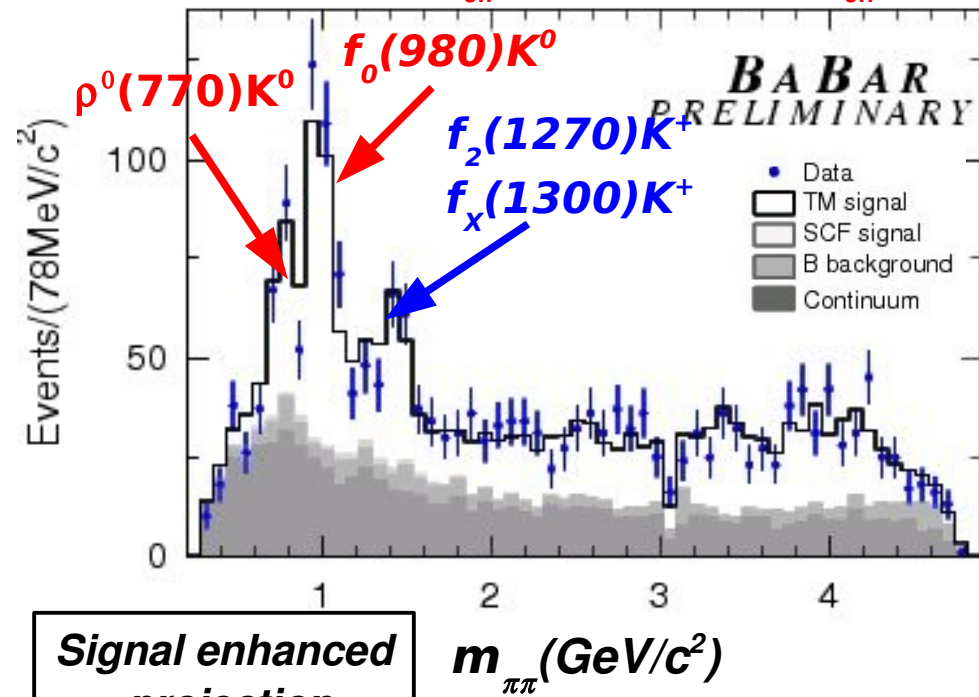


β_{eff} from time-dependent DP analysis: $K^0_S \pi^+ \pi^-$

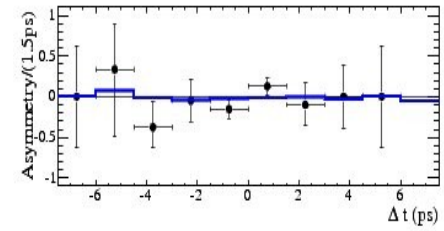
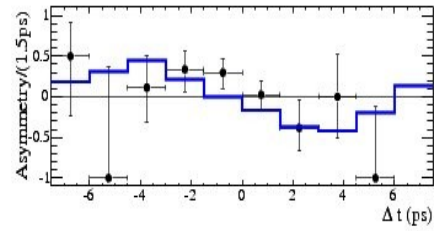
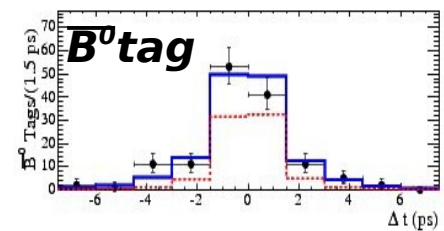
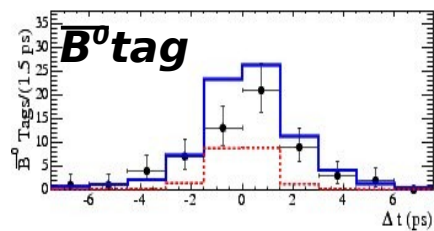
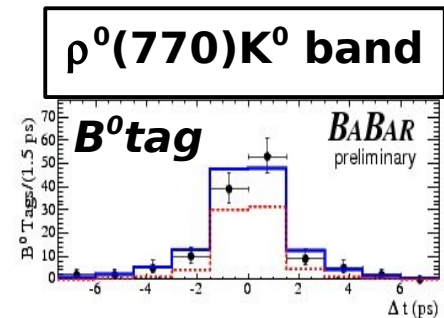
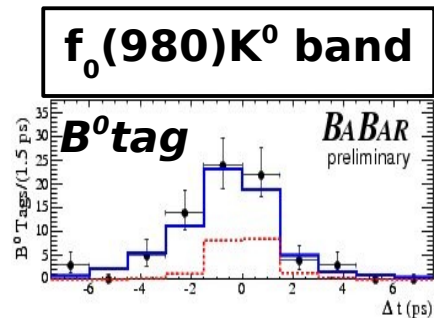
- $\pi\pi$ spectrum: as in $B^+ \rightarrow K^+ \pi^- \pi^+$, $f_2(1270)K^0_S$ and a scalar $f_x(1300)K^0_S$
- Amplitude analysis for $f_0(980)K^0$ and $\rho^0(770)K^0$:

measure of $2\beta_{\text{eff}}$ instead of $\sin(2\beta_{\text{eff}})$

Time dependent asymmetries:



Signal enhanced projection

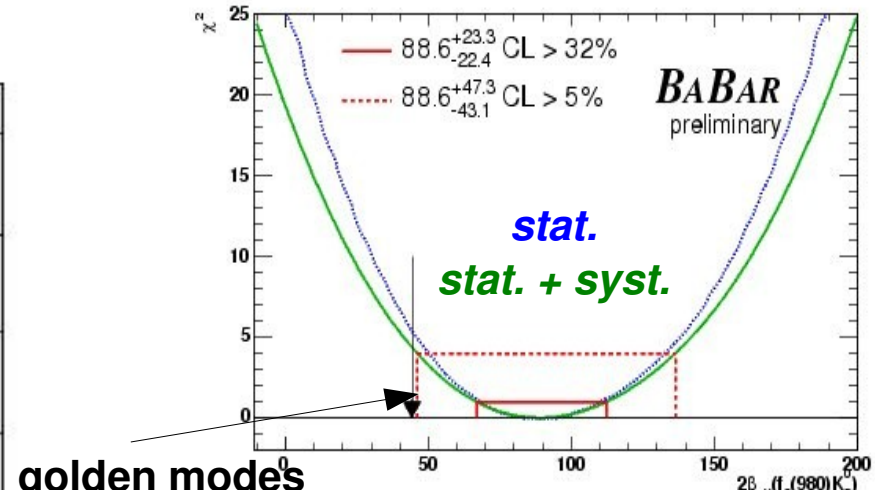
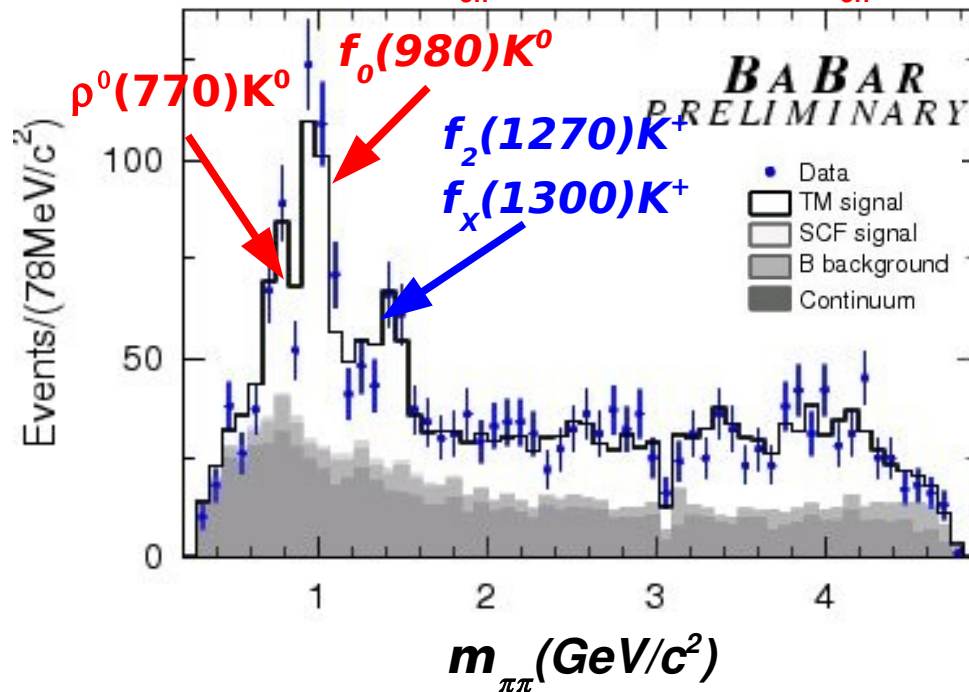




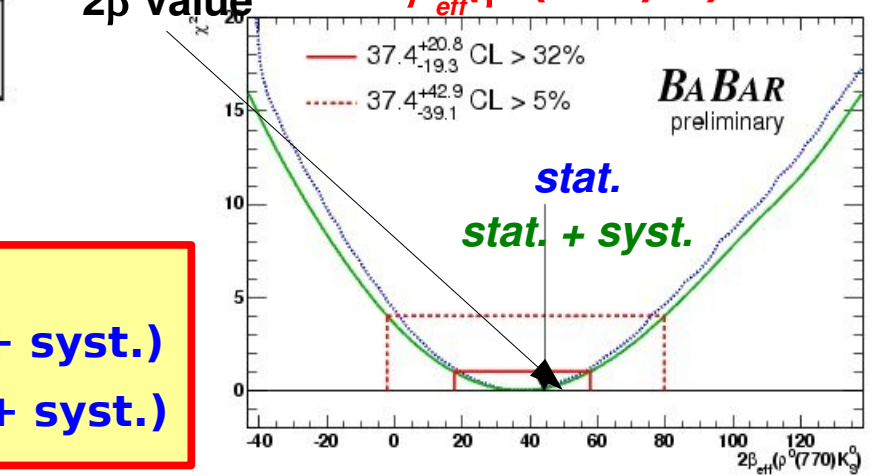
β_{eff} from time-dependent DP analysis: $K^0_S \pi^+ \pi^-$

- $\pi\pi$ spectrum: as in $B^+ \rightarrow K^+ \pi^- \pi^+$, $f_2(1270)K^0_S$ and a scalar $f_x(1300)K^0_S$
- Amplitude analysis for $f_0(980)K^0$ and $\rho^0(770)K^0$: $2\beta_{\text{eff}}(f_0(980)K^0)$

measure of $2\beta_{\text{eff}}$ instead of $\sin(2\beta_{\text{eff}})$



golden modes
 2β value



arXiv:0708.2097

$$2\beta_{\text{eff}}(f_0(980)K^0) = (88.6^{+23.3}_{-22.4})^\circ \text{ (stat. + syst.)}$$

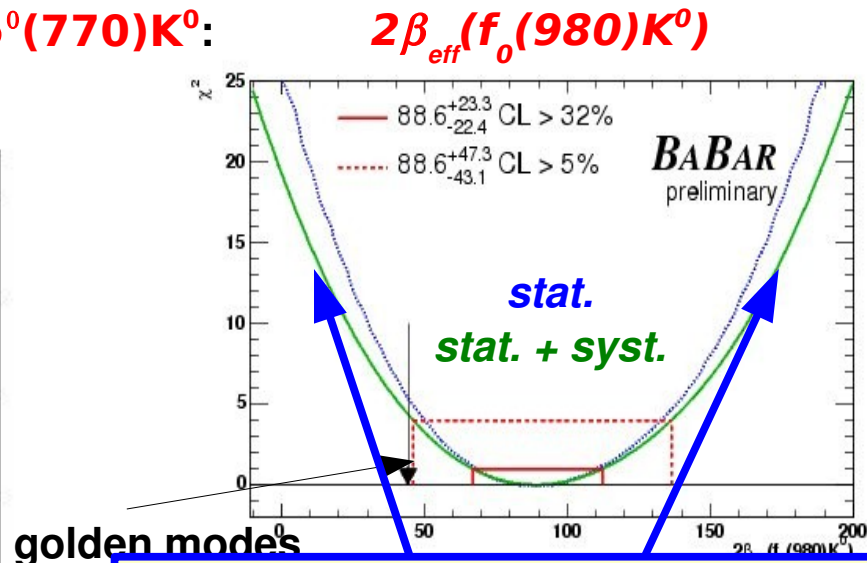
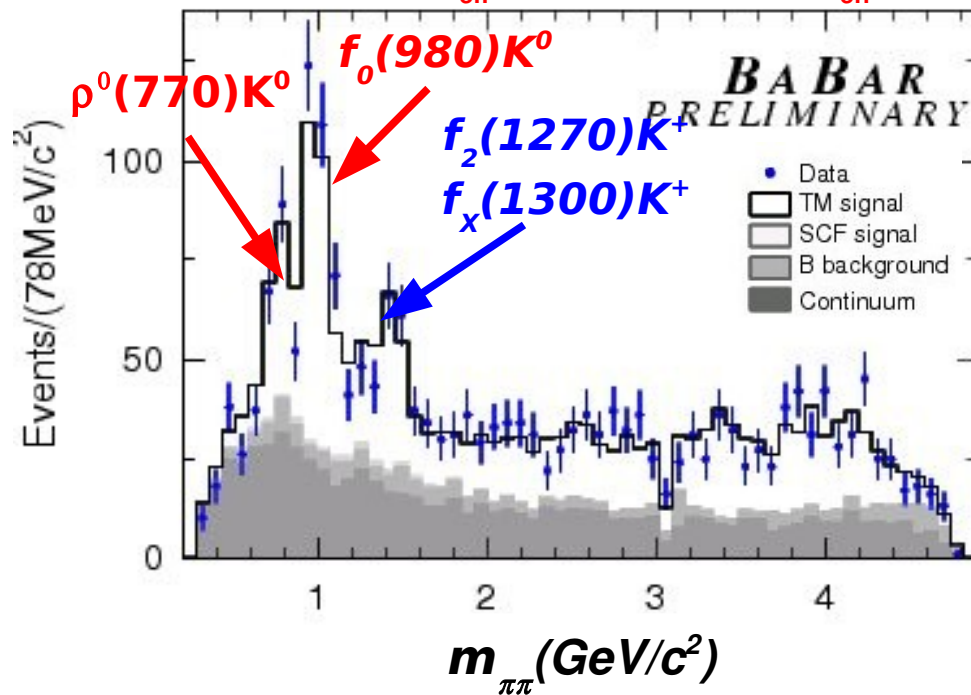
$$2\beta_{\text{eff}}(\rho^0(770)K^0) = (37.4^{+20.8}_{-19.3})^\circ \text{ (stat. + syst.)}$$



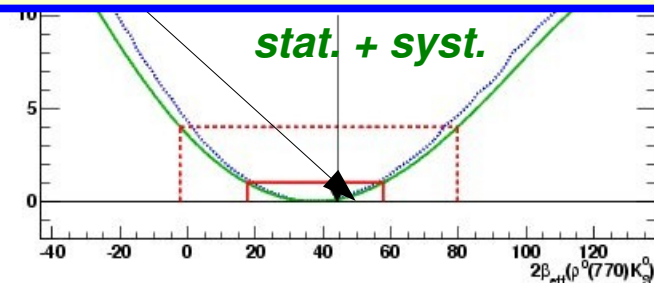
β_{eff} from time-dependent DP analysis: $K^0_S \pi^+ \pi^-$

- $\pi\pi$ spectrum: as in $B^+ \rightarrow K^+ \pi^- \pi^+$, $f_2(1270)K^0_S$ and a scalar $f_x(1300)K^0_S$
- Amplitude analysis for $f_0(980)K^0$ and $\rho^0(770)K^0$: $2\beta_{\text{eff}}(f_0(980)K^0)$

measure of $2\beta_{\text{eff}}$ instead of $\sin(2\beta_{\text{eff}})$



Non-gaussian result for $f_0 K^0_S$
 $2\beta_{\text{eff}}(f_0(980)K^0) = 0 (=180)$
 excluded at 4.3σ (3.9σ)



arXiv:0708.2097

$$2\beta_{\text{eff}}(f_0(980)K^0) = (88.6^{+23.3}_{-22.4})^\circ \text{ (stat. + syst.)}$$

$$2\beta_{\text{eff}}(\rho^0(770)K^0) = (37.4^{+20.8}_{-19.3})^\circ \text{ (stat. + syst.)}$$



β_{eff} from time-dependent DP analysis: $K^+K^-K^0$

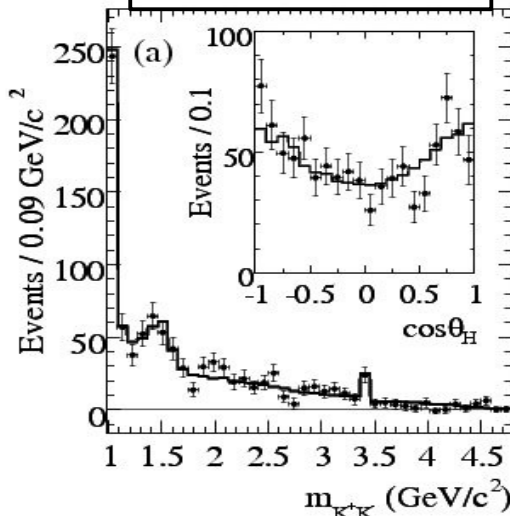
- Fit strategy:

fit on the whole phase space. Average CPV parameters (same β_{eff})

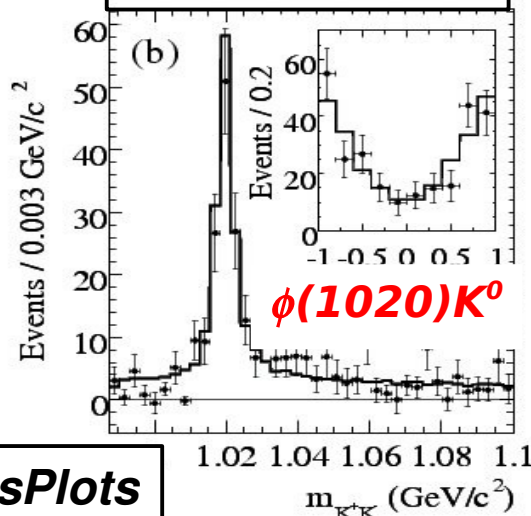
fit on low KK mass (mostly $f_0(980)K^0_s$ and $\phi(1020)K^0_s$ components).

fit on high KK mass (mostly non-resonant component).

whole KK mass



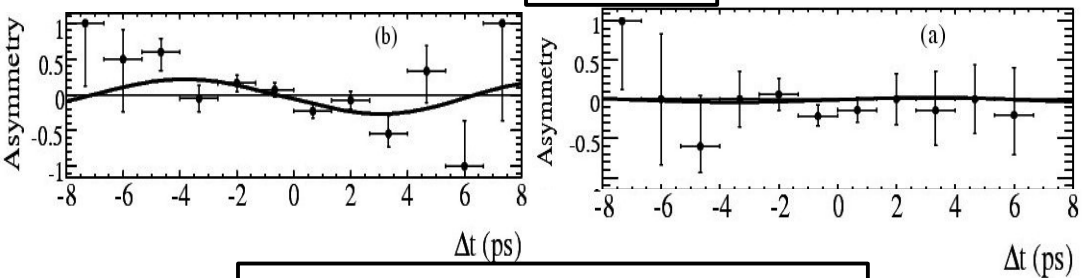
low KK mass



PRL99:161802

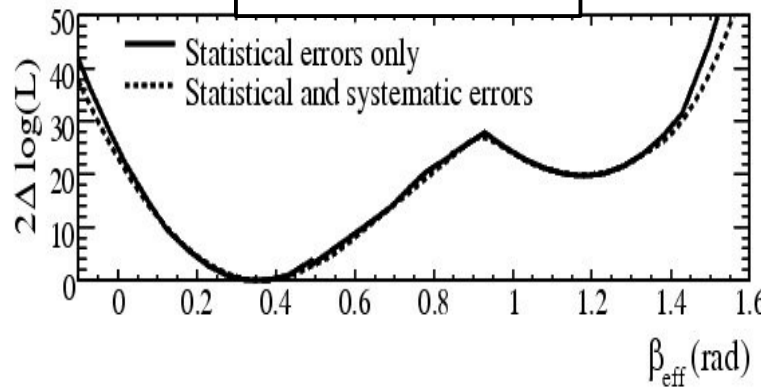
	A_{CP}	β_{eff} (rad)
Whole DP	$-0.015 \pm 0.077 \pm 0.053$	$0.352 \pm 0.076 \pm 0.026$
High-mass	$-0.054 \pm 0.102 \pm 0.060$	$0.436 \pm 0.087^{+0.055}_{-0.031}$
(1) ϕK^0	$-0.08 \pm 0.18 \pm 0.04$	$0.11 \pm 0.14 \pm 0.06$
(1) $f_0 K^0$	$0.41 \pm 0.23 \pm 0.07$	$0.14 \pm 0.15 \pm 0.05$
(2) ϕK^0	-0.11 ± 0.18	0.10 ± 0.13
(2) $f_0 K^0$	-0.20 ± 0.31	3.09 ± 0.19

sPlots



time-dependent asymmetries

Likelihood scan





β_{eff} from time-dependent DP analysis: $K^+K^-K^0$

- Fit strategy:

fit on the whole phase space. Average CPV parameters (same β_{eff})

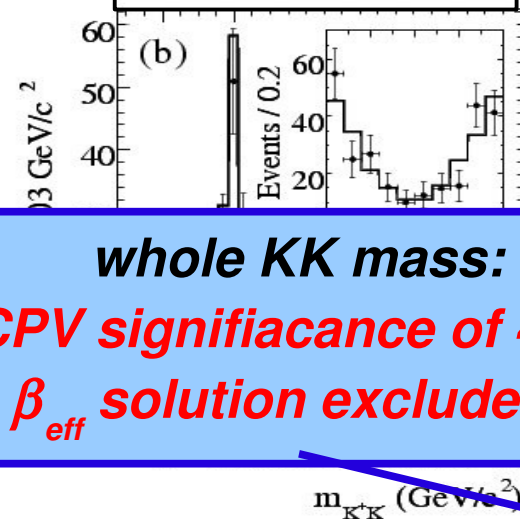
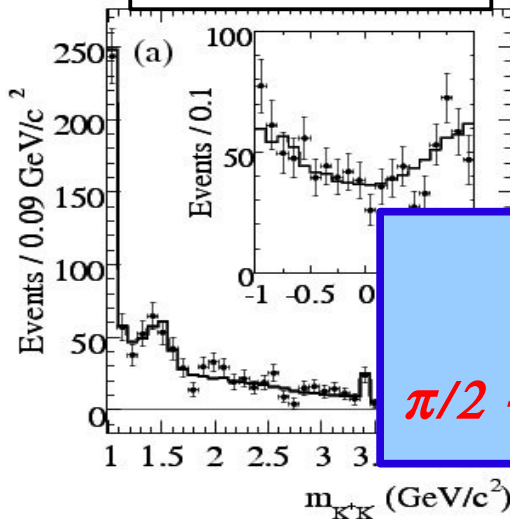
fit on low KK mass (mostly $f_0(980)K_s^0$ and $\phi(1020)K_s^0$ components).

fit on high KK mass (mostly non-resonant component).

whole KK mass

low KK mass

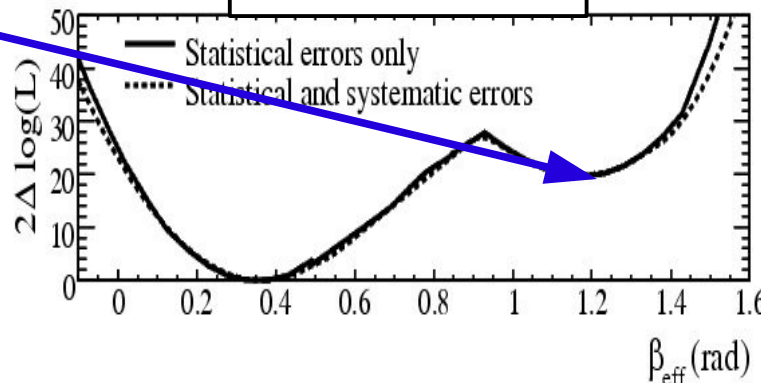
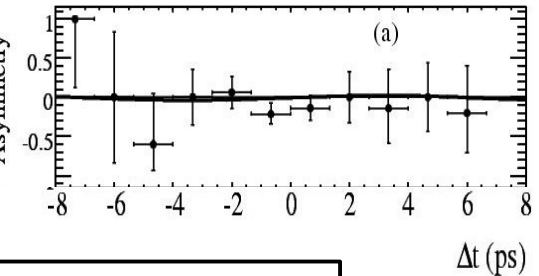
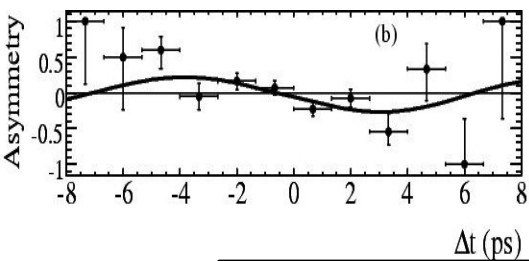
PRL99:161802



	A_{CP}	$\beta_{\text{eff}}(\text{rad})$
Whole DP	$-0.015 \pm 0.077 \pm 0.053$	$0.352 \pm 0.076 \pm 0.026$
High mass	$0.054 \pm 0.102 \pm 0.060$	$0.426 \pm 0.087 \pm 0.055$ -0.031
	$-0.08 \pm 0.18 \pm 0.04$	$0.11 \pm 0.14 \pm 0.06$
	$0.41 \pm 0.23 \pm 0.07$	$0.14 \pm 0.15 \pm 0.05$
	-0.11 ± 0.18	0.10 ± 0.13
	-0.20 ± 0.31	3.09 ± 0.19

whole KK mass:
CPV significance of 4.8σ
 $\pi/2 - \beta_{\text{eff}}$ solution excluded at 4.5σ

Likelihood scan



time-dependent asymmetries



β_{eff} (loop $b \rightarrow s$) vs β (tree $b \rightarrow s$)

9 $b \rightarrow s q \bar{q}$ modes

golden modes:

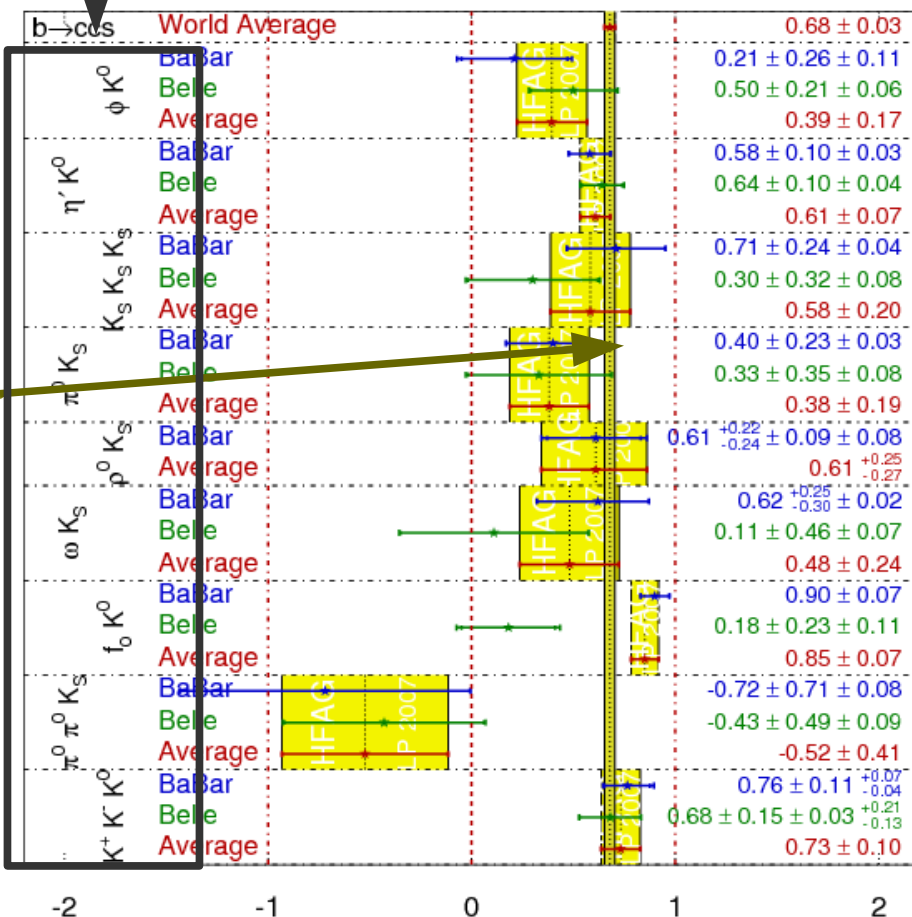
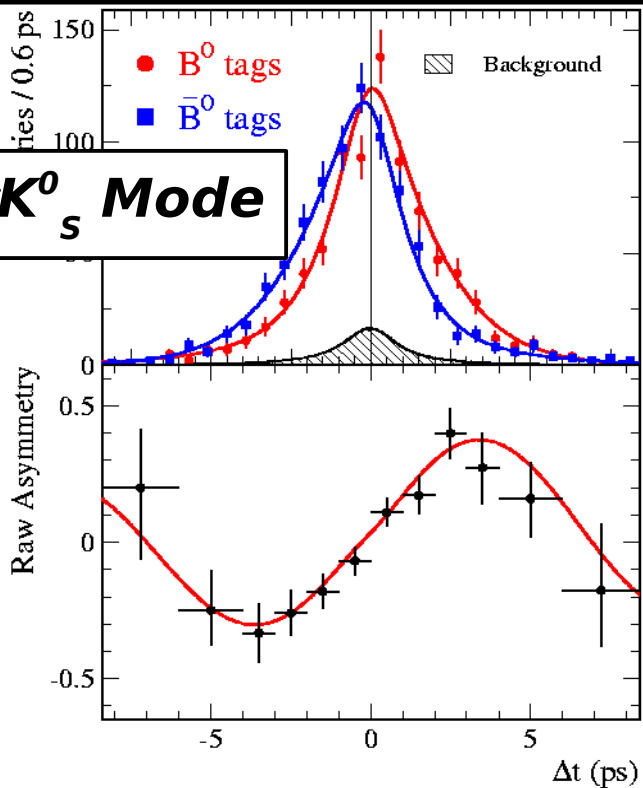
$$\sin(2\beta) = 0.680 \pm 0.025$$

(HFAG average)

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

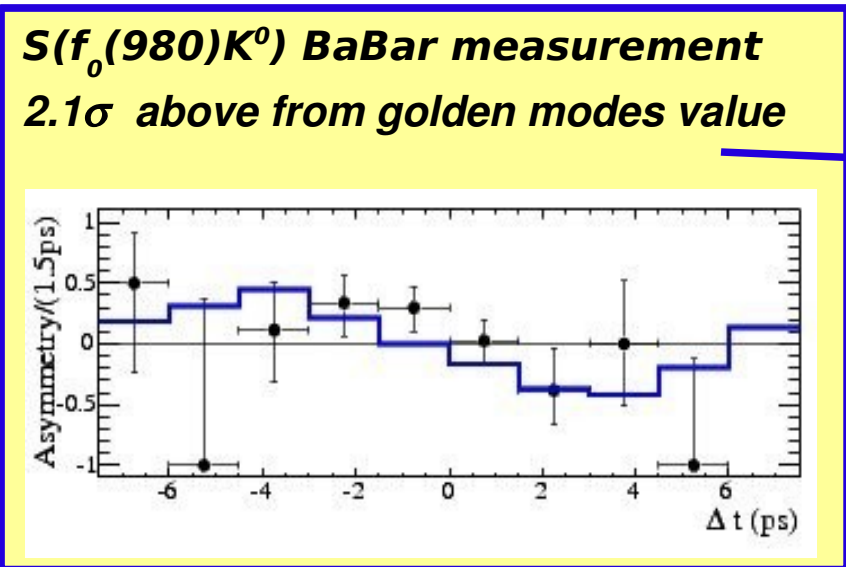
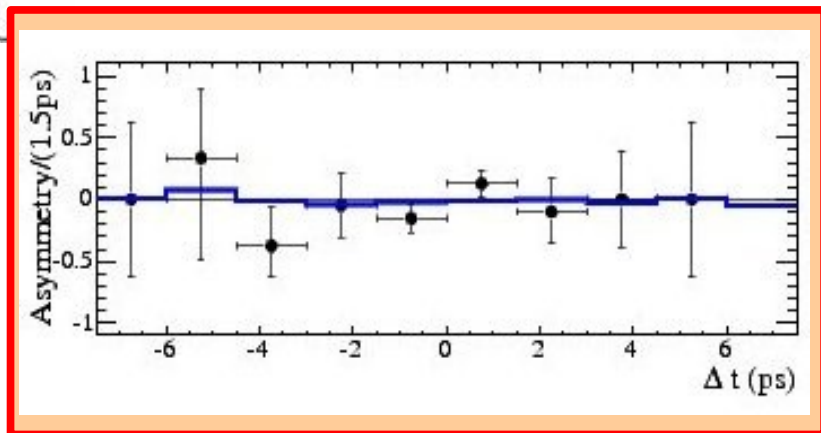
HFAG
LP 2007
PRELIMINARY

$J/\psi K_s^0$ Mode





β_{eff} (loop $b \rightarrow s$) vs β (tree $b \rightarrow s$)



$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$ **HFLAG**
 LP 2007
 PRELIMINARY

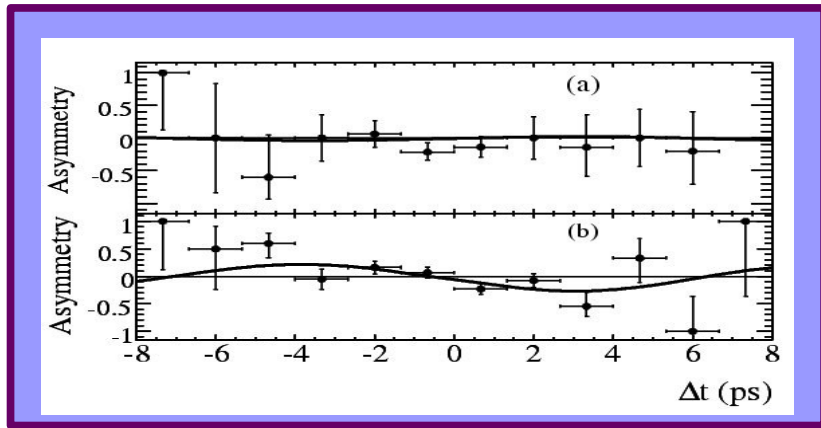
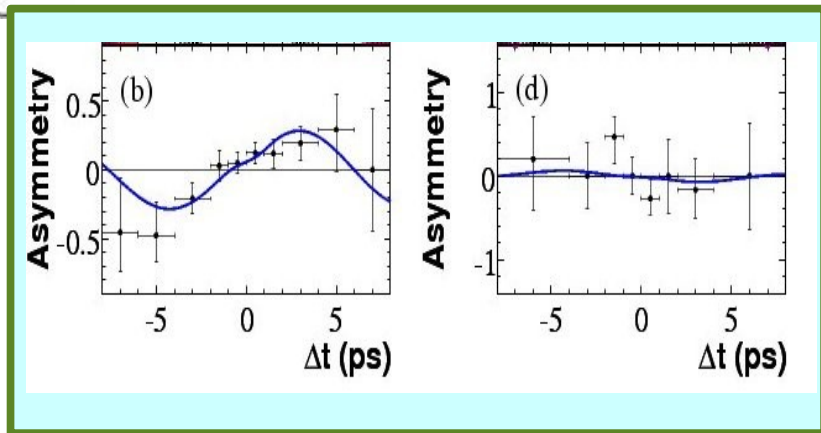
$b \rightarrow ccs$	World Average		0.68 ± 0.03
ϕK^0	BaBar		$0.21 \pm 0.26 \pm 0.11$
	Belle		$0.50 \pm 0.21 \pm 0.06$
	Average		0.39 ± 0.17
$\eta' K^0$	BaBar		$0.58 \pm 0.10 \pm 0.03$
	Belle		$0.64 \pm 0.10 \pm 0.04$
	Average		0.61 ± 0.07
$K_S K_S K_S$	BaBar		$0.71 \pm 0.24 \pm 0.04$
	Belle		$0.30 \pm 0.32 \pm 0.08$
	Average		0.58 ± 0.20
$\pi^0 K_S$	BaBar		$0.40 \pm 0.23 \pm 0.03$
	Belle		$0.33 \pm 0.35 \pm 0.08$
	Average		0.38 ± 0.19
$\rho^0 K_S$	BaBar		$0.61^{+0.22}_{-0.24} \pm 0.09 \pm 0.08$
	BaBar		$0.61^{+0.25}_{-0.27} \pm 0.09 \pm 0.08$
	Average		$0.62^{+0.25}_{-0.26} \pm 0.09$
ωK_S	Belle		$0.11 \pm 0.46 \pm 0.07$
	Average		0.48 ± 0.24
	$f_0 K^0$	BaBar	
Belle			$0.18 \pm 0.23 \pm 0.11$
Average			0.85 ± 0.07
$\pi^0 \pi^0 K_S$	BaBar		$-0.72 \pm 0.71 \pm 0.08$
	Belle		$-0.43 \pm 0.49 \pm 0.09$
	Average		-0.52 ± 0.41
$K^+ K^- K^0$	BaBar		$0.76 \pm 0.11^{+0.07}_{-0.04}$
	Belle		$0.68 \pm 0.15 \pm 0.03^{+0.21}_{-0.13}$
	Average		0.73 ± 0.10

S golden modes value



β_{eff} (loop $b \rightarrow s$) vs β (tree $b \rightarrow s$)

$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$ **HFLAG**
 LP 2007
 PRELIMINARY



Mode	Source	Value
ϕK^0	BaBar	$0.21 \pm 0.26 \pm 0.11$
	Belle	$0.50 \pm 0.21 \pm 0.06$
	Average	0.39 ± 0.17
$\eta' K^0$	BaBar	$0.58 \pm 0.10 \pm 0.03$
	Belle	$0.64 \pm 0.10 \pm 0.04$
	Average	0.61 ± 0.07
$K_S K_S K_S$	BaBar	$0.71 \pm 0.24 \pm 0.04$
	Belle	$0.30 \pm 0.32 \pm 0.08$
	Average	0.58 ± 0.20
$\pi^0 K_S$	BaBar	$0.40 \pm 0.23 \pm 0.03$
	Belle	$0.33 \pm 0.35 \pm 0.08$
	Average	0.38 ± 0.19
$\rho^0 K_S$	BaBar	$0.61^{+0.22}_{-0.24} \pm 0.09 \pm 0.08$
	Belle	$0.61^{+0.25}_{-0.27} \pm 0.25 \pm 0.27$
	Average	$0.61 \pm 0.09 \pm 0.08$
ωK_S	BaBar	$0.62^{+0.25}_{-0.30} \pm 0.02$
	Belle	$0.11 \pm 0.46 \pm 0.07$
	Average	0.48 ± 0.24
$t_0 K^0$	BaBar	0.90 ± 0.07
	Belle	$0.18 \pm 0.23 \pm 0.11$
	Average	0.85 ± 0.07
$\pi^0 K_S$	BaBar	$-0.72 \pm 0.71 \pm 0.08$
	Belle	$-0.43 \pm 0.49 \pm 0.09$
	Average	-0.52 ± 0.11
$K^+ K^- K^0$	BaBar	$0.76 \pm 0.11^{+0.07}_{-0.04}$
	Belle	$0.68 \pm 0.15 \pm 0.03^{+0.21}_{-0.13}$
	Average	0.73 ± 0.10

S golden modes value



“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K_S^0\pi^+\pi^-$

$K\pi$ Isospin relations:

$$A(B^0 \rightarrow K^{*+}\pi^-) = V_{us} V_{ub}^* T^{+-} + V_{ts} V_{tb}^* P^{+-}$$

$$\sqrt{2} \cdot A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* T^{00} + V_{ts} V_{tb}^* (-P^{+-} + P_{EW})$$

Neglecting P_{EW} , the amplitude combinations:

$$3A_{3/2} = A(B^0 \rightarrow K^{*+}\pi^-) + \sqrt{2} \cdot A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* (T^{+-} + T^{00})$$

$$3\bar{A}_{3/2} = \bar{A}(\bar{B}^0 \rightarrow K^{*0}\pi^+) + \sqrt{2} \cdot \bar{A}(\bar{B}^0 \rightarrow \bar{K}^{*0}\pi^0) = V_{us}^* V_{ub} (T^{+-} + T^{00})$$

which gives: $R_{3/2} = (3A_{3/2}) / (3\bar{A}_{3/2}) = e^{-2i\gamma}$

CPS PRD74:051301
GPSZ PRD75:014002

Direct access to γ CKM angle



“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K_S^0\pi^+\pi^-$

$K^*\pi$ Isospin relations:

$$A(B^0 \rightarrow K^{*+}\pi^-) = V_{us} V_{ub}^* T^{+-} + V_{ts} V_{tb}^* P^{+-}$$

$$\sqrt{2} \cdot A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* T^{00} + V_{ts} V_{tb}^* (-P^{+-} + P_{EW})$$

Neglecting P_{EW} , the amplitude combinations:

$$3A_{3/2} = A(B^0 \rightarrow K^{*+}\pi^-) + \sqrt{2} \cdot A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* (T^{+-} + T^{00})$$

$$3\bar{A}_{3/2} = \bar{A}(B^0 \rightarrow K^{*-}\pi^+) + \sqrt{2} \cdot \bar{A}(B^0 \rightarrow \bar{K}^{*0}\pi^0) = V_{us}^* V_{ub} (T^{+-} + T^{00})$$

which gives: $R_{3/2} = (3A_{3/2}) / (3\bar{A}_{3/2}) = e^{-2i\gamma}$

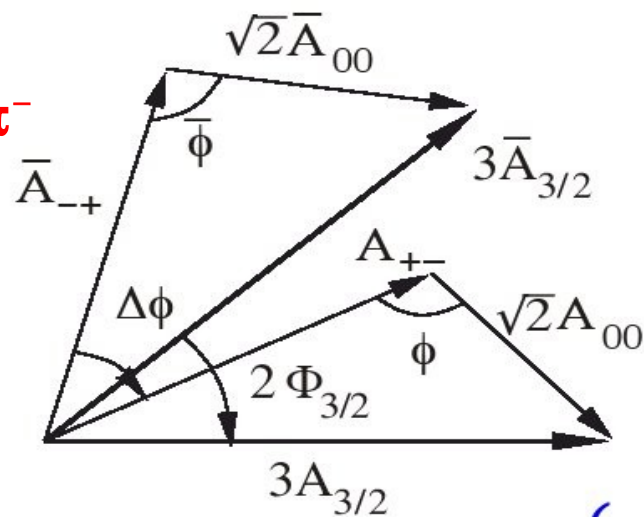
CPS PRD74:051301
GPSZ PRD75:014002

From experiment:

Measurable from $K^+\pi^-\pi^0$ and $K_S^0\pi^+\pi^-$

- $|A(B^0 \rightarrow K^{*+}\pi^-)|$ and $|A(B^0 \rightarrow K^{*0}\pi^0)|$
- $|\bar{A}(B^0 \rightarrow \bar{K}^{*-}\pi^+)|$ and $|\bar{A}(B^0 \rightarrow \bar{K}^{*0}\pi^0)|$

Through BRs





“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K^0_S\pi^+\pi^-$

$K^*\pi$ Isospin relations:

$$A(B^0 \rightarrow K^{*+}\pi^-) = V_{us} V_{ub}^* T^{+-} + V_{ts} V_{tb}^* P^{+-}$$

$$\sqrt{2} A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* T^{00} + V_{ts} V_{tb}^* (-P^{+-} + P_{EW})$$

Neglecting P_{EW} , the amplitude combinations:

$$3A_{3/2} = A(B^0 \rightarrow K^{*+}\pi^-) + \sqrt{2} A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* (T^{+-} + T^{00})$$

$$3\bar{A}_{3/2} = \bar{A}(B^0 \rightarrow K^{*-}\pi^+) + \sqrt{2} \bar{A}(B^0 \rightarrow \bar{K}^{*0}\pi^0) = V_{us}^* V_{ub} (T^{+-} + T^{00})$$

which gives: $R_{3/2} = (3A_{3/2}) / (3\bar{A}_{3/2}) = e^{-2i\gamma}$

CPS PRD74:051301
GPSZ PRD75:014002

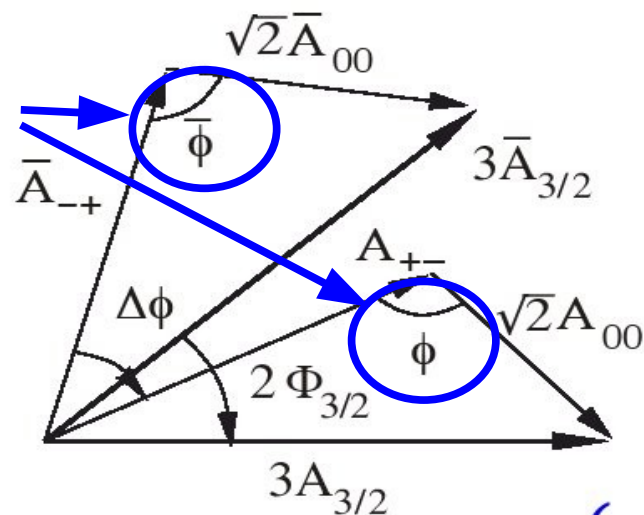
From experiment:

Measurable from $K^+\pi^-\pi^0$

$$\phi = \arg(A(B^0 \rightarrow K^{*+}\pi^-) A^*(B^0 \rightarrow K^{*0}\pi^0))$$

$$\bar{\phi} = \arg(\bar{A}(B^0 \rightarrow K^{*-}\pi^+) \bar{A}^*(B^0 \rightarrow \bar{K}^{*0}\pi^0))$$

Through interference





“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K^0_S\pi^+\pi^-$

$K^*\pi$ Isospin relations:

$$A(B^0 \rightarrow K^{*+}\pi^-) = V_{us} V_{ub}^* T^{+-} + V_{ts} V_{tb}^* P^{+-}$$

$$\sqrt{2} A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* T^{00} + V_{ts} V_{tb}^* (-P^{+-} + P_{EW})$$

Neglecting P_{EW} , the amplitude combinations:

$$3A_{3/2} = A(B^0 \rightarrow K^{*+}\pi^-) + \sqrt{2} A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* (T^{+-} + T^{00})$$

$$3\bar{A}_{3/2} = \bar{A}(\bar{B}^0 \rightarrow K^{*-}\pi^+) + \sqrt{2} \bar{A}(\bar{B}^0 \rightarrow \bar{K}^{*0}\pi^0) = V_{us}^* V_{ub} (T^{+-} + T^{00})$$

which gives: $R_{3/2} = (3A_{3/2}) / (3\bar{A}_{3/2}) = e^{-2i\gamma}$

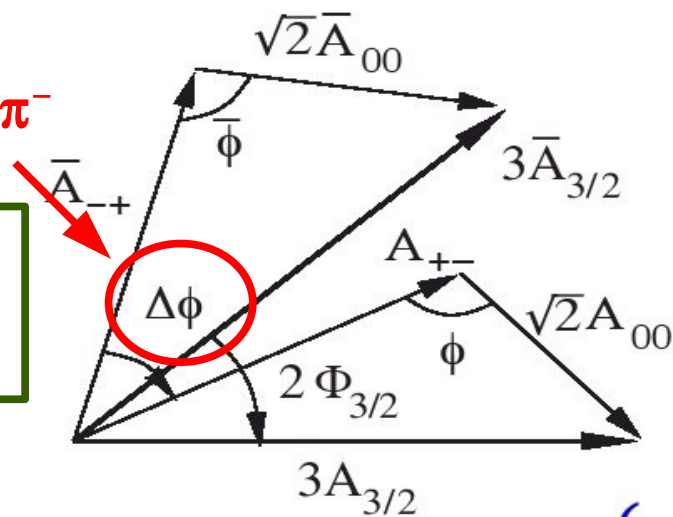
CPS PRD74:051301
GPSZ PRD75:014002

From experiment:

Measurable from $K^0_S\pi^+\pi^-$

$$\Delta\phi = \arg(A(B^0 \rightarrow K^{*+}\pi^-) A^*(\bar{B}^0 \rightarrow \bar{K}^{*-}\pi^+))$$

Through interference





“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K^0_S\pi^+\pi^-$

$K^*\pi$ Isospin relations:

$$A(B^0 \rightarrow K^{*+}\pi^-) = V_{us} V_{ub}^* T^{+-} + V_{ts} V_{tb}^* P^{+-}$$

$$\sqrt{2} A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* T^{00} + V_{ts} V_{tb}^* (-P^{+-} + P_{EW})$$

Neglecting P_{EW} , the amplitude combinations:

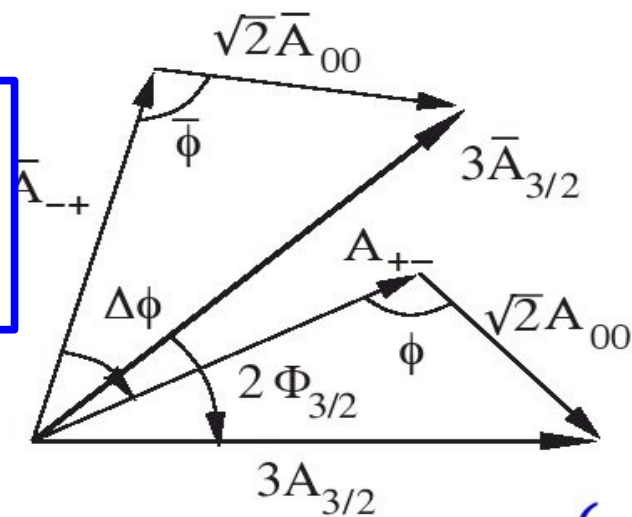
$$3A_{3/2} = A(B^0 \rightarrow K^{*+}\pi^-) + \sqrt{2} A(B^0 \rightarrow K^{*0}\pi^0) = V_{us} V_{ub}^* (T^{+-} + T^{00})$$

$$3\bar{A}_{3/2} = \bar{A}(\bar{B}^0 \rightarrow K^{*0}\pi^+) + \sqrt{2} \bar{A}(\bar{B}^0 \rightarrow \bar{K}^{*0}\pi^0) = V_{us}^* V_{ub} (T^{+-} + T^{00})$$

which gives: $R_{3/2} = (3A_{3/2}) / (3\bar{A}_{3/2}) = e^{-2i\gamma}$

CPS PRD74:051301
GPSZ PRD75:014002

With non zero P_{EW} ,
non-trivial constraint in $(\rho-\eta)$



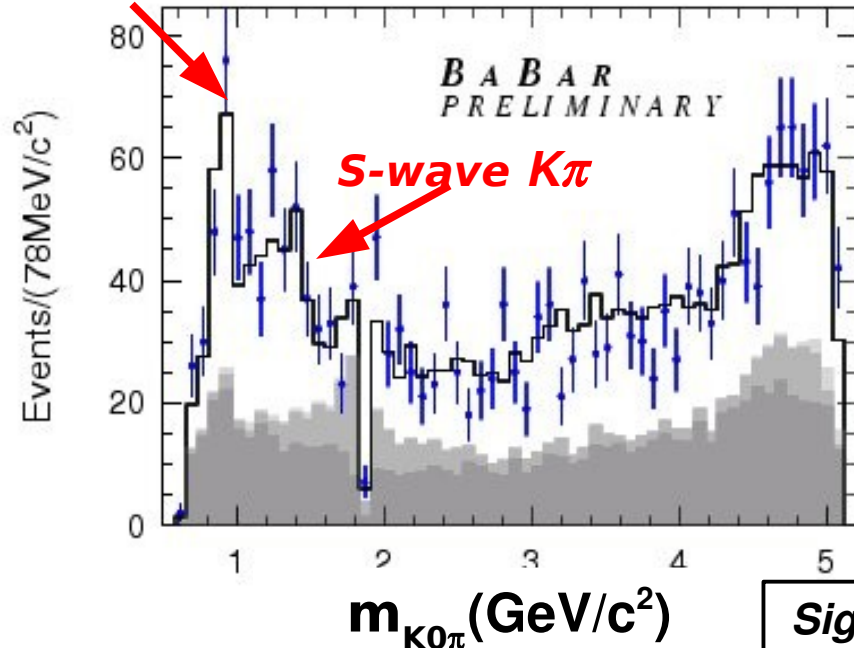


“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K_S^0\pi^+\pi^-$

- **$K\pi$ spectrum:** as in the $B^+ \rightarrow K^+\pi^-\pi^+$ using **LASS lineshape** to describe **S-wave $K\pi$** . No significant $K_2^{*0}(1430)$ contribution

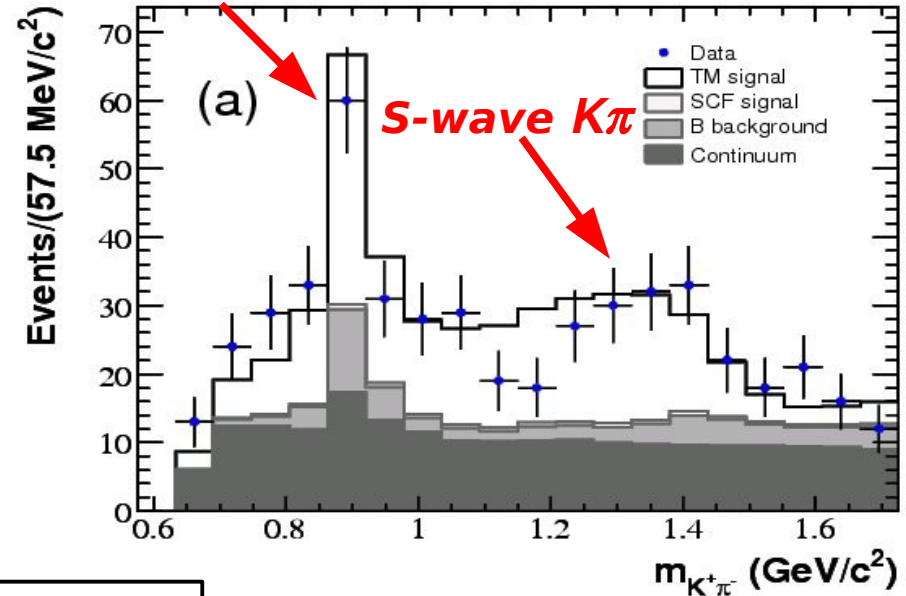
$K_S^0\pi^+\pi^-$ time-dependent DP analysis

$K^*(892)\pi$



$K^+\pi^-\pi^0$ time-integrated DP analysis

$K^*(892)\pi$



Signal enhanced projections

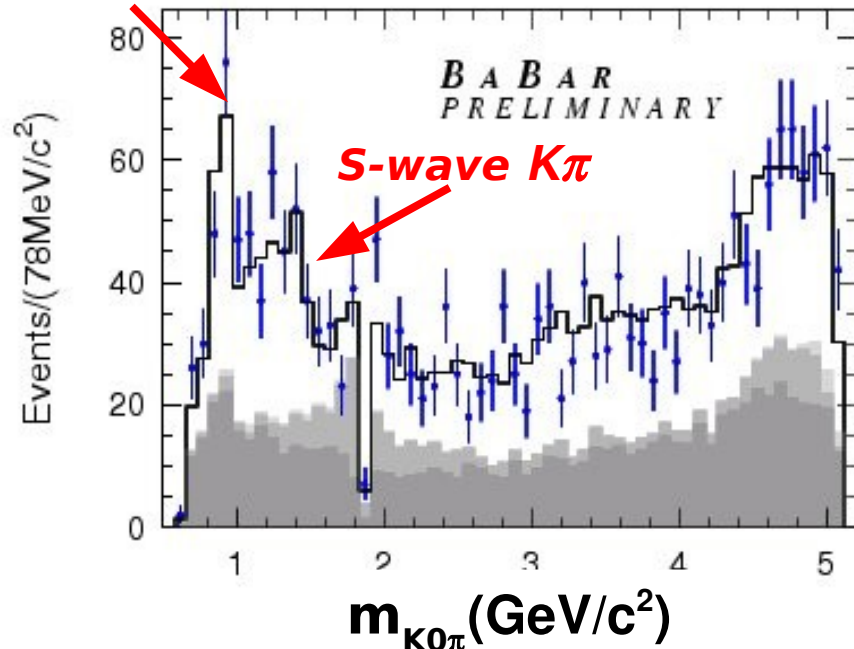


" γ " (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K_S^0\pi^+\pi^-$

- $K\pi$ spectrum:** as in the $B^+ \rightarrow K^+\pi^-\pi^+$ using **LASS** lineshape to describe **S-wave $K\pi$** . No significant $K_2^{*0}(1430)$ contribution

$K_S^0\pi^+\pi^-$ time-dependent DP analysis

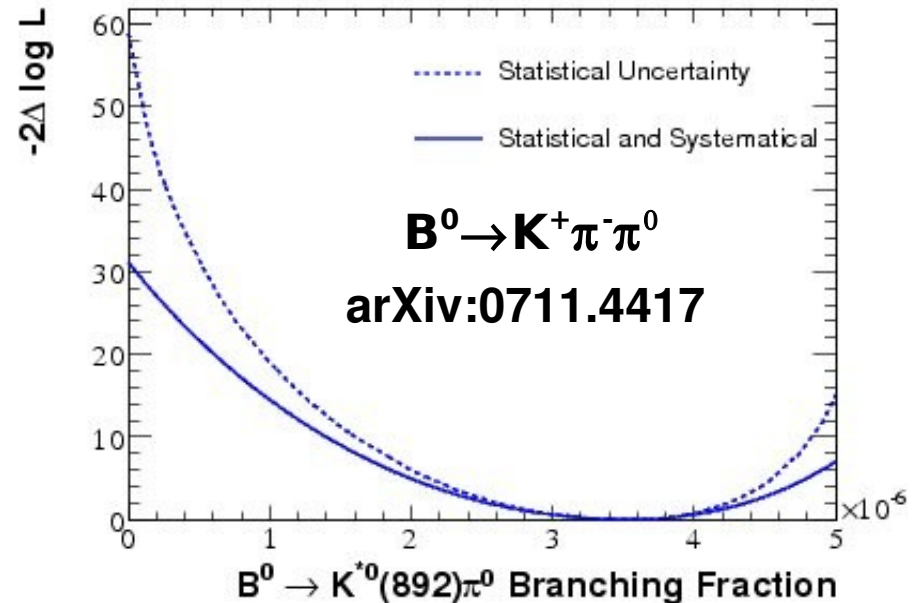
$K^*(892)\pi$



$K^+\pi^-\pi^0$ time-integrated DP analysis

Observation at 5.6σ of $B^0 \rightarrow K^{*0}(892)\pi^0$ decay

$$BF(B^0 \rightarrow K^{*0}(892)\pi^0) = (3.6^{+0.7}_{-0.8} \pm 0.4) \times 10^{-6}$$

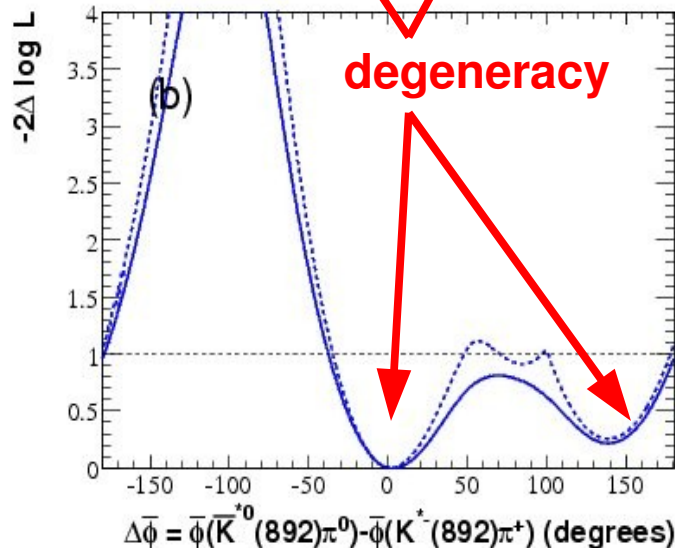
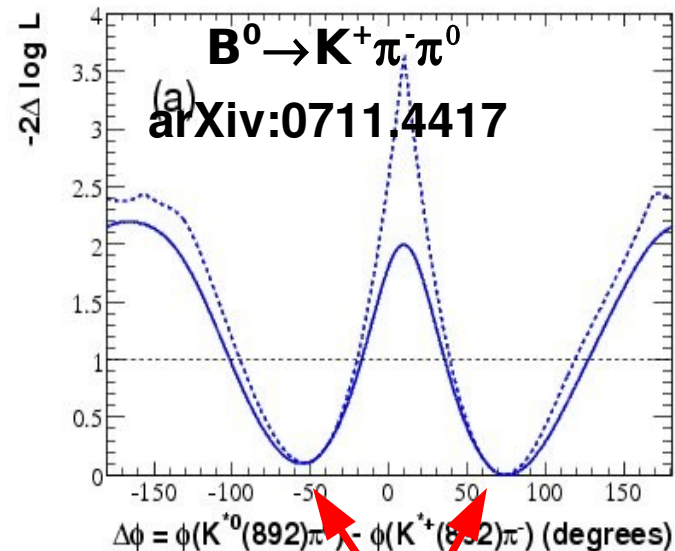
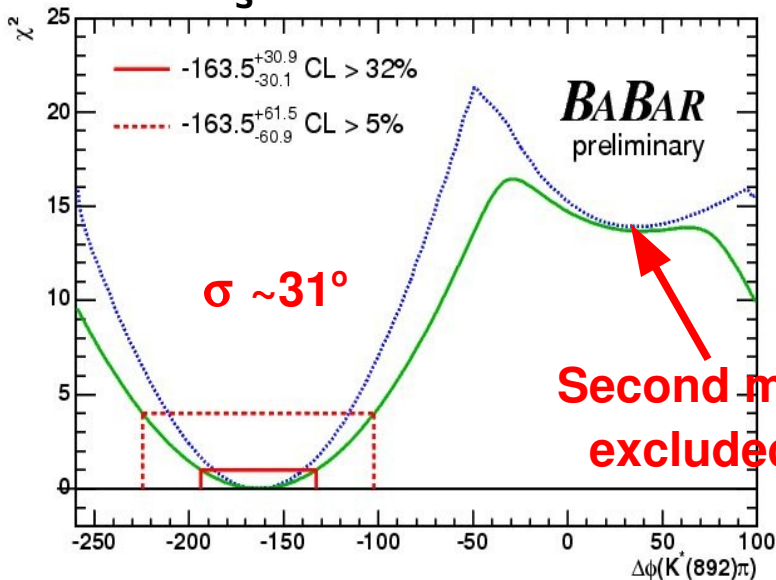




“ γ ” (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K^0_S\pi^+\pi^-$

- $|A_{ij}| \leftrightarrow$ BRs well measured
- $\Delta\phi$ obtained from Dalitz $B^0 \rightarrow K^0_S\pi^+\pi^-$:
 Single likelihood min, error $\sim 31^\circ$
- ϕ and $\bar{\phi}$ obtained from Dalitz $B^0 \rightarrow K^+\pi^-\pi^0$:
 2 minima close in Likelihood units, $\sim 1\sigma$.
 Phases weakly constrained

$B^0 \rightarrow K^0_S\pi^+\pi^-$, arXiv:0708.2097



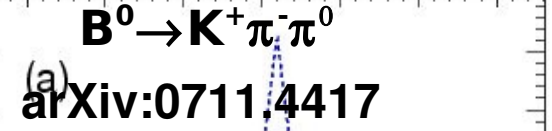


" γ " (CPS/GPSZ) from $K^+\pi^-\pi^0$, $K^0_S\pi^+\pi^-$

- $|A_{ij}| \leftrightarrow$ BRs well measured

- $\Delta\phi$ obtained from Dalitz

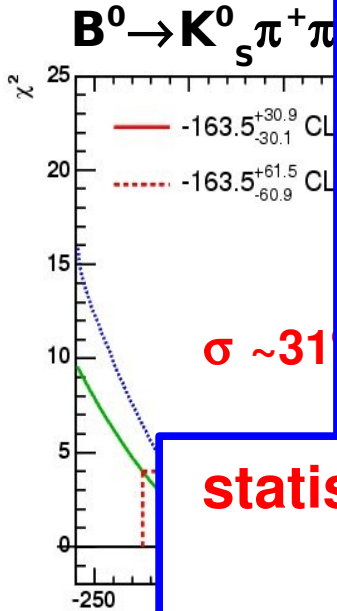
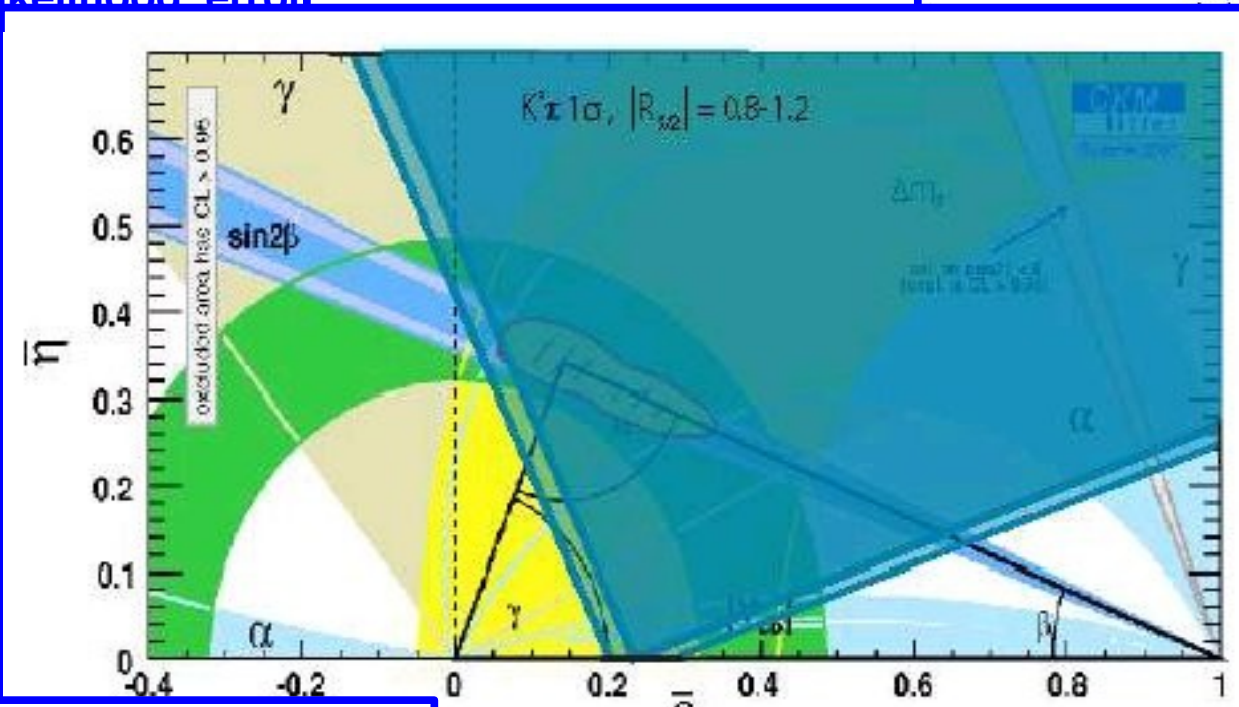
All ingredients for CPS/
GPSZ are there!



Single likelihood error

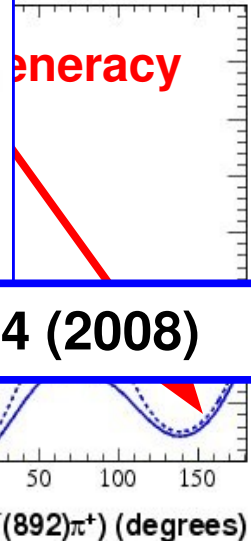
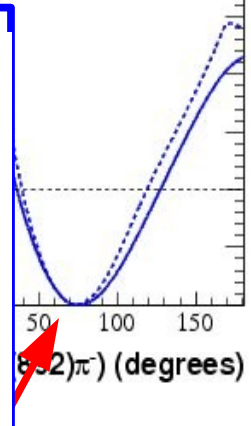
- ϕ and $\bar{\phi}$

2 minima
Phases



statistically limited
constraint

Gronau *et. al.* PRD:77,057504 (2008)





Conclusions

- BaBar is exploring many interesting topics in Charmless B decays:
 - Probing $\pi\pi$ and $K\pi$ mass spectrum with: $B^+ \rightarrow K^+ \pi^- \pi^+$
 - Evidence of DCPV: $B^+ \rightarrow K^+ \pi^- \pi^+$ (3.7σ in $\rho^0 K^+$)
 - Probing KK mass spectrum with:
 $B^+ \rightarrow K^+ K^- \pi^+$ & $B^0 \rightarrow K^+ K^- K^0$
 - $\sin(2\beta_{\text{eff}})$ from $\eta' K_s^0$, results compatible with $b \rightarrow s c \bar{c}$
 - β_{eff} from time-dependent DP analyses:
 $\rho^0 K_s^0$, $f_0 K_s^0$, ϕK_s^0 & high mass $K^+ K^- K^0$
 - “ γ ” via CPS/GPSZ: $B^0 \rightarrow K^+ \pi^- \pi^0$, $B^0 \rightarrow K_s^0 \pi^- \pi^+$, non-trivial constraint in $(\bar{\rho} - \bar{\eta})$ plane



Backup



Outline

- Dalitz analysis of $B^+ \rightarrow K^+ \pi^- \pi^+$:
 - ◆ $\pi\pi$ mass spectrum.
 - ◆ $K\pi$ mass spectrum.
 - ◆ Large Direct CP Violation (DCPV).
- \overline{KK} S-wave from $B^+ \rightarrow K^+ K^- \pi^+$ & $B^0 \rightarrow K^+ K^- K^0$
- $b \rightarrow s \overline{q} q$ penguin-dominated charmless decays.
 - ◆ $b \rightarrow s \overline{q} q$ penguins and new physics.
 - ◆ $\sin(2\beta_{\text{eff}})$ from $B^0 \rightarrow \eta' K^0$ (Q2B analysis)
 - ◆ Dalitz analyses: $2\beta_{\text{eff}}$ from $B^0 \rightarrow K^0_S \pi^+ \pi^-$ & $B^0 \rightarrow K^+ K^- K^0$
- “ γ ” (CPS/GPSZ) from $B^0 \rightarrow K^+ \pi^- \pi^0$ & $B^0 \rightarrow K^0_S \pi^+ \pi^-$ Dalitz analyses.
- Conclusions



The Standard Model and the CKM Matrix

- SM:** gauge theory of **strong** and **electroweak** interactions. With the symmetry group,

$$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$$

Elementary Particles

Quarks	<i>u</i> up	<i>c</i> charm	<i>t</i> top	γ photon	<i>g</i> gluon
	<i>d</i> down	<i>s</i> strange	<i>b</i> bottom		
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	<i>Z</i> Z boson	<i>W</i> W boson
	<i>e</i> electron	μ muon	τ tau		

I II III
Three Families of Matter

In the quark sector:
mass eigenstates
 \neq
gauge eigenstates

$$\begin{cases} L_{CC} = g V_{CKM}^{ij} \bar{u}_L^i \gamma_\mu d_L^j W^{\mu-} + h.c. \\ CP^{-1} L_{CC} CP = g (V_{CKM}^T)^{ij} \bar{d}_L^i \gamma_\mu u_L^j W^{\mu-} + h.c. \end{cases}$$

V_{CKM} Complex \rightarrow CP violation in SM

$V_{CKM} V_{CKM}^\dagger = I \rightarrow$ Quarks mixing described by 3 real parameters and one phase

λ power expansion until λ^3 with $\lambda = \sin(\theta_{\text{cabibbo}}) \approx 0.22$

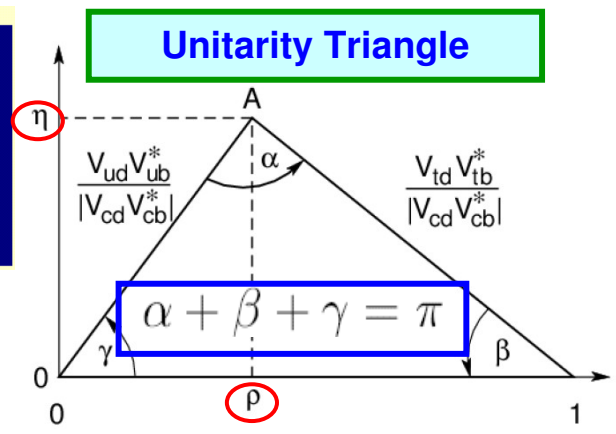
CKM matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

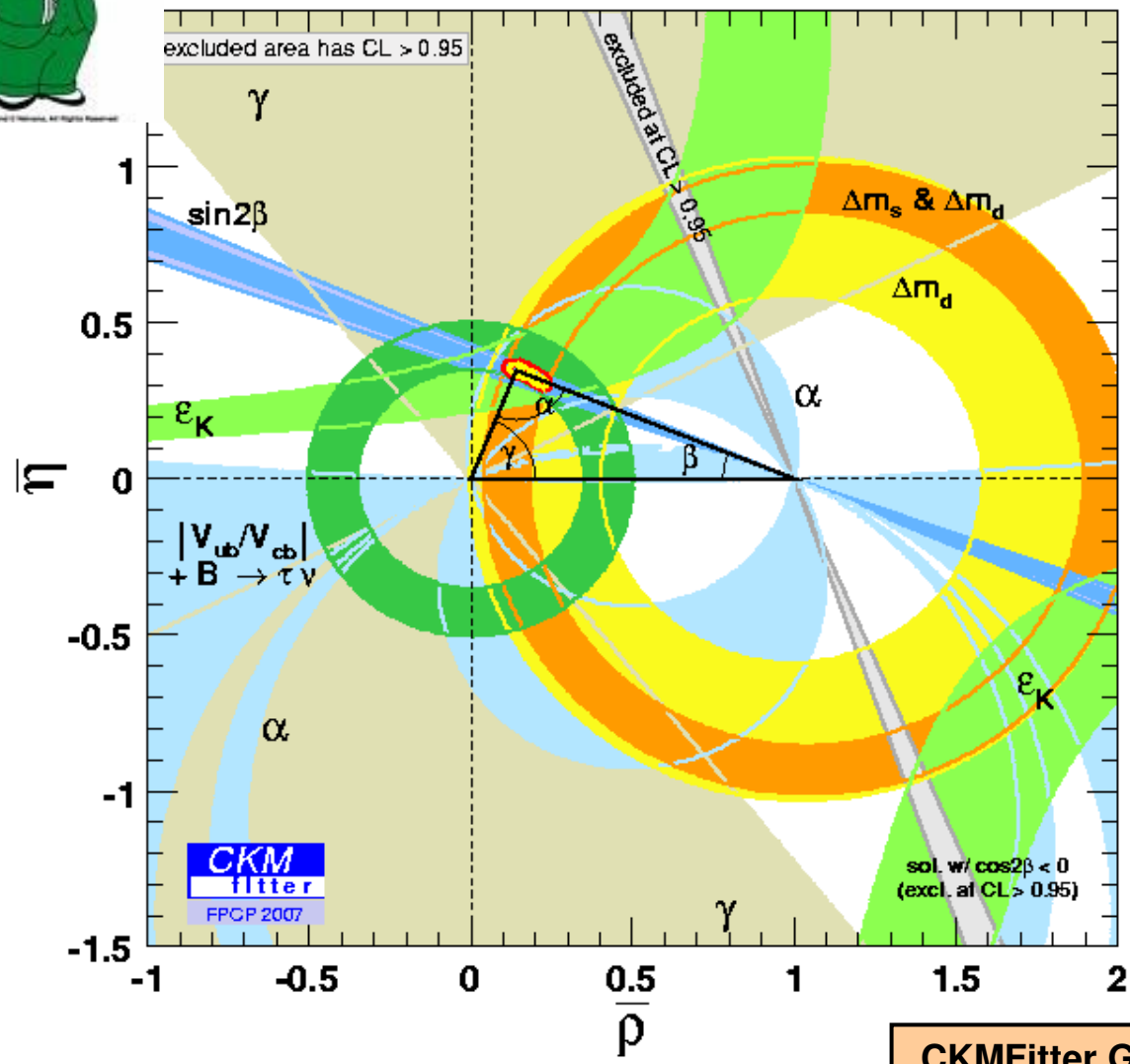
Wolfenstein parameterization:

Experimental hierarchic structure

CP violation possible in the SM only if $\eta \neq 0$



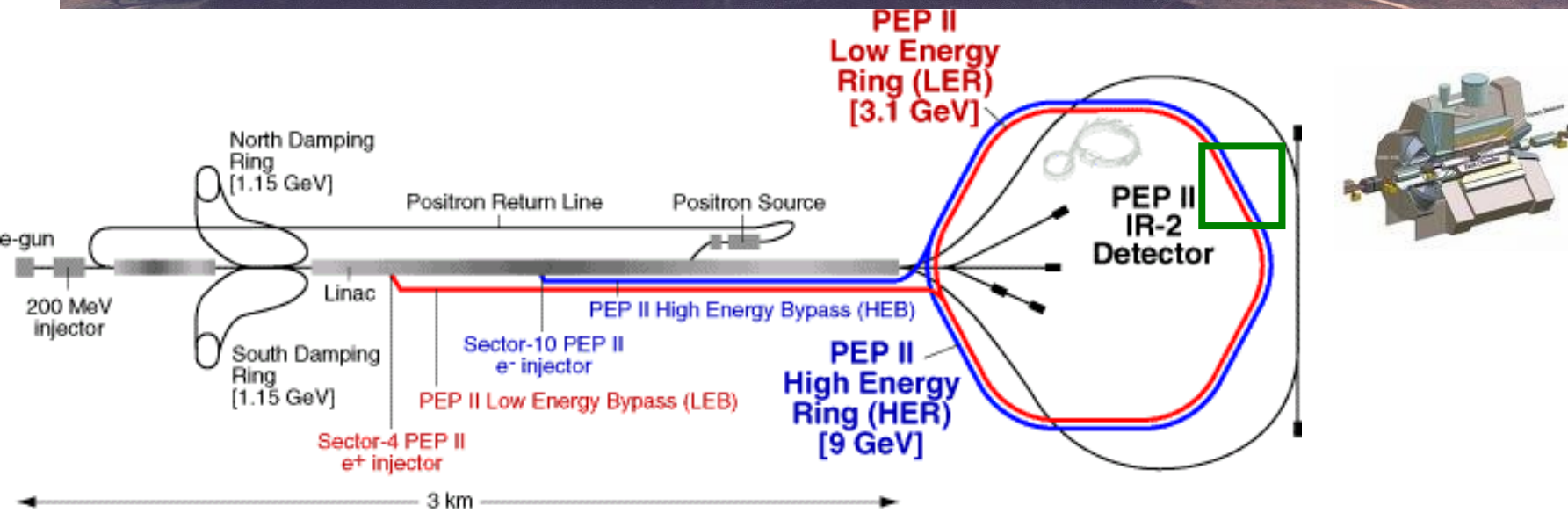
CKM Matrix: Current knowledge

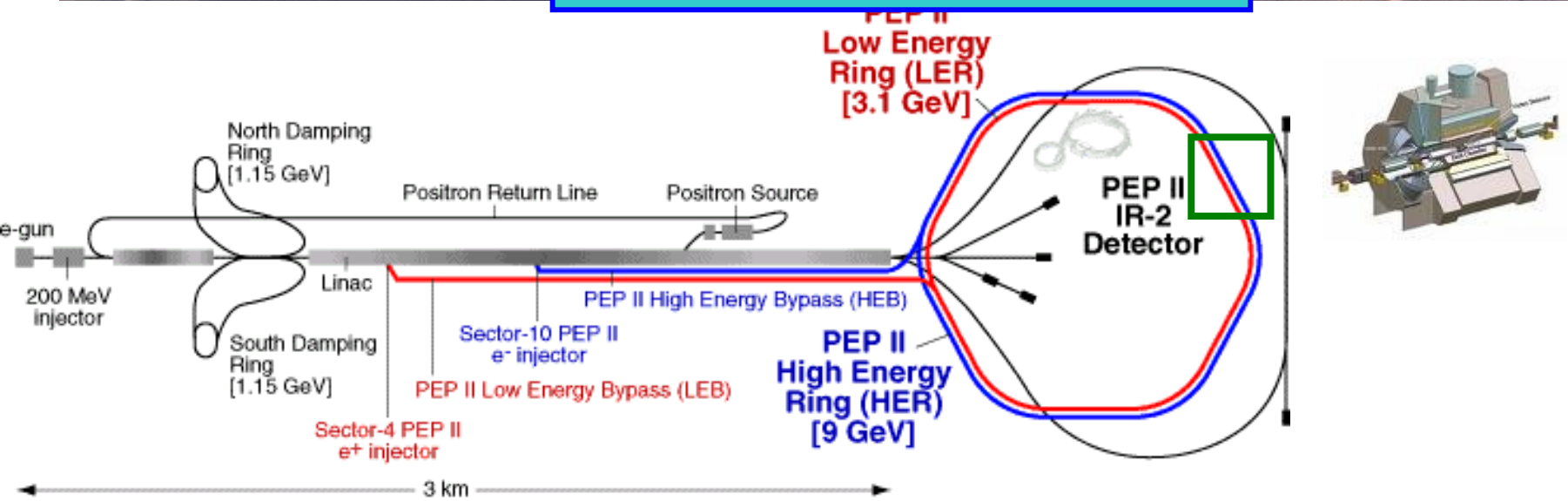
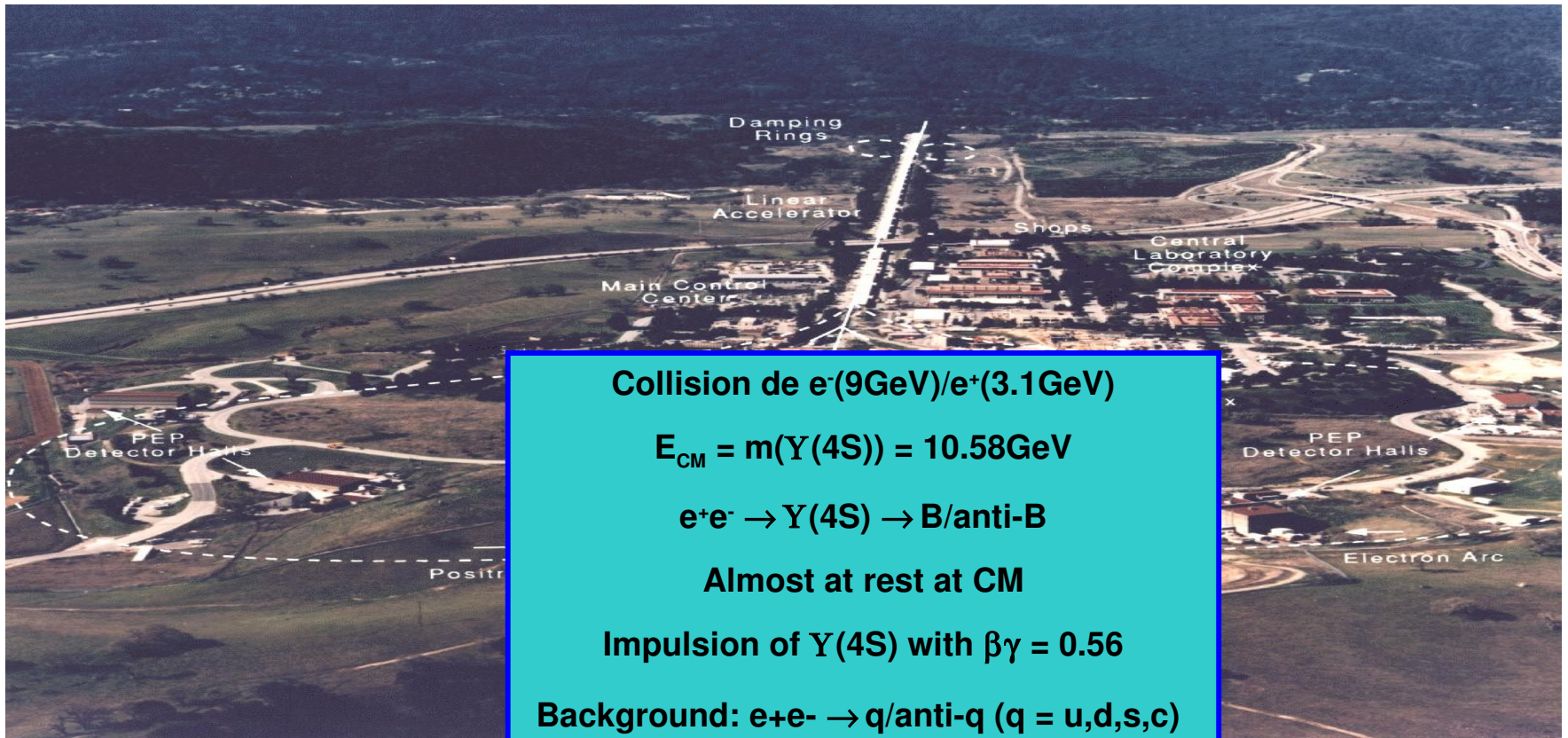


**All measurement compatible between each other
(Compatible with SM)**

Compare "pure tree" measurements with "pure loop" measurements

CKMFitter Group (J. Charles et al.) Eur. Phys. J. C41, 1-131 (2005)



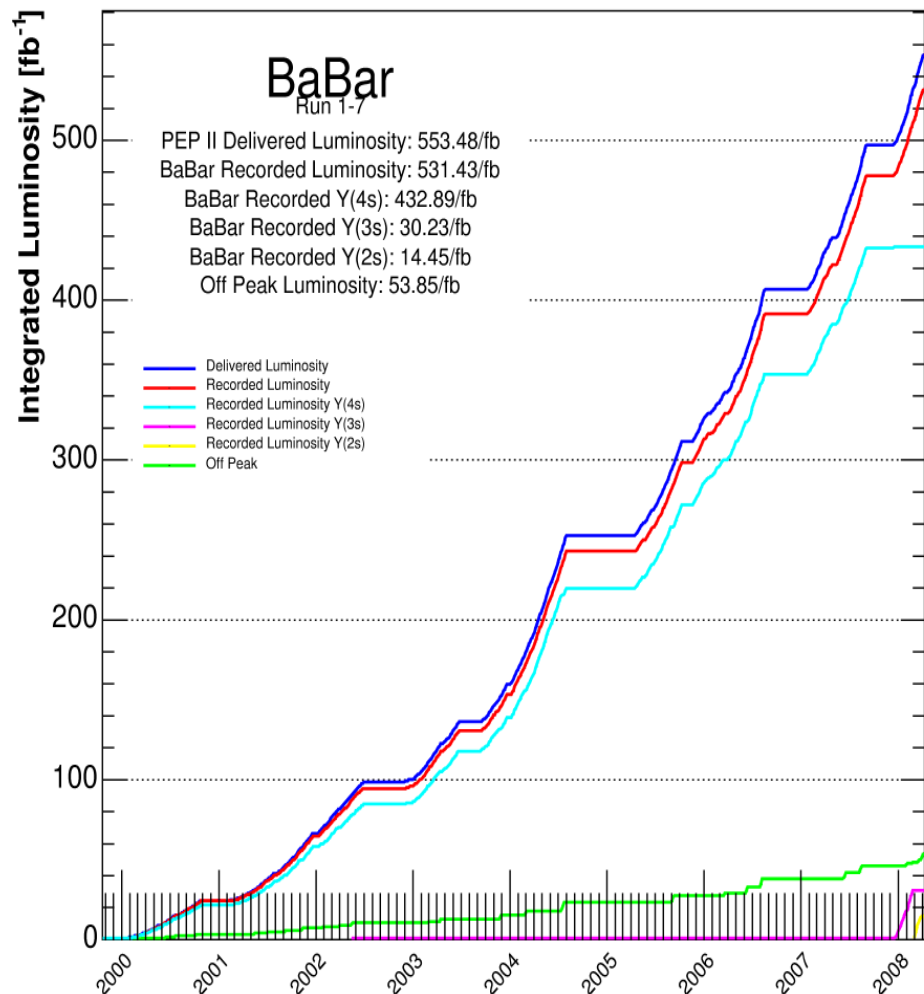




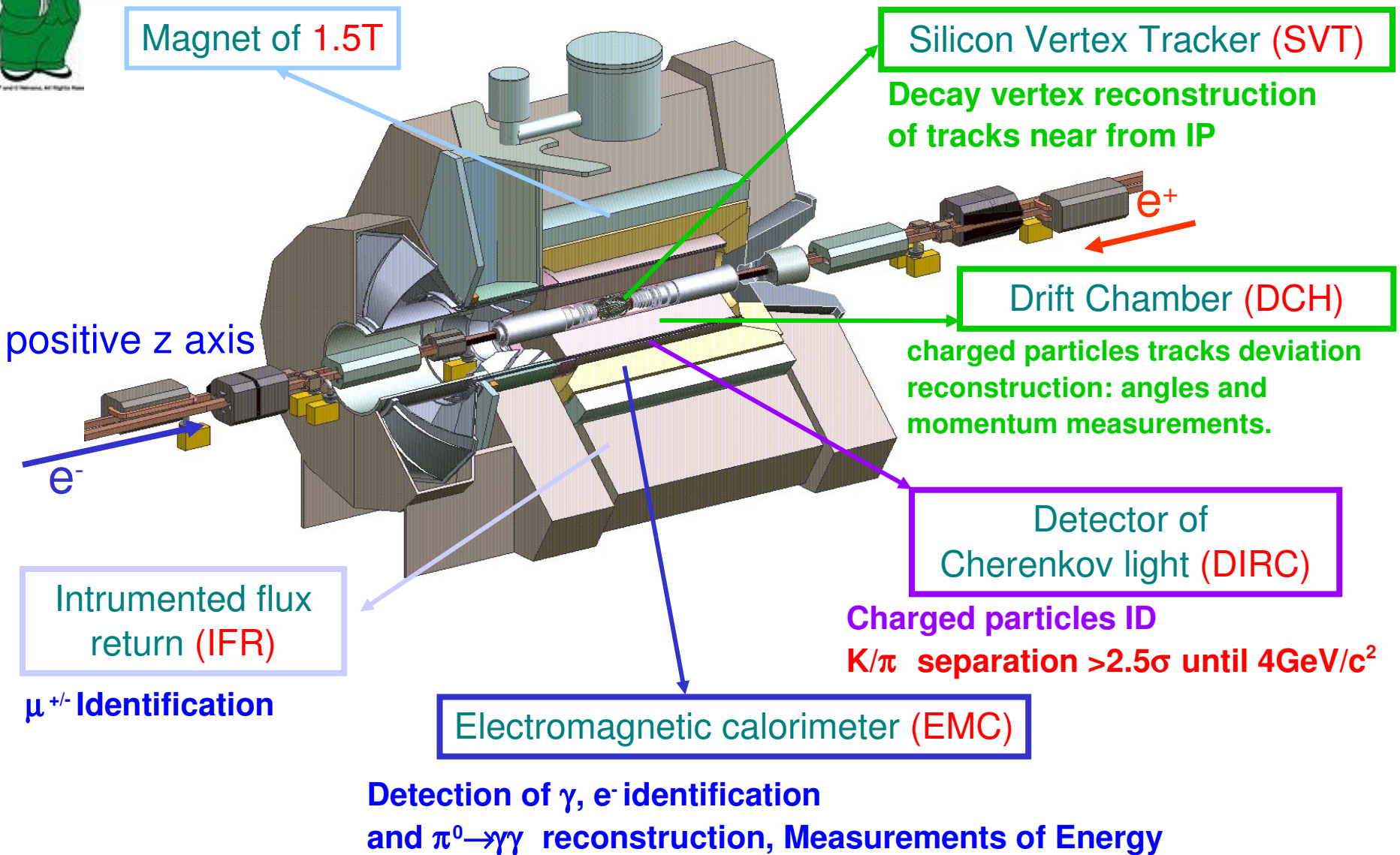
The BaBar Experiment

- Y(4S) data taking ended Dec 2007 ~ 465 M B anti-Bs.
- Have recorded ~ 30/fb on Y(3S) and ~15/fb on Y(2S).
- Routinely collected data at 40MeV below Y(4S) peak (off-peak data) for background characterization.
- Finished running on April 8th

As of 2008/04/11 00:00



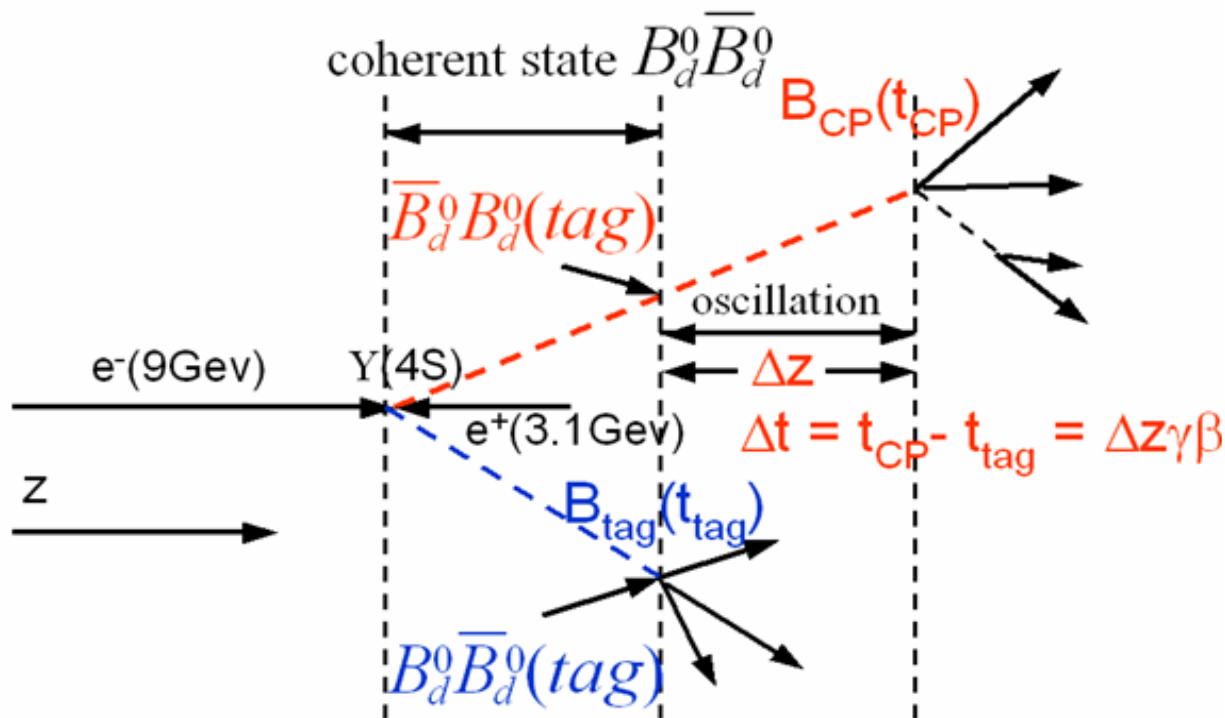
The BaBar Detector





The Δt and tagging measurement

- The neutral B mesons are produced in a coherent B^0 anti- B^0 state
- Flavor B tagging is made with B partner
- Δt measurement from Δz

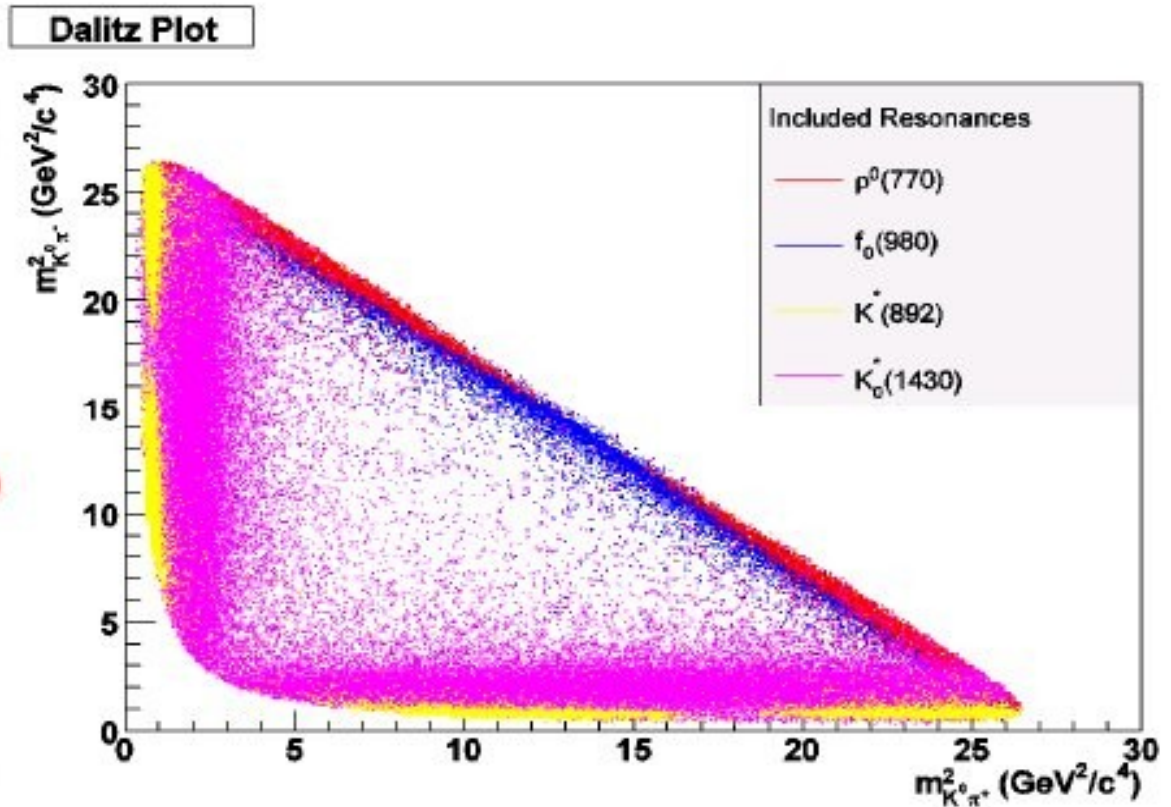




The Dalitz Plot

- 2 degrees of freedom in $B \rightarrow P_1 P_2 P_3$, usually $m^2_{P_1 P_2}$ and $m^2_{P_1 P_3}$:
3 daughters x 3 p comp - 4 (E, p conservation) - 3 Euler angles

Resonances, bands of constant m^2_{12} , m^2_{23} or m^2_{13}
 Overlap \rightarrow interference
 \rightarrow sensitive to relative phase
 Observe intensity $|A|^2$,
 with $A \sim \sum c_i BW_i$ (Isobar)
 c_i characterize model
 so $|A|^2 \sim c_k^* c_l BW_k^* BW_l$
 $k, l > 1$ lift degeneracies
 Ideal to measure phases!





Δt -Dalitz Plot PDF

Time Dalitz Plot and tagging Pdf

$$f(\Delta t, DP, q_{tag}) \propto (|A|^2 + |\bar{A}|^2) \frac{e^{-|\Delta t|/\tau}}{4\tau} \left(1 + q_{tag} \frac{2 \operatorname{Im}[\bar{A}A^*]}{|A|^2 + |\bar{A}|^2} \sin(\Delta m_d \Delta t) - q_{tag} \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} \cos(\Delta m_d \Delta t) \right)$$

Dalitz Plot $\left\{ \begin{array}{l} A(DP) = \sum a_j F_j(DP) \\ \bar{A}(DP) = \sum \bar{a}_j \bar{F}_j(DP) \end{array} \right.$

Isobar Model $\left\{ \begin{array}{l} \text{shapes of intermediate states over DP} \\ \text{CP violation varies over the DP} \end{array} \right.$

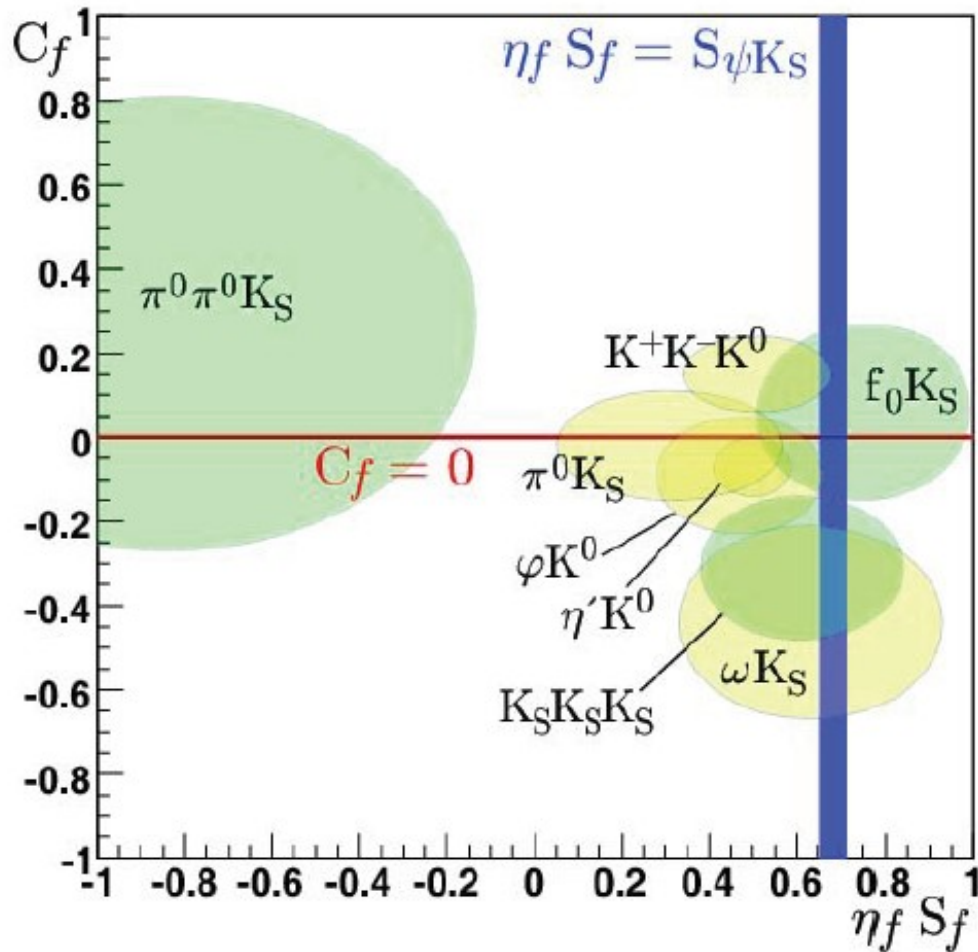
Amplitudes a_j and \bar{a}_j determine DP interference pattern.

Time-Dependent CP Parameters:

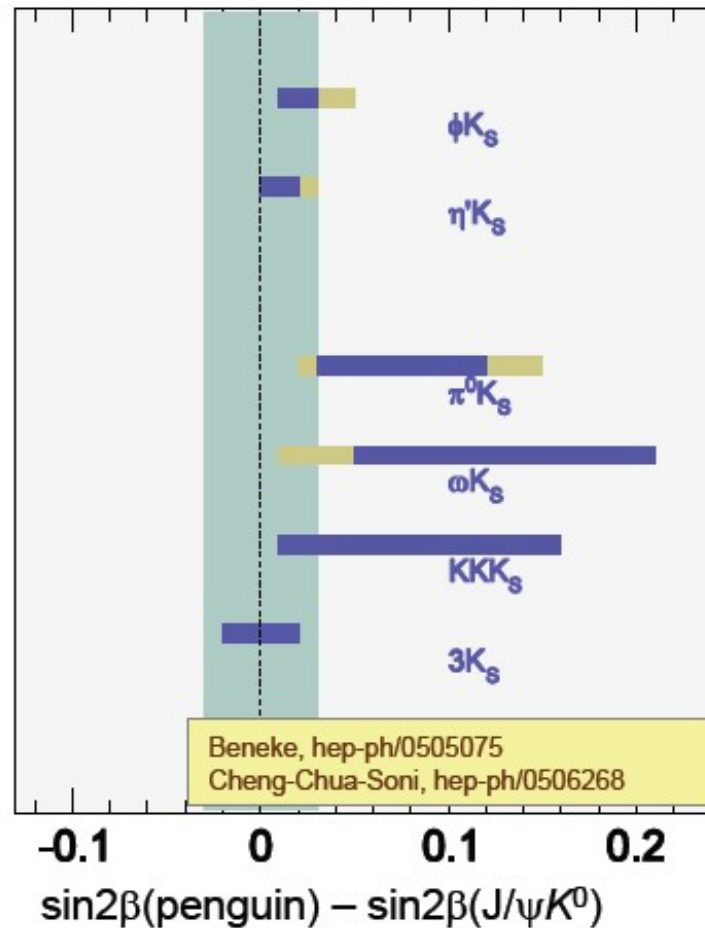
$$C_j = \frac{|a_j|^2 - |\bar{a}_j|^2}{|a_j|^2 + |\bar{a}_j|^2} \quad S_j = \frac{2 \operatorname{Im}[\bar{a}_j a_j^*]}{|a_j|^2 + |\bar{a}_j|^2}$$

interference helps
 disentangling strong and weak phases, and
 thus raises the degeneracy in the
 time-dependent CP parameter S

$b \rightarrow s$ penguins : summary



recent theory estimates :

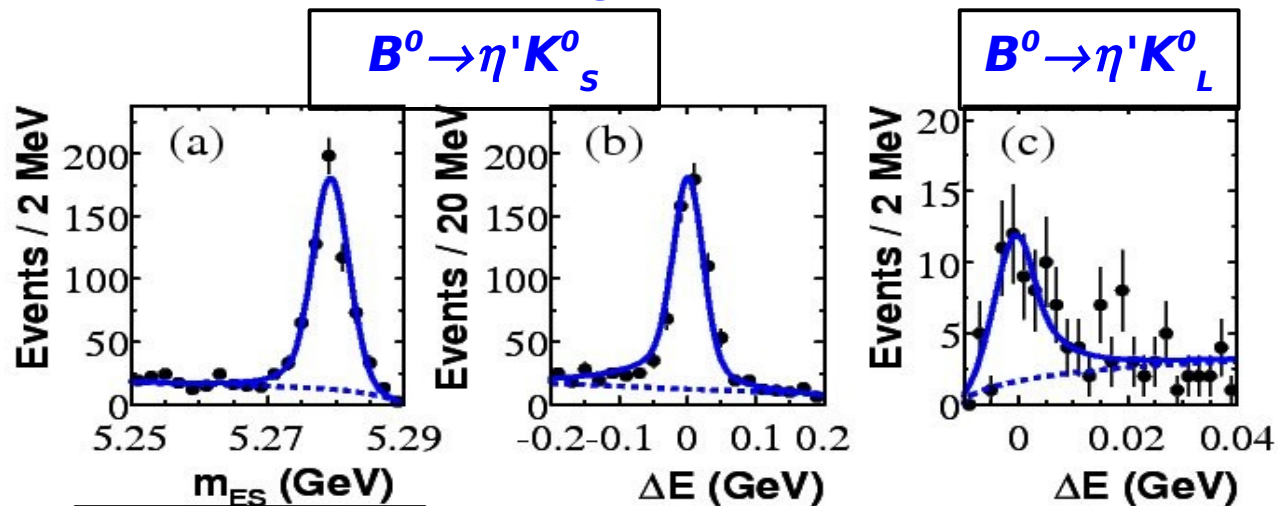




$\sin(\beta_{\text{eff}})$ from $B^0 \rightarrow \eta' K^0$

- Channel have access only to $\sin(\beta_{\text{eff}})$

Samples of:
 $B^0 \rightarrow \eta' K^0_S$ and
 $B^0 \rightarrow \eta' K^0_L$ used.



Measurements:

$C = -0.16 \pm 0.07 \pm 0.03$

$S = 0.58 \pm 0.10 \pm 0.03$

Observed mixing-induced CPV at 5.5σ level